Using S-PLUS for Data Analysis & Graphics

J H Maindonald

Statistical Consulting Unit of the Graduate School
Australian National University.

Languages shape the way we think, and determine what we can think about. (Benjamin Whorf)
oz.all
function()
{
  oz()
  points(.Oz.cities)
  points(.Oz.cities$x[7], .Oz.cities$y[7], pch = 16)
  justif <- c(1, 1, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1)
  here <- justif == 0
  cities1 <- lapply(.Oz.cities, function(x, here)
                     x[here], here = here)
  chw <- par()$cxy[1]
  cities1$x <- cities1$x + chw/2
  chh <- par()$cxy[2]
  cities2 <- lapply(.Oz.cities, function(x, here)
                     x[!here], here = here)
  cities2$x <- cities2$x - chw/2
  text(cities1, cities1$name, adj = 0)
  text(cities2, cities2$name, adj = 1)
}
## Contents

<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>Introduction – Why S-PLUS?</td>
<td>1</td>
</tr>
<tr>
<td>1. Starting Up</td>
<td>2</td>
</tr>
<tr>
<td>1.1 Using the Command Window</td>
<td>3</td>
</tr>
<tr>
<td>1.2 A Short S-PLUS Session</td>
<td>4</td>
</tr>
<tr>
<td>1.3 Using the S-PLUS Data Menu</td>
<td>5</td>
</tr>
<tr>
<td>1.4 Further Notational Details</td>
<td>6</td>
</tr>
<tr>
<td>1.5 On-line Help</td>
<td>7</td>
</tr>
<tr>
<td>1.6 Exercises</td>
<td>8</td>
</tr>
<tr>
<td>2. An Overview of S-PLUS</td>
<td>11</td>
</tr>
<tr>
<td>2.1 The Uses of S-PLUS</td>
<td>12</td>
</tr>
<tr>
<td>2.2 The Look and Feel of S</td>
<td>13</td>
</tr>
<tr>
<td>2.3 S-PLUS Objects</td>
<td>14</td>
</tr>
<tr>
<td>2.4 Loops</td>
<td>15</td>
</tr>
<tr>
<td>2.5 S-PLUS Functions</td>
<td>16</td>
</tr>
<tr>
<td>2.6 Vectors</td>
<td>17</td>
</tr>
<tr>
<td>2.7 Data Frames</td>
<td>18</td>
</tr>
<tr>
<td>2.8 Common Useful Functions</td>
<td>19</td>
</tr>
<tr>
<td>2.9 Making Tables</td>
<td>20</td>
</tr>
<tr>
<td>2.10 The Use of attach()</td>
<td>21</td>
</tr>
<tr>
<td>2.11 More Detailed Information</td>
<td>22</td>
</tr>
<tr>
<td>2.12 Exercises</td>
<td>23</td>
</tr>
<tr>
<td>3. Plotting</td>
<td>25</td>
</tr>
<tr>
<td>3.1 plot () and allied functions</td>
<td>26</td>
</tr>
<tr>
<td>3.2 Fine control – Parameter settings</td>
<td>27</td>
</tr>
<tr>
<td>3.3 Adding points, lines and text</td>
<td>28</td>
</tr>
<tr>
<td>3.4 Identification and Location on the Figure Region</td>
<td>29</td>
</tr>
<tr>
<td>3.5 Plots that show the distribution of data values</td>
<td>30</td>
</tr>
<tr>
<td>3.6 Other Useful Plotting Functions</td>
<td>31</td>
</tr>
<tr>
<td>3.7 Guidelines for Graphs</td>
<td>32</td>
</tr>
<tr>
<td>3.8 Exercises</td>
<td>33</td>
</tr>
<tr>
<td>3.9 References</td>
<td>34</td>
</tr>
<tr>
<td>4. Trellis Graphics</td>
<td>35</td>
</tr>
<tr>
<td>4.1 Fine control over the graphics window</td>
<td>36</td>
</tr>
<tr>
<td>4.2 Examples that Present Panels of Scatterplots – Using xyplot ()</td>
<td>37</td>
</tr>
<tr>
<td>4.3 An Incomplete List of Trellis Functions</td>
<td>38</td>
</tr>
<tr>
<td>4.4 Trellis Functions – Further Examples</td>
<td>39</td>
</tr>
<tr>
<td>4.5 The Panel Function</td>
<td>40</td>
</tr>
<tr>
<td>4.6 Adding a Key</td>
<td>41</td>
</tr>
<tr>
<td>4.7 The Subscripts Argument</td>
<td>42</td>
</tr>
<tr>
<td>4.8 Exercises</td>
<td>43</td>
</tr>
<tr>
<td>5. Regression Models and Analysis of Variance</td>
<td>44</td>
</tr>
<tr>
<td>5.1 The Model Formula in Straight Line Regression</td>
<td>45</td>
</tr>
</tbody>
</table>
Introduction – Why S-PLUS?

S-PLUS is a commercial implementation and substantial enhancement of the S data analysis, graphics and programming environment. The data analysis and graphics abilities are implemented in an environment that is attractive for more general interactive commercial and scientific computation. In the words of the citation for John Chambers’ 1998 Association for Computing Machinery Software Award, S has “forever altered how people analyse, visualize and manipulate data.” These notes hope to convey a sense of why it is reasonable to describe S in this way.

Insightful Corporation, who market S-PLUS, have made substantial enhancements to S. They have ported the system across to Microsoft Windows 95, 98 and NT. They developed the graphical user interface that is available for Microsoft Windows environments. The S-PLUS command line language retains some features that reflect S-PLUS’s origin in a Unix environment.

Leading statistical researchers have contributed substantial new statistical analysis abilities. Some of these enhancements are distributed as part of S-PLUS, and some are available separately. Section 13.3 gives useful web addresses for software libraries that are available separately.

Features which S-PLUS offers include:

1. There are extensive and powerful graphics abilities, which are tightly linked with its analytic abilities. Trellis graphics, not widely available elsewhere, are a distinguishing feature of S-PLUS graphics. Trellis graphics provide multi-panel graphical summaries that reflect data structure. These may be very helpful in highlighting major features of the data. Carefully chosen trellis plots often provide clues which may be followed up in subsequent analysis.

2. S-PLUS gives access to a style of interactive statistical analysis that statistical professionals increasingly take for granted.

3. S-PLUS offers a modern and up to date choice of statistical methods. There are ongoing projects that aim to fill perceived gaps.

4. S-PLUS gives access to a sophisticated and relatively state of the art programming language. Professionals who are familiar both with the S language and with the relevant statistical methodology can often rapidly develop any new routine that they need. Analyses need not be limited by the abilities that are immediately available.

5. S-PLUS finds extensive use for rapid prototyping and development of new statistical methods. S-PLUS is used in most major centres that develop new statistical methods for practical use.

6. Because computer-intensive components can be handled by a call to a C function, S-PLUS’s implementation as an interpreted language is not usually a serious handicap.

7. S-PLUS users have access to large libraries of S-PLUS functions that have been developed by Frank Harrell & others (Division of Biostatistics & Epidemiology, Virginia Medical Institute), Brian Ripley (Statistics Department, Oxford University) and Bill Venables (CMIS, CSIRO) and R. J. Tibshirani & others (Statistics Department, Stanford University).

---

1 The S system was developed by Richard A Becker, John M Chambers, Allan R Wilks, William S Cleveland, and colleagues, at AT&T Bell Laboratories. The S system is now a project of Lucent Technologies.
S-PLUS is the statistical computing environment of choice for many highly skilled statistical professionals. As a result, it has received higher levels of critical scrutiny than most other statistical software. Note however that many of the model fitting routines in S-PLUS are leading edge. Some features have not been tested and checked as adequately as one would like. Because the language is powerful it also, inevitably, has elements of subtlety. There are traps which call for special care from users. There are also annoying inconsistencies. Especially when you are doing anything at all complicated, check every step with care.

Jeff Wood (CMIS, CSIRO), Andreas Rukhstuhl (Technikum Winterthur Ingenieurschule, Switzerland), and Ken Brewer (Department of Statistics & Econometrics, ANU) gave me exemplary help in getting this document somewhere near shipshape form. I am indebted to John Braun (University of Winnipeg) for a number of the exercises. I take full responsibility for the errors that remain.

S-PLUS is available from the CMIS division of CSIRO:

  **Web address** [http://www.cmis.csiro.au](http://www.cmis.csiro.au)

  **Email address** S+inquiries@cmis.csiro.au

This document has immediate relevance to the use of S-PLUS under Windows 95. Sections which might be omitted at a first reading are marked with an asterisk.
1. Starting Up

S-PLUS must be installed on your system! If it is not, follow the instructions that came with the installation CD-ROM.

Following installation you should have one or more S-PLUS icons (or a folder containing one or more icons) on your screen. If you have closed the screen icons then click on the START menu, place the mouse cursor on Programs, and look for a program folder that holds the S-PLUS icon(s).

Click on the S-PLUS icon. If there is more than one icon, this will be because you have different icons for different projects or groups of projects. Click on the icon for the project on which you want to work. For this demonstration I will click on my S-course icon.

