

HESSIAN ENERGY AND  
OPTIMAL PARAMETRISATIONS  
OF SURFACES

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**Abstract** Suppose  $S \subset \mathbb{R}^n$  is a smooth surface with boundary, having the same topological type as the disc. We consider the problem of obtaining “optimal” parametrisations  $Y : \overline{\Omega} (\subset \mathbb{R}^2) \rightarrow S$  where both  $\Omega$  and  $Y$  are arbitrary. We give a positive answer to various formulations of this problem, which we call the *Cartography Problem*. Some examples, related problems, and regularity results are also considered.