Here, we will work from the command line. If you do not have a command line window, click on Window (or type Alt/W) and then on Commands Window. On my system the following appears:

![An S-PLUS screen, at the start of a session. We have opened a Commands window, but closed the object browser. There is no script window.](image)

Fig. 1: An S-PLUS screen, at the start of a session. We have opened a Commands window, but closed the object browser. There is no script window.

In interactive use under Microsoft Windows there are several ways to input commands to S-PLUS. One can use any or all of the following three forms of input:

1. Open and work in a command window, typing commands at the command line prompt. For the moment, we will work in a commands window.

2. Open and work in a script window. In the screen snapshot above, there is no script window. To get a script window, go to the File menu.
Commands can be input to the script window from a file, and/or typed in directly. Any commands that are to be input to S-PLUS are highlighted in the script window. Clicking on the arrow in the script toolbar then sends these commands to S-PLUS.

3. Use the graphical user (gui) point and click command interface. In other words, use the icons such as are shown in the screen snapshot. In this course, we will make little use of the graphical user command interface.

Under Unix, the standard form of input is the command line interface. Under both Microsoft Windows and Unix, a further possibility is to run S-PLUS from within the emacs editor.

1.1 Using the Command Window

Here is what appeared in the command window when it was first opened:

```
Working data will be in C:\stats\S-course\_Data
>
```

The command line prompt, i.e. the >, is an invitation to start typing in your commands. For example, type in `2+2` and press the Enter key. Here is what I now have on my screen:

```
Working data will be in C:\stats\S-course\_Data
Data
> 2+2
[1] 4
>
```

Here the result is 4. I will explain the [1] later. The final > indicates that S-PLUS is ready for another command.

Just in case you want to quit from S-PLUS at this point, you should know that the exit or quit command is

```
> q()
```

Alternatives are to click on the File menu and then on Exit, or to click on the X in the top right hand corner of the S-PLUS window.

1.2 A Short S-PLUS Session

We will read into S-PLUS a file that holds the population figures for Australian states and territories, and the total population, at various times since 1917. We will use information from this file to create a graph. Here is the information on the file:

```
Year  NSW  Vic.  Qld  SA  WA  Tas.  NT  ACT  Aust.
1917  1904  1409  683  440  306  193  5   3  4941
1927  2402  1727  873  565  392  211  4   8  6182
1937  2693  1853  993  589  457  233  6  11  6836
1947  2985  2055 1106  646  502  257 11  17  7579
1957  3625  2656 1413  873  688  326 21  38  9640
1967  4295  3274 1700 1110  879  415 52 103 11799
1977  5002  3837 2130 1286 1204  415 104 214 14192
1987  5617  4210 2675 1393 1496  449 158 265 16264
1997  6274  4605 3401 1480 1798  474 187 310 18532
```

The preferred way to input these data is to use the Import Data dialogue under the File menu. This dialogue may be used to import files with a variety of different formats, as well as text files. It offers what is usually the preferred means to import Excel files.

Specify

```
File | Import Data | From File ...
```
Fig. 2 shows a screen snapshot, immediately before clicking on **From File**.

![Fig. 2: The import of data from a file, immediately before clicking on From File…](image)

After clicking on **From File**…, click on the **Look in** pull-down menu and specify that the data are to be found on the A drive. Fig. 3 shows what you should see:

![Fig. 3: The Import Data dialogue.](image)

The names of any `.txt` files on the A: drive are now displayed on the screen. The file we want is `austpop.txt`. Click on this name, causing `austpop.txt` to appear in the File name field. Now click on **Open**, and the data will pop up in a window on the screen. After checking that S-PLUS has entered the column header information correctly and that the data seem correct, you may wish to close the austpop window. The data are now stored as an object in the S-PLUS project directory, with the name `austpop`. There was an option to change the name when the data were read in, but `austpop` seems like a reasonable name, and we will stick with it. Type in `austpop` at the command line prompt. The object will be displayed, thus:
We will learn later that `austpop` is a special form of S-PLUS object, known as a data frame. Data frames that consist entirely of numeric data are similar in structure to numeric matrices.

We will now do a plot of the ACT population between 1917 and 1997. We will first of all remind ourselves of the column names:

```r
> names(austpop)
[1] "Year"  "NSW"   "Vic."  "Qld"    "SA"    "WA"    "Tas."  "NT"    "ACT"   "Aust."
```

A simple way to get the plot is:

```r
> plot(ACT ~ Year, data=austpop, pch=16)
```

The option `pch=16` sets the plotting character to solid black dots. Fig. 4 shows the graph:

![ACT population versus year, over 1917 - 1997.](image)

There is a great deal that we could do to improve this plot. We can specify more informative axis labels, change size of the text and of the plotting symbol, and so on.

If you wish to quit from the S-PLUS session at this point, type

```r
> q()
```

### 1.3 Using the S-PLUS Data Menu
Click on the New Data Frame button on the standard toolbar. The button is in the centre of Fig. 5:

![New Data Frame Button](Image)

Fig.5: The New Data Frame Button

You should then see the following Data Window (Fig. 6)

![Data Window](Image)

Fig. 6: The Data Window. Notice that, for the data frame that will be entered, the default name is SDF1.

You can now start entering data, pretty much as though you were working with a spreadsheet. By default, the data go into a data frame with the name SDF n, where n is the next available number. By right-clicking with the cursor in the body of the sheet, you get a menu. Right click on Properties… to go to a Properties dialogue, where you can change the name of the data frame to any legal name you choose.

Alternatively you can select the Data menu (click on Data), click on New Data Object…, and click on OK.

**1.4 Further Notational Details**

As noted earlier, the command line prompt is

> 

S-PLUS commands (expressions) are typed in following this prompt.

---

2 Multiple commands may appear on the one line, with the semicolon (;) as the separator.
There is also a continuation prompt, used when, following a carriage return, the command is still not complete. By default, the continuation prompt is

```
+
```

In these notes, we often continue commands over more than one line, but omit the + that will appear on the commands window if the command is typed in as we show it.

When typing the names of S-PLUS objects or commands, case is significant. Thus `Austpop` is different from `austpop`. For file names however, the Microsoft Windows conventions apply, and case does not distinguish file names. On Unix systems letters that have a different case are treated as different.

Anything which follows a `#` on the command line is taken as comment, and ignored by S-PLUS.

**Note:** Recall that we had to type `q()` , not `q`, in order to quit from the S-PLUS session. This is because `q` is a function. Typing `q` on its own, without the parentheses, displays the text of the function on the screen. Try it!

### 1.5 On-line Help

To get a help window (under S-PLUS for Windows) with a list of help topics, type in

```
> help()
```

In S-PLUS for Windows, you can alternatively click on the help menu item, and then use key words to do a search. To get help on a specific S-PLUS function, e. g. `plot()`, type in

```
> help(plot)
```

In addition, the official manuals noted in Appendix 1 are available on-line for searching.

In general the supplied documentation does a good job in providing broad-ranging accounts of the methodology, with extensive references to recent literature. It is often short on detail. Users may need to experiment to discover precisely what a specific S-PLUS function does. The documentation may be short on details of the specific formula that has been used.

### 1.6 Exercises

1. The following data give, for each amount by which an elastic band is stretched over the end of a ruler, the distance which the band moved when released:

<table>
<thead>
<tr>
<th>Stretch (mm)</th>
<th>Distance (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>46</td>
<td>148</td>
</tr>
<tr>
<td>54</td>
<td>182</td>
</tr>
<tr>
<td>48</td>
<td>173</td>
</tr>
<tr>
<td>50</td>
<td>166</td>
</tr>
<tr>
<td>44</td>
<td>109</td>
</tr>
<tr>
<td>42</td>
<td>141</td>
</tr>
<tr>
<td>52</td>
<td>166</td>
</tr>
</tbody>
</table>

Enter the data into a data frame `elasticband` (or into a name of your own choosing). Plot distance against stretch.

2. The following ten observations, taken during the years 1970-79, are on October snow cover for Eurasia. (Snow cover is in millions of square kilometers):

<table>
<thead>
<tr>
<th>Year</th>
<th>Cover</th>
</tr>
</thead>
<tbody>
<tr>
<td>1970</td>
<td>8.5</td>
</tr>
<tr>
<td>1971</td>
<td>12.0</td>
</tr>
<tr>
<td>1972</td>
<td>14.9</td>
</tr>
<tr>
<td>1973</td>
<td>10.0</td>
</tr>
</tbody>
</table>
1974  10.7
1975   7.9
1976  21.9
1977  12.5
1978  14.5

i. Enter the data into S-PLUS. You might call the data set snow.cover.

ii. Plot snow cover versus time.

iii. Repeat, after taking logarithms of snow cover.

3. Input the following data, on damage that had occurred in space shuttle launches prior to the disastrous launch of Jan 28 1986. These are the data, for 6 launches out of 24, that were included in the pre-launch charts that were used in deciding whether to proceed with the launch. (Data for the 23 launches where the rocket casing could be recovered is in the data set orings that accompanies these notes.)

<table>
<thead>
<tr>
<th>Temperature (F)</th>
<th>Erosion incidents</th>
<th>Blowby incidents</th>
<th>Total incidents</th>
</tr>
</thead>
<tbody>
<tr>
<td>53</td>
<td>3</td>
<td>2</td>
<td>5</td>
</tr>
<tr>
<td>57</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>63</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>70</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>75</td>
<td>0</td>
<td>2</td>
<td>1</td>
</tr>
</tbody>
</table>

Enter these data into a data frame, with (for example) column names temperature, erosion, blowby and total. Plot total incidents against temperature.
2. An Overview of S-PLUS

This chapter gives brief summary information that should be enough for getting started on the graphics and data analysis exercises in chapters 3-6. Chapters 7 and 8 give more detailed information.

2.1 The Uses of S-PLUS

2.1.1 S-PLUS may be used as a calculator.

S-PLUS evaluates and prints out the result of any expression that one types in at the command line. Remember that S-PLUS expressions are typed following the prompt (>) on the screen. The result is printed on subsequent lines

```r
> 2+2
4
> sqrt(10)
[1] 3.162278
> 2*3*4*5
[1] 120
> 1000*(1+0.075)^5
[1] 435.6293
> pi  # S-PLUS knows about pi
[1] 3.141593
> 2*pi*6378 # Circumference of Earth at Equator, in km; radius is 6378km
[1] 40074.16
> sin(c(30,60,90)*pi/180)  # Convert angles to radians, then take sin()
[1] 0.500 0.866 1.000
```

2.1.2 S-PLUS will provide numerical or graphical summaries of data

There is a special class of object called a data frame, used to store rectangular arrays in which the columns may be vectors of numbers or factors or text strings. Data frames are central to the way that all the more recent S-PLUS routines process data. For now, think of data frames as matrices, where the rows are observations and the columns are variables.

As a first example, consider the supplied data frame `hills`, available from Professor Brian Ripley’s MASS library. This has three columns (variables), with the names `dist`, `climb`, and `time`. Typing in `summary(hills)` gives summary information on these variables. There is one column for each variable, thus:

```r
> summary(hills)

    distance   climb     time
  Min.    : 2.000   Min. : 300   Min. :15.95
  1st Qu. : 4.500   1st Qu. : 725   1st Qu. : 28.00
  Median  : 6.000   Median :1000   Median : 39.75
  Mean    : 7.529   Mean  :1815   Mean  : 57.88
  3rd Qu. : 8.000   3rd Qu. :2200   3rd Qu. : 68.62
  Max.    :28.000   Max. :7500   Max. :204.60
```

Thus we can immediately see that the range of distances (first column) is from 2 miles to 28 miles, and that the range of times (third column) is from 15.95 (minutes) to 204.6 minutes.
We will discuss graphical summaries in the next section.

2.1.3 S-PLUS has extensive abilities for graphical presentation

S-PLUS has two styles of graphics – conventional graphics and trellis graphics. Conventional graphics using `plot()` and related commands requires you to attend to details which trellis graphics may handle fairly automatically. When trellis graphics does not have the immediate features that you need, adaptation to get exactly what you want can sometimes be complicated.

In addition to `plot()` there are functions for adding points and lines to existing graphs, for placing text at specified positions, for specifying tick marks and tick labels, for labelling axes, and so on.

For plotting Fig. 4, you could in fact replace

```r
plot(ACT~Year, data=austpop, pch=16)
```

by

```r
xyplot(ACT~Year, data=austpop, pch=16)
```

The first of these is a conventional graphics command, while the second is a trellis graphics command. The general form of trellis display is a multi-panel display in which the trellis-like layout of the panels can be designed to reflect important features of the data.

Trellis graphics provide various alternative helpful forms of graphical summary. A helpful form of graphical summary for the `hills` data frame is the scatterplot matrix, shown in Fig. 7, that was obtained by typing

```r
splom(~hills) # splom is an acronym for scatterplot matrix
```

![Figure 7: Scatterplot matrix for the Scottish hill race data.](image)

The diagonal panels give the x-axis variables and labels for all panels in the same column. They give the y-axis variables and labels for all panels in the same row.

2.1.4 S-PLUS will handle a variety of specific analyses

The examples that will be given are correlation and regression.

**Correlation:**

```r
> options(digits=3)
```
Suppose we wish to calculate logarithms, and then calculate correlations. We can do all this in one step, thus:

```r
> cor(hills)

distance climb time
dist 1.000 0.652 0.920
climb 0.652 1.000 0.805
time 0.920 0.805 1.000
```

Unfortunately S-PLUS was not clever enough to relabel dist as log(dist), climb as log(climb), and time as log(time). Notice that the correlations between time and distance, and between time and climb, have reduced. Why?

**Straight Line Regression:**

Here is a straight line regression calculation. One specifies an `lm` (= linear model) expression, which S-PLUS evaluates. The data were given in section 1.6. They are stored in the data frame `elasticband`, and the variable names are the names of columns in that data frame. The command asks for the regression of lawn depression on elastic weight.

```r
> plot(stretch~distance, data=elasticband)
> lm(stretch~distance, data=elasticband)
```

```
Call:
  lm(formula = stretch ~ distance, data = elasticband)

Coefficients:
(Intercept) distance
   26.38   0.1395

Degrees of freedom: 7 total; 5 residual
Residual standard error: 2.859
```

For more complete information type:

```r
summary(lm(stretch~distance, data=elasticband))
```

Try it!

### 2.1.5 S-PLUS is an Interactive Programming Language

Suppose we want to calculate the Fahrenheit temperatures which correspond to Celsius temperatures 25, 26, ..., 30. Here is a way to do this in S-PLUS:

```r
> celsius <- 25:30
> fahrenheit <- 9/5*celsius+32
> conversion <- data.frame(Celsius=celsius, Fahrenheit=fahrenheit)
> print(conversion)
```

```
Celsius Fahrenheit
1  25  77.0
2  26  78.8
3  27  80.6
4  28  82.4
5  29  84.2
```
We could also have used a loop. In general it is preferable to avoid loops whenever, as here, there is a good alternative. Loops may involve severe computational overheads.

2.2 The Look and Feel of S

S-PLUS is a function language. There is a language core that uses standard forms of algebraic notation, allowing the calculations described in Section 2.1.1. Beyond this, most computation is handled using functions. Even the action of quitting from an S session uses, as we noted earlier, the function call `q()'.

In most expressions you can treat every object – vectors, arrays, lists and so on – as a whole. Use of operators and functions that operate on objects as a whole largely avoids the need for explicit loops. For an example, look back to section 2.1.5 above.

The structure of an S-PLUS program looks very like the structure of the widely used general purpose language C and its successors C++ and Java.

2.3 S-PLUS Objects

All S-PLUS entities, including functions and data structures, exist as objects. They can all be operated on as data. Type in `ls()' to get a vector of text strings giving the names of all objects in your working directory. An alternative to `ls()' is `objects()'. In both cases you can restrict the names to those with a particular pattern, e.g. starting with the letter ‘p’. However different parameter settings are required depending on whether you use `ls()' or `objects()'.

In S-PLUS 4.0 or later the object browser allows you to filter out what you list, i.e. you can restrict the list to data frames, or to matrices, or to vectors.

Typing the name of an object causes the contents of the object to be printed. Try typing in `q', `mean', etc.

**Important:** Objects that are created stay in place until removed. It pays to remove objects that will be no longer required at the end of each session, while the details are fresh in the mind. Care is needed to avoid removing anything that may be required later.

2.4 Looping

In S-PLUS there is often a better alternative to writing an explicit loop. Where possible, you should use one of the built-in functions to avoid explicit looping. A simple example of a `for' loop

```R
for (i in 1:10) print(i)
```

Here is another example of a `for' loop, to do in a complicated way what we did very simply in section 2.1.5:

```R
> # Fahrenheit to Celsius
```

---

3 Note however that S-PLUS has no header files, most declarations are implicit, there are no pointers, and vectors of text strings can be defined and manipulated directly. The implementation of S-PLUS relies heavily on list processing ideas from the LISP language. Lists are a key part of S-PLUS syntax.

4 Asterisks (*) identify sections which are more technical and might be omitted at a first reading.

5 Other looping constructs are:

```R
repeat <expression>  ## You'll need break somewhere inside
while (x>0) <expression>
```

Here `<expression>' is an S-PLUS statement, or a sequence of statements that are enclosed within braces.
for (fahrenheit in 25:30) print(c(fahrenheit, 9/5*fahrenheit + 32))

[1] 25 77
[1] 26.0 78.8
[1] 27.0 80.6
[1] 28.0 82.4
[1] 29.0 84.2
[1] 30 86

2.4.1 More on looping
Here is a long-winded way to sum the three numbers 3, 5 and 9.

> answer <- 0
> for (j in c(31,51,91){answer <- j+answer}
> answer
[1] 173

The calculation iteratively builds up the object answer, using the successive values of j listed in the vector (31,51,91). i.e. Initially, j = 31, and answer is assigned the value 31 + 0 = 31. Then j = 51, and answer is assigned the value 51 + 31 = 82. Finally, j = 91, and answer is assigned the value 91 + 81 = 173. Then the procedure ends, and the contents of answer can be examined by typing in answer and pressing the Enter key.

There is a much easier way to do this calculation:

> sum(c(31,51,91))
[1] 173

Skilled S-PLUS users have limited recourse to loops. There are often, as in the example above, better alternatives.

2.5 S-PLUS Functions
We give two simple examples of S-PLUS functions.

2.5.1 An Approximate Miles to Kilometers Conversion

> miles.to.km <- function(miles)miles*8/5

The return value is the value of the final (and in this instance only) expression which appears in the function body.

Use the function thus

> miles.to.km(175)  # Approximate distance to Sydney, in miles
[1] 280

You can do the conversion for several distances, all at the one time. To convert a vector of the three distances 100, 200 and 300 miles to distances in kilometers, specify:

> miles.to.km(c(100,200,300))
[1] 160 320 480

2.5.2 A Plotting function
The data set florida has the votes in the 2000 election for the various Presidential candidates, county by county in the state of Florida. The following plots the vote for Buchanan against the vote for Bush.

---

6 Alternatively a return value may be given using an explicit return() statement. This is however an uncommon construction.
Here is a function that makes it possible to plot the figures for any pair of candidates.

```r
plot.florida <- function(xvar="BUSH", yvar="BUCHANAN"){  
  x <- florida[,xvar]  
  y <- florida[,yvar]  
  plot(x, y, xlab=xvar,ylab=yvar)  
  mtext(side=3, line=1,  
    "Votes in Florida, by county, in the 2000 US Presidential election")  
}
```

Note that the function body is enclosed in braces ({ }).

Now try

```r
plot.florida()  
plot.florida(yvar="NADER")  # yvar="NADER" over-rides the default  
plot.florida(xvar="GORE", yvar="NADER")
```

Fig. 8 shows the graph produced by `plot.florida()`.

![Graph showing votes in Florida by county in the 2000 US Presidential election.](image)

**Figure 8:** Votes in Florida, by county, in the election night returns in the 2000 US Presidential election.

### 2.6 Vectors

Examples of vectors are

```r
c(2,3,5,2,7,1)  
3:10  # The numbers 3, 4, ..., 10  
c(T,F,F,F,T,T,F)  
c("Canberra","Sydney","Newcastle","Darwin")
```

16
Vectors may have mode logical, numeric or character. The first two vectors above are numeric, the third is logical (i.e. a vector with elements of mode logical), and the fourth is a string vector (i.e. a vector with elements of mode character).

The missing value symbol, which is NA, can be included as an element of a vector.

### 2.6.1 Joining (concatenating) vectors

The `c` in `c(2, 3, 5, 7, 1)` above was an acronym for “concatenate”, i.e. the meaning is: “Join these numbers together in to a vector. Existing vectors may be included among the elements that are to be concatenated. In the following we form vectors `x` and `y`, which we then concatenate to form a vector `z`:

```r
> x <- c(2, 3, 5, 2, 7, 1)
> y <- c(10, 15, 12)
> z <- c(x, y)
```

We will later meet lists. The concatenate function `c()` may also be used to join lists.

### 2.6.2 Subsets of Vectors

There are two common ways to extract subsets of vectors:

1. Specify the numbers of the elements which are to be extracted, e.g.

```r
> x <- c(3, 11, 8, 15, 12)  # Assign to x the values 3, 11, 8, 15, 12
> x[c(2, 4)]  # Extract elements (rows) 2 and 4
```

One can use negative numbers to omit elements:

```r
> x <- c(3, 11, 8, 15, 12)
> x[-c(2, 3)]
```

2. Specify a vector of logical values. The elements that are extracted are those for which the logical value is `T`. (Beware of NAs, as noted below.) Thus suppose we want to extract values of `x` which are greater than 10.

```r
> x <- c(3, 11, 8, 15, 12)
```

---

7 Below, we will meet the notion of “class”, which is important for some of the more sophisticated language features of S-PLUS. The logical, numeric and character vectors just given have class NULL, i.e. they have no class. There are special types of numeric vector which do have a class attribute. Factors are the most important example. Although often used as a compact way to store character strings, factors are, technically, numeric vectors. The class attribute of a factor has, not surprisingly, the value “factor”.

8 A third more subtle method is available when vectors have named elements. One can then use a vector of names to extract the elements, thus:

```r
c(Andreas=178, John=185, Jeff=183)[c("John", "Jeff")]
```
Arithmetic relations that may be used in the extraction of subsets of vectors are <, <=, >, >=, ==, and ! =. The first four compare magnitudes, == tests for equality, and ! = tests for inequality.

### 2.6.3 The Use of NA in Vector Subscripts

Note that any arithmetic operation or relation that involves `NA` generates an `NA`.

Suppose that one has

```r
y <- c(1, NA, 3, 0, NA)
```

Be warned that `y[y == NA] <- 0` leaves `y` unchanged. The reason is that all elements of `y == NA` evaluate to `NA`. Also `y[NA]` evaluates to `NA`. Where an element on the left of an expression evaluates to `NA`, no assignment is made.

To replace all `NA`s by 0, use

```r
y[is.na(y)] <- 0
```

### 2.6.3 Factors

A factor is a special type of vector, stored internally as a numeric vector with values 1, 2, 3, ..., `m`. The value `m` is the number of levels.

Consider a survey that has data on 691 females and 692 males. If the first 691 are females and the next 692 males, we can create a vector of strings that holds the values thus:

```r
gender <- c(rep("female", 691), rep("male", 692))
```

(TThe usage is that `rep("female", 691)` creates 691 copies of the character string “female”, and similarly for the creation of 692 copies of “male”.)

We can change the vector to a factor, by entering:

```r
gender <- factor(gender)
```

Internally the factor `gender` is stored as 691 1’s, followed by 692 2’s. It has stored with it a table that looks like this:

<table>
<thead>
<tr>
<th></th>
<th>female</th>
<th>male</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

One benefit is that once stored as a factor, the space required for storage is reduced.

In most (but not all) contexts that seem to demand a character string, the 1 is translated into “female” and the 2 into “male”. The values “female” and “male” are the `levels` of the factor. By default, the levels are chosen to be in alphanumeric order, so that “female” precedes “male”.

Hence:

```r
> print(levels(gender))  # Assumes gender is a factor, created as above
[1] "female" "male"
```

---

9 Where there are vectors on both sides of the equation (e.g. `x <- 1:5; x[y>10] <- y[y>10]`), this may have the effect of making the vector of places on the left that are available for assignment shorter than the vector of values that is to be assigned. The result may be nonsense.
The order of the levels in a factor determines the order in which the levels appear in graphs that use this information, and in tables. To cause “male” to come before “female”, use

```r
gender <- factor(gender, levels=c("male", "female"))
levels(gender)  # Check the order of the levels
```

This syntax is available both when the factor is first created, or later when one wishes to change the order in an existing factor. Incorrect spelling of the level names will generate an error message. Try

```r
gender <- factor(c(rep("female", 691), rep("male", 692)))
table(gender)
gender <- factor(gender, levels=c("male", "female"))
table(gender)
gender <- factor(gender, levels=c("Male", "femal e"))  # Generates an error
rm(gender)     # Remove gender.
```

2.7 Data Frames

Data frames are fundamental to the use of the newer style S-PLUS modelling and graphics functions. A data frame is a generalisation of a matrix, in which different columns may have different modes. All elements of any column must however have the same mode, i.e. all numeric or all factor, or all character.

Among the data sets that are supplied to accompany these notes is one called `vehicle.summary`. Here is what one sees when it is printed out:

```r
> vehicle.summary

<table>
<thead>
<tr>
<th>abbrev</th>
<th>Type</th>
<th>Average.Price</th>
</tr>
</thead>
<tbody>
<tr>
<td>Small</td>
<td>Sm</td>
<td>7737</td>
</tr>
<tr>
<td>Medium</td>
<td>Md</td>
<td>21623</td>
</tr>
<tr>
<td>Compact</td>
<td>Cm</td>
<td>15202</td>
</tr>
<tr>
<td>Large</td>
<td>Lr</td>
<td>21500</td>
</tr>
<tr>
<td>NK</td>
<td>-</td>
<td>NA</td>
</tr>
<tr>
<td>Van</td>
<td>Vn</td>
<td>14014</td>
</tr>
<tr>
<td>Sporty</td>
<td>Sp</td>
<td>15308</td>
</tr>
</tbody>
</table>
```

The rows of the data frame have names Small, Medium, . . . To print out the row names, type in

```r
row.names(vehicle.summary)
```

The column names are `abbrev`, `Type`, and `Average.Price`. To print out the column names, type in

```r
names(vehicle.summary)
```

The first two columns are of mode character, and the third of mode numeric. Columns can be vectors of any mode. They can be factors. Note the missing value for `Average.Price` in the fifth row.

Any of the following will pick out the second column of the data frame `type.df`, then storing it in the vector `type`.

```r
type <- vehicle.summary$Type
type <- vehicle.summary[, 2]
type <- vehicle.summary[, "Type"]
type <- vehicle.summary[[2]]  # Take the object that is store d in the second list element.
```

10 Also legal is `vehicle.summary[2]`. This gives a data frame with the single column `Type`. 
2.7.1 Inclusion of character string vectors in data frames

When data are imported using the Import Data dialogue, or when the `data.frame()` function is used to create data frames, vectors of character strings are by default turned into factors. Often this is convenient. If not, there is a setting on the options menu of the Import Data dialogue that will prevent this behaviour. The `as.is=T` parameter setting will prevent this behaviour when `data.frame()` is used to include one or more columns of factors in a data frame.

2.7.2 Built-in data sets

We will often use one of S-PLUS’s built-in data sets, all stored as data frames. One such data frame is `environmental`, giving measurements made on 111 successive days in New York. Here is summary information on this data frame

```r
> summary(environmental)
```

```text
ozone        radiation    temperature         wind            ozone        radiation    temperature         wind            ozone        radiation    temperature         wind            ozone        radiation    temperature         wind
Min.:  1.0      Min.:  7      Min.:57.0      Min.: 2.30      Min.:  1.0      Min.:  7      Min.:57.0      Min.: 2.30      Min.:  1.0      Min.:  7      Min.:57.0      Min.: 2.30      Min.:  1.0      Min.:  7      Min.:57.0      Min.: 2.30
1st Qu.: 18.0   1st Qu.:114   1st Qu.:71.0   1st Qu.: 7.40  : 18.0   1st Qu.:114   1st Qu.:71.0   1st Qu.: 7.40  : 18.0   1st Qu.:114   1st Qu.:71.0   1st Qu.: 7.40  : 18.0   1st Qu.:114   1st Qu.:71.0   1st Qu.: 7.40  : 18.0
Mean: 42.1      Mean:185      Mean:77.8      Mean: 9.94      Mean: 42.1      Mean:185      Mean:77.8      Mean: 9.94      Mean: 42.1      Mean:185      Mean:77.8      Mean: 9.94      Mean: 42.1      Mean:185      Mean:77.8      Mean: 9.94
3rd Qu.: 62.0   3rd Qu.:256   3rd Qu.:84.5   3rd Qu.:11.50   3rd Qu.: 62.0   3rd Qu.:256   3rd Qu.:84.5   3rd Qu.:11.50   3rd Qu.: 62.0   3rd Qu.:256   3rd Qu.:84.5   3rd Qu.:11.50   3rd Qu.: 62.0   3rd Qu.:256   3rd Qu.:84.5   3rd Qu.:11.50
Max.:168.0      Max.:168.0      Max.:168.0      Max.:168.0      Max.:334      Max.:97.0      Max.:20.70      Max.:334      Max.:97.0      Max.:20.70      Max.:334      Max.:97.0      Max.:20.70      Max.:334      Max.:97.0      Max.:20.70
```

See section 14.1 for a list of the built-in data sets to which we will refer in this course.

2.8 Common Useful Functions

- `print()`  # Prints a single S-PLUS object
- `cat()`    # Prints multiple objects, one after the other
- `length()` # Number of elements in a vector or a list
- `mean()`   
- `median()`
- `range()`
- `unique()` # Vector of distinct values
- `diff()`   # Vector of first differences
  
  # N. B. diff(x) has one less element than x
- `sort()`   # Sort elements into order.
- `order()`  # x[order(x)] orders elements of x, with NAs last
- `cumsum()`
- `cumprod()`
- `rev()`    # reverse the order of vector elements

The functions `mean()`, `median()`, `range()`, and a number of other functions, take the argument `na.rm=T`; i.e. remove NAs, then proceed with the calculation.

By default, `sort()` omits any NAs. The function `order()` places NAs last. Hence:

```r
> x <- c(1, 20, 2, NA, 22)
> order(x)
[1] 1 3 2 5 4
> x[order(x)]
[1] 1 2 20 22 NA
> sort(x)
[1] 1 2 20 22
```

11 The data set `air` is identical, except that `ozone` has been replaced by the cube root of ozone level.
2.8.1 Applying a function to all columns of a data frame

The function \texttt{sapply()} does this. It takes as arguments the name of the data frame, and the function that is to be applied. Here are examples, using the supplied data set \texttt{rainforest}.

\begin{verbatim}
> sapply(rainforest, is.factor)
dbh wood bark root rootsk branch species
F F F F F T
> sapply(rainforest[,7], range)  # The final column (7) is a factor
dbh wood bark root rootsk branch
[1,] 4 NA NA NA NA NA
[2,] 56 NA NA NA NA NA
> sapply(rainforest[,7], mean)
dbh wood bark root rootsk branch
16.1 NA NA NA NA NA
\end{verbatim}

The functions \texttt{mean} and \texttt{range}, and several of the other functions noted above, have the parameters \texttt{na.rm}. For example

\begin{verbatim}
range(rainforest$branch, na.rm=T)  # Omit NAs, then determine range
[1] 4 120
\end{verbatim}

One can specify \texttt{na.rm=T} as a third argument to the function \texttt{sapply}. This argument is then automatically passed to the function that is specified in the second argument position. For example:

\begin{verbatim}
> sapply(rainforest[,7], range, na.rm=T)
dbh wood bark root rootsk branch
[1,] 4 3 8 2 0.3 4
[2,] 56 1530 105 135 24.0 120
\end{verbatim}

Chapter 8 has further details on the use of \texttt{sapply()}. There is an example that shows how to use it to count the number of missing values in each column of data.

2.9 Making Tables

\texttt{table()} makes a table of counts. Specify one vector of values (often a factor) for each table margin that is required. Here are some examples

\begin{verbatim}
> table(rainforest$species)  # rainforest is a supplied data set
  Acacia mabellae C. fraseri Acmena smithii B. myrtifolia
     16        12       26       11
> table(barley$year, barley$site)  # barley is a built-in data set
1932        10        10        10        10        10
1931        10        10        10        10        10
\end{verbatim}

\textbf{Warning:} NAs are ignored in tabulations unless you specify otherwise. The action needed to get NAs tabulated under a separate NA category depends, annoyingly, on whether or not the vector is a factor. If the vector is not a factor, specify \texttt{exclude=NULL}. If the vector is a factor named e. g. \texttt{ff}, then you must specify \texttt{na.include(ff)}, rather than \texttt{ff}, as a parameter to \texttt{table()}. 

2.9.1 Chi-Square tests for two-way tables

Use \texttt{chisq.test()} for a test for no association between rows and columns in the output from \texttt{table()}. This assumes that counts enter independently into the cells of a table. For example, the test is invalid if there is clustering in the data.
2.9.2 Number of NAs, broken down by subgroups of the data

The following shows how to get information on the number of NAs in subgroups of the data:

```r
> table(rainforest$species, !is.na(rainforest$branch))
FALSE  TRUE
  Acacia mabe llae   6   10
   C. fraseri      0   12
  Acmena smithii    15   11
  B. myr tifolia    1   10
```

Thus for Acacia mabellae there are 6 NAs for the variable branch (i.e. number of branches over 2cm in diameter), out of a total of 16 data values.

2.10 The Use of attach()

Users have, by default, access both to objects in their own working directory and to objects in a variety of system directories. There is a search list (type `search()` to see this list) that controls where S-PLUS looks first. The `attach` function extends this list.

Users can extend the search list in two ways. S-PLUS data frames can be added to the search list. Alternatively, or in addition, one can add new directories. Adding data frames to the search list is a convenience, so that explicit reference to the data frame from which vectors are taken is not necessary. The addition of new directories is needed so that the users will have access to objects in those directories.

The command `library()` gives access to libraries, which must be already installed, that are not otherwise available. Details of the attaching and detaching of other (non-library) directories will be given later, in chapter 5.

The S-PLUS documentation speaks of attaching databases, as a way of encompassing all these types of extension.

2.10.1 Attaching Data Frames

A data frame is in fact a specialised list, with its columns as the objects. Once a data frame has been added to the search list, the user can refer to the columns by name, without the need to specify the data frame to which they belong. If there is any overlap of names, the order on the search list determines the name that will be taken.

Thus

```r
attach(vehicle.summary)
```

then allows the user to refer to `Type` and `Average.Price`, where it would otherwise be necessary to type `vehicle.summary$Type` and `vehicle.summary$Average.Price`. This assumes that there are no other variables or columns of attached data frames that have either of these names.

```r
> attach(vehicle.summary)
> Type
Small  Medium  Compact  Large  NK  Van  Sporty
'Small' 'Medium' 'Compact' 'Large' 'Van' 'Sporty'
> Average.Price
Small  Medium  Compact  Large  NK  Van  Sporty
  7737  21623  15202 21500 NA 14014  15308
```

To detach this data frame, type

```r
> detach("vehicle.summary")
```
i.e. quotes are now used.
Note how the use of quotes changes. Specify the name (without quotes) when attaching, and enclose the name between quotes when detaching.

2.10.2 Libraries

Third party libraries that are installed on the user’s system are likely to be attached and appear on the search list only if the user requests them. These are usually attached using the command `library()`. To attach the Venables and Ripley mass library that is included in the S-PLUS distribution, type in

```
library(mass)
```

2.11 More Detailed Information

This chapter has given the minimum detail that seems to me necessary for getting started. Look in chapters 7 and 8 for a more detailed coverage of the topics in this chapter. It may pay, at this point, to glance through chapter 7 to see what is there. Remember also to use the S-PLUS help.

Topics from chapter 7, additional to those covered above, that may be important for relatively elementary uses of S-PLUS include:

- The entry of patterned data (7.1.2)
- The handling of missing values in subscripts when vectors are assigned (7.2)
- Unexpected consequences (e.g. conversion of columns of numeric data into factors) from errors in data (7.3.1).

2.12 Exercises

1. For each of the following code sequences, predict the result. Then use S-PLUS to do the computation:
   a) ```R
   answer <- 0
   for (j in 3:5) { answer <- j + answer }
   ```
   b) ```R
   answer <- 10
   for (j in 3:5) { answer <- j + answer }
   ```
   c) ```R
   answer <- 10
   for (j in 3:5) { answer <- j * answer }
   ```

2. Look up the help for the function `prod()`, and use `prod()` to do the calculation in 1(c) above. Alternatively, how would you expect `prod()` to work? Try it!

3. Add up all the numbers from 1 to 100 in two different ways: using `for` and using `sum`.

4. Multiply all the numbers from 1 to 50 in two different ways: using `for` and using `prod`.

5. The volume of a sphere of radius \( r \) is given by \( 4\pi r^3/3 \). For spheres having radii 3, 4, 5, ..., 20 find the corresponding volumes and print the results out in a table. Construct a data frame with columns `radius` and `volume`.

6. Use `sapply()` to apply the function `is.factor` to each column of the built-in data frame `market.survey`. For each of the columns that are identified as factors, determine the levels. Which columns are ordered factors? [Use `is.ordered()`].

23
3. Plotting

The complex of functions plot(), points(), lines(), text(), mtext(), axis() etc. belong to the earlier style of S-PLUS graphics, that preceded trellis graphics.

3.1 plot() and allied functions

The following are equivalent:

\[ \text{plot}(y \sim x) \]
\[ \text{plot}(x, y) \]

where \( x \) and \( y \) must be the same length. This second form of command is the model that is followed for points(), lines(), text(), etc., which modify the current plot. The command is the model that is followed by points() etc.

Try

\[ \text{plot}((0:20)\times\pi/10, \sin((0:20)\times\pi/10)) \]
\[ \text{plot}((1:30)\times0.92, \sin((1:30)\times0.92)) \]

Comment on the pattern of the points in these graphs. Is it obvious from these graphs that the points lie on a sine curve? One way to make it obvious is to reduce the height of the graphsheet, while keeping the same height.

Here are further examples:

\[ \text{attach(elasticband)} \quad \# \text{SPLUS now knows where to find distance & stretch} \]
\[ \text{plot(distance}\sim\text{stretch}) \]
\[ \text{detach(“elasticband”)}\quad \# \text{Not strictly necessary, but it is well to tidy up.} \]
\[ \text{plot(}\text{ACT }\sim\text{Year, data=austpop, type=’l’}) \]
\[ \text{plot(}\text{ACT }\sim\text{Year, data=austpop, type=’b’}) \]

The points() function adds points to a plot. The lines() function adds lines to a plot. The text() function adds text to the plot. The mtext() function places text in one of the margins. The axis() function gives fine control over axis ticks and labels.

3.1.1 Newer plot methods

Above, I described the default plot method. There are other ways to use plot(). In spite of its ancient ancestry, the plot function has been updated to become a generic function that has special methods for “plotting” different classes of object. For example, you can plot a data frame. Plotting a data frame gives, for each numeric variable, a normal probability plot. Or you can plot the lm object that is created by the use of the lm() modelling function. This is designed to give helpful diagnostic and other information that will aid in the interpretation of regression results.

Try

\[ \text{plot(hills)} \]

3.2 Fine control – Parameter settings

Much of the time, the default settings of parameters, such as character size, are adequate. If however you do need to adjust parameters, the par() function will do this. For example,
increases the text size 25% above the default. The setting \texttt{mex = 1.25} may be needed to ensure that there is room in the margin for the increased text size.

On the first use of \texttt{par()} to make changes to the current device, it is a good idea to store the existing settings, for later restoration if this is required. In order to store the existing settings in \texttt{oldpar}, before making changes to parameters (here \texttt{cex} and \texttt{mex}), specify

\begin{verbatim}
oldpar <- par(cex=1.25, mex=1.25)
\end{verbatim}

One can then restore the original parameter settings later, with \texttt{par(oldpar)}.

For example

\begin{verbatim}
attach(elasticband)
oldpar <- par(cex=1.5, mex=1.5)
plot(distance-stretch)
par(oldpar)       # Restores the earlier settings
detach("elasticband")
\end{verbatim}

Inside a function it is a good idea to specify, e.g.

\begin{verbatim}
oldpar <- par(cex=1.25, mex=1.25)
on.exit(par(oldpar))    # Restores the settings on exiting the function
\end{verbatim}

### 3.2.1 Multiple plots on the one page

The parameter \texttt{mfrow} can be used to configure the graphics sheet so that subsequent plots appear row by row, one after the other in a rectangular layout, on the one page. If you want a column by column layout, then use \texttt{mfcol}. In the example below we look at four different transformations of the primates data.

\begin{verbatim}
par(mfrow=c(2,2), pch=16)
attach(primates)  # Needed if primates is not already attached.
plot(Bodywt,Brainwt)
plot(sqrt(Bodywt),sqrt(Brainwt))
plot((Bodywt)^0.1,(Brainwt)^0.1)
plot(log(Bodywt),log(Brainwt))
detach("primates")
par(mfrow = c(1,1), pch=1)
\end{verbatim}

### 3.2.2 The shape of the graph sheet

Often it is desirable to exercise control over the shape of the graph page, e.g. so that the individual plots are approximately square. In S-PLUS for windows you can use \texttt{graphsheet()} to set up the graphics page. It takes the parameters \texttt{width} (in inches), \texttt{height} (in inches) and \texttt{pointsize} (in 1/72 of an inch). The setting of \texttt{pointsize} (default =12) determines character heights. It is the relative sizes of these parameters that matter for screen display or for incorporation into Word and similar programs. Graphs can be enlarged or shrunk by pointing at one corner, holding down the left mouse button, and pulling.

### 3.3 Adding points, lines and text

Here is a simple example that shows how to use the function \texttt{text()} to add text labels to the points on a plot.

\begin{verbatim}
> primates
        Bodywt  Brainwt
Potar monkey  10.0    115
\end{verbatim}
<table>
<thead>
<tr>
<th></th>
<th>Bodywt</th>
<th>Brainwt</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gorilla</td>
<td>207.0</td>
<td>406</td>
</tr>
<tr>
<td>Human</td>
<td>62.0</td>
<td>1320</td>
</tr>
<tr>
<td>Rhesus monkey</td>
<td>6.8</td>
<td>179</td>
</tr>
<tr>
<td>Chimp</td>
<td>52.2</td>
<td>440</td>
</tr>
</tbody>
</table>

attach(primates)  # Needed if primates is not already attached.

plot(Bodywt, Brainwt, xlim=c(5, 240))

# Specify xlim so that there is room for the labels
text(x=Bodywt, y=Brainwt, labels=row.names(primates), adj=0)
# adj=0 implies left adjusted text

Fig. 9 shows the result.

![Figure 9: Plot of the primate brain weight data, with row names as labels.](image)

Fig. 9 would be adequate for identifying points, but is not a presentation quality graph.

Fig. 10 shows how to improve it.

![Figure 10: Improved version of Fig. 9.](image)
We stop text from over-writing the point symbols, and we improve the labelling of the axes. We use the `xlab` (x-axis) and `ylab` (y-axis) parameters to specify meaningful axis titles. We move the labelling to one side of the points by the use of appropriate horizontal and vertical offsets. We use `chw <- par()$cxy[1]` to get a 1-character space horizontal offset. We use `pch=16` to make the plot character a heavy black dot. This helps make the points stand out against the labelling.

Here is the S-PLUS code:

```s-plus
plot(x=Bodywt, y=Brainwt, pch=16, plot(x=Bodywt, y=Brainwt, pch=16, plot(x=Bodywt, y=Brainwt, pch=16, plot(x=Bodywt, y=Brainwt, pch=16, xlab="Body weight (kg)", ylab="Brain weight (g)", xlim=c(5,240))  
chw <- par()$cxy[1]  # Character width text(x=Bodywt+0.75*chw, y=Brainwt, labels=row.names(primates), adj=0)text(x=Bodywt+0.75*chw, y=Brainwt, labels=row.names(primates), adj=0)text(x=Bodywt+0.75*chw, y=Brainwt, labels=row.names(primates), adj=0)text(x=Bodywt+0.75*chw, y=Brainwt, labels=row.names(primates), adj=0)
detach("primates")
```

### 3.3.1 Adding Text in the Margin

```
mtext(side, line, text, ..) adds text in the margin of the current plot. The sides are numbered 1(x-axis), 2(y-axis), 3(top) and 4.
```

### 3.4 Identification and Location on the Figure Region

Two functions are available for this purpose. They are for use once a graph has been drawn.

- `identify()` labels points. One positions the cursor near the point that is to be identified, and clicks the left mouse button.
- `locator()` prints out the co-ordinates of points. One positions the cursor at the location for which coordinates are required, and clicks the left mouse button.

A click with the right mouse button signifies that the identification or location task is complete, unless the setting of the parameter `n` is reached first. For `identify()` the default setting of `n` is the number of data points, while for `locator()` the default setting is `n = 500`.

#### 3.4.1 identify()

This function requires specification of a vector `x`, a vector `y`, and a vector of text strings that are available for use a labels. The data set `florida` has the votes in the 2000 election for the various Presidential candidates, county by county in the state of Florida. We plot the vote for Buchanan against the vote for Bush, then invoking `identify()` so that we can label selected points on the plot.

```s-plus
attach(florida)  # if not already attached plot(BUSH, BUCHANAN, xlab="Bush", ylab="Buchanan") identify(BUSH, BUCHANAN, County)
```

Click to the left or right, and slightly above or below a point, depending on the preferred positioning of the label. When labelling is terminated (click with the right mouse button), the row numbers of the observations that have been labelled are printed on the screen, in order.

#### 3.4.2 locator()

Left click at the locations whose coordinates are required

```s-plus
attach(florida)  # if not already attached plot(BUSH, BUCHANAN, xlab="Bush", ylab="Buchanan") locator()
```
The function can be used to mark new points (specify `type="p"`) or lines (specify `type="l"`) or both points and lines (specify `type="b"`).

### 3.5 Plots that show the distribution of data values

We discuss histograms, density plots, boxplots and normal probability plots.

#### 3.5.1 Histograms

The shapes of histograms depend on the placement of the breaks. Fig. 11 is an example:

![Histograms example](image)

**Figure 11:** The two graphs show the same data, but with a different choice of breakpoints.

Here is the code used to plot the histograms:

```r
par(mfrow = c(1, 2))
attach(possum)
here <- sex == "f"
hist(totlngth[here], breaks = 72.5 + (0:5) * 5, ylim = c(0, 20))
hist(totlngth[here], breaks = 75 + (0:5) * 5, ylim = c(0, 20))
par(mfrow = c(1,1))
```

#### 3.5.2 Density Plots

Density plots, now that they are available, are often a preferred alternative to a histogram. In Fig. 12 the histograms from Figure 11 are overlaid with a density plot.

![Density plots example](image)
Density plots do not depend on the choice of breakpoints. The choice of width and type of window, controlling the nature and amount of smoothing, does affect the appearance of the plot. The main effect is to make it more or less smooth.

The density plot can be produced with

```r
plot(density(totlngth[here]), type="l")
```

Note that in Fig. 12 the y-axis for the histogram is labelled so that the area of a rectangle is the frequency for that rectangle. To get the plot on the left, specify:

```r
here <- sex == "f"
dens <- density(totlngth[here])
xlim <- range(dens$x)
ylim <- range(dens$y)
hist(totlngth[here], breaks = 72.5 + (0:5) * 5,
    probability = T, xlim = xlim, ylim = ylim)
lines(dens)
```

### 3.5.3 Boxplots

Here is how to obtain a boxplot of the above data:

```r
boxplot(totlngth[here])
```

```r
detach("possum")
```

Fig. 13 adds information that should assist in the interpretation of boxplots.

![Boxplot of female possum lengths, with additional labelling information.](image)

### 3.5.4 Normal probability plots

`qqnorm(y)` gives a normal probability plot of the elements of `y`. The points of this plot will lie approximately on a straight line if the distribution is Normal. It is a good idea to calibrate your eye
to recognise plots which indicate non-normal variation by doing several normal probability plots for random samples of the relevant size from a normal distribution.

```
attach(possum)
here <- sex == "f"
par(mfrow = c(3,4)) # A 3 by 4 layout of plots
y <- total[here]
qqnorm(y) # Normal probability plot for lengths
for(i in 1:11) qqnorm(rnorm(43)) # Plots for 11 normal random samples
par(mfrow = c(1,1))
detach("possum")
```

![Normal probability plots](image)

**Figure 14:** Normal probability plots. If data are from a normal distribution then points should fall, approximately, along a line. The plot in the top left hand corner shows the 43 lengths of female possums. The other plots are for independent normal random samples of size 43.

Fig. 14 shows the plots that result. There is one unusually small value. Otherwise the distribution for the female possum lengths is as close to normal as many of the other plots.

The idea is an important one. In order to judge whether data are normally distributed, one examines a number of randomly generated samples of the same size from a normal distribution. It is a way to train the eye.

By default, `rnorm()` generates random samples from a distribution with mean 0 and standard deviation 1.

### 3.6 Other Useful Plotting Functions
### 3.6.1 Scatterplot smoothing

`scatter.smooth()` plots points, then adds a smooth curve through the points. For example:

```r
attach(ais)
here <- sex == "f"
plot(pcBfat[here] ~ ht[here], xlab = "Height", ylab = "% Body fat")
scatter.smooth(ht[here], pcBfat[here])
```

### 3.6.2 Adding lines to plots

Use the function `abline()` for this. The parameters may be an intercept and slope, or a vector that holds the intercept and slope, or an lm object. Alternatively it is possible to draw a horizontal line (`h = <height>`), or a vertical line (`v = <ordinate>`).

```r
here <- sex == "f"
plot(pcBfat[here] ~ ht[here], xlab = "Height", ylab = "% Body fat")
abline(lm(pcBfat[here] ~ ht[here]))
```

### 3.6.3 Rugplots

By default `rug(x)` adds, along the x-axis of the current plot, vertical bars showing the distribution of values of `x`. It can however be particularly useful for showing the actual values along the side of a boxplot. Fig. 15 shows a boxplot of the distribution of total lengths of female possums, with a rugplot added along the y-axis.

![Figure 15: Distribution of heights of female athletes.](image)

Here is the code

```r
here <- ais$sex == "f"
boxplot(ht[here], boxwex = 0.15, ylab = "Height")
rug(ht[here], side = 2)
detach("ais")
```
The parameter boxwex is used to control the width of the boxplot. Reduction from the default width often gives a more elegant result.

### 3.7 Guidelines for Graphs

Design graphs to make their point tersely and clearly, with a minimum waste of ink. Label as necessary to identify important features. In scatterplots the graph should attract the eye’s attention to the points that are plotted, and to important grouping in the data. Use solid points when there is little or no overlap.

When there is extensive overlap, use open plotting symbols. Where points are dense, overlapping points will give a high ink density, which is exactly what one wants.

Use scatterplots in preference to bar or related graphs whenever the horizontal axis represents a quantitative effect.

Use graphs from which information can be read directly and easily in preference to those that rely on visual impression and perspective. Thus in scientific papers contour plots are much preferable to surface plots or two-dimensional bar graphs.

Draw graphs so that reduction and reproduction will not interfere with visual clarity.

Explain clearly how error bars should be interpreted — ± SE limits, ± 95% confidence interval, ± SD limits, or whatever. Explain what source of error is represented. It is pointless to present information on a source of error that is of little or no interest.

### 3.8 Exercises

1. Plot the graph of brain weight (brain) versus body weight (body) for the built-in data set brains. Label the axes appropriately.

2. Repeat the plot 1, but this time plotting log(brain weight) versus log(body weight). Use the row labels to label the points with the three largest body weight values. Label the axes in untransformed units.

3. Repeat the plots 1 and 2, but this time place the plots side by side on the one page.

4. The supplied data set huron has mean July average water surface elevations, in feet, IGLD (1955) for Harbor Beach, Michigan, on Lake Huron, Station 5014, for 1860-1986.13

   a) Plot mean.height against year.

   b) Use the identify function to determine which years correspond to the lowest and highest mean levels. That is, type

   ```r
   identify(huron$year,huron$mean.height,labels=huron$year)
   ```

   and use the left mouse button to click on the lowest point and highest point on the plot. To quit, press both mouse buttons simultaneously.

   c) As in the case of many time series, the mean levels are correlated from year to year. To see how each year's mean level is related to the previous year's mean level, use

   ```r
   lag.plot(huron$mean.height)
   ```

   This plots the mean level at year i against the mean level at year i-1.

5. Write versions of plot.florida() that (a) plot the square roots of the numbers of votes on the respective axes; and (b) plot the logarithms of the numbers of votes on the respective axes.

---

6. Try \( x \leftarrow r \text{norm}(10) \). Print out the numbers that you get. Look up the help for \texttt{rnorm}. Now generate a sample of size 10 from a normal distribution with mean 170 and standard deviation 4.

7. Use \texttt{mfrow()} to set up the layout for a 3 by 4 array of plots. In the top 4 rows, show normal probability plots (section 3.4.2) for four separate ‘random’ samples of size 10, all from a normal distribution. In the middle 4 rows, display plots for samples of size 100. In the bottom four rows, display plots for samples of size 1000. Comment on how the appearance of the plots changes as the sample size changes.

8. The function \texttt{runif()} can be used to generate a sample from a uniform distribution, by default on the interval 0 to 1. Try \( x \leftarrow \text{runif}(10) \), and print out the numbers you get. Then repeat exercise 7 above, but taking samples from a uniform distribution rather than from a normal distribution. What shape do the points follow?

9. If you find exercise 8 interesting, you might like to try it for some further distributions. For example \( x \leftarrow r \text{chisq}(10, 1) \) will generate 10 random values from a chi-squared distribution with degrees of freedom 1. The statement \( x \leftarrow \text{rt}(10, 1) \) will generate 10 random values from a t distribution with degrees of freedom 1. Make normal probability plots for samples of various sizes from these distributions.

10. For the first two columns of the data frame \texttt{hills}, examine the distribution using:

(a) histograms

(b) density plots

(c) normal probability plots.

Repeat (a), (b) and (c), now working with the logarithms of the data values.

### 3.9 References


4. Trellis Graphics

Trellis plots allow the use of the layout on the page to reflect meaningful aspects of data structure. They offer other innovations also, that are described in S-PLUS documentation and in articles that you can get from the internet. Go to 

S-PLUS 4.0 and later attaches the Trellis library automatically. In S-PLUS 3.4 for UNIX, use

library(trellis, first=T) 

to attach the Trellis library.

4.1 Fine control over the graphics window

Implementations of trellis under S-PLUS 4.0 and later for Windows have a unified approach to hard copy and screen display. It is often best to print or copy directly from the screen display. A variety of different display formats are available, most of which can be used either for the screen display or for the printer.

S-PLUS 4.0 and later for Windows open the graphics window automatically when it is needed. On occasions it is however desirable to open it explicitly, allowing you to make changes from the default height and width, pointsize, etc.

If you want the default trellis settings, specify

trellis.device(graphsheet)

rather than the standard

graphsheet()

In either case you can set width=, height=, pointsize=, color=, etc.. The parameters width and height are in inches, while pointsize is in units of $\frac{1}{172}$ inch. If you do not want colour you can specify

trellis.device(graphsheet, color=F)

One side effect of setting color=F is that, if you use the groups= parameter when you call a trellis function, different symbols rather than different colours will by default be used to distinguish the different groups.

To close the current graphics window, specify

dev.off()    # closes current graphics device

4.2 Examples that Present Panels of Scatterplots – Using xyplot()

The basic function for use in drawing panels of scatterplots is xyplot(). We will use the S-PLUS built-in data frame CO2 to demonstrate the use of xyplot(). In this data frame uptake and conc are variables, while Type (2 levels), Treatment (2 levels) and Plant (3 levels within each Type and Treatment combination) are factors.

xyplot(uptake~conc|Type+Treatment, data=CO2)  # Simple use of xyplot()
xyplot(uptake~conc|Type+Treatment, data=CO2, panel=panel.smooth)
xyplot(uptake~conc|Type+Treatment, data=CO2, panel=panel.superpose, groups=Plant)
All three of the above commands plot uptake against conc for each combination of Type and Treatment. The second command adds a smooth. The third command uses different colours or different symbols if the plot is black and white, for the different Echinochloa crus-galli plants. 

Fig. 16 shows the output from the third of these sets of commands:

![Fig. 16: Output from xyplot(uptake~conc|Type+Treatment, data=CO2, panel=panel.superpose, groups=Plant)](image)

If you want to smooth separately for the separate groups, you will need to write your own panel function. We will come to that later.

4.2.1 Using Ranges of Continuous Variables to Define Panels
The function `equal.count()` may be used to break a continuous variable down into (possibly overlapping) ranges. For example

```r
hills$climbcat <- equal.count(hills$climb, 3)
# climbcat specifies three overlapping ranges of "climb"
xyplot(time ~ distance | climbcat, data=hills)
```

You can use the parameter `overlap` of `equal.count()` to control the fraction of overlap. By default `overlap` is 0.5, i.e. each successive pair of categories have around half their values in common.

4.3 An Incomplete List of Trellis Functions

```r
splom(~data.frame)                     # Scatterplot matrix
contourplot(numeric1~numeric2*numeric3 , . .)  # Contour plot
levelplot(numeric1~numeric2*numeric3 , . .)    # Glitzy contour display
wireframe(numeric1~numeric2*numeric3 , . .)wireframe(numeric1~numeric2*numeric3 , . .)wireframe(numeric1~numeric2*numeric3 , . .)wireframe(numeric1~numeric2*numeric3 , . .)
bwplot(factor~numeric , . .)           # Box and whisker plot
qq(factor~numeric , . .)qq(factor~numeric , . .)qq(factor~numeric , . .)qq(factor~numeric , . .)
dotplot(character~numeric , . .)       # 1-dim. Display
dotplot(character~numeric , . .)       # 1-dim. Display
barchart(character~numeric , . .)barchart(character~numeric , . .)barchart(character~numeric , . .)barchart(character~numeric , . .)
piechart(character~numeric , . .)      # Pie chart
```

There are a number of other trellis functions.

4.3.1 Trellis Examples and Trellis Help

You can get a list of example functions which demonstrate trellis graphics by typing in

```r
?trellis.examples
```

To see the code for any of these functions, type the name of the example function and press the Enter key. Many of the example trellis functions are more complicated than is really necessary. Nevertheless they often serve as useful models.

To get documentation for arguments to trellis functions, type in

```r
?trellis.args
```

4.4 Trellis Functions – Further Examples

4.4.1 bwplot()

We will do a plot of data from the singer data frame, which gives heights of singers in the New York choral society.

```r
> sapply(singer,is.factor)  # First check the columns of the data set
                      # height voice.part
                      # height voice.part
                      # height voice.part
                      # height voice.part
> bwplot(voice.part~height, data=singer)
```

Fig. 17 shows the result:

![Boxplot of singer data](image)

Fig. 17: Heights of singers in the New York Choral Society, by voice part.
It assists interpretation to know how many points are represented in each boxplot. The `table()` command will give this information:

```r
> table(singer$voice.part)
Bass 2 Bass 1 Tenor 2 Tenor 1 Alto 2 Alto 1 Soprano 2 Soprano 1
26 39 21 21 27 35 30 36
```

### 4.4.2 Scatterplot matrix Examples – `splom()`

The function `splom()` plots out a scatterplot matrix, or perhaps a series of panels of scatterplot matrices. Just as before one can have multiple panels of scatterplot matrices, different symbols may be used for different groups, and so on. Here are some possibilities:

```r
splom(~hillraces)
splom(~kyphosis[,1] | kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
splom(~kyphosis[,1], panel=panel.superpose, groups=kyphosis[,1])
splom(~kyphosis[,1], panel=panel.smooth)
```

Compare the first two displays. The second uses the same panel, but different colours, for “absent” and “present”. Which display do you consider the more helpful?

### 4.5 The Panel Function

The Trellis functions have a default `panel` function as argument. For `xyplot()` the default panel function is `panel.xyplot()`. Thus:

```r
xyplot(uptake~conc|Type+Treatment, data=CO2)
```

is equivalent to:

```r
xyplot(uptake~conc|Type+Treatment, data=CO2, panel=panel.xyplot)
```

A built-in alternative to `panel.xyplot()` is `panel.smooth()`. This fits a smooth curve to the data. A further possibility is to write your own panel function. This allows you to greatly enhance the capabilities of the Trellis library.

If you want different colours for different groups then, as demonstrated earlier, specify the `groups` argument when you call the trellis function, and set `panel` equal to `panel.superpose`. We can control the different colours used for the different groups. Also we can join the points for each plant. Thus we have:

```r
xyplot(uptake~conc|Treatment+Type, data=CO2, panel=panel.superpose,
       groups=Plant, col=2:4, type="b")
```

There are three plants in each panel. So we specified three colours, which are recycled each time we move to a new panel. The parameters `type="b"` and `col=2:4` both get passed to `panel.superpose()`. There are three possible settings for `type`. The default is `type="p"` (points); other settings are `type="l"` (lines), and `type="b"` (both points & lines).

### 4.5.1 A user-defined panel function

Here is how you might, while using `bwplot`, use a rugplot along the x-direction to examine in more detail the distribution of data values in each panel.

```r
bwplot(Type ~ uptake|Treatment, data=CO2,
       panel=function(x,y){ panel.bwplot(x,y); rug(x) } )
```

Of course it would be nice to make the colour of the rug bars different for the two different Types. Here is how to do it. We have to define our own panel function, which calls `panel.bwplot()` and does more besides.

```r
panel.mybw <- function(x,y)
```

38
Note that `Type` has values 1 and 2. When `panel.bwplot` is called to create each individual panel, `uptake` is the x argument, and `Type` is the y argument.

**4.6 Adding a Key**

Keys may be used to identify the plotting symbols, line styles and colours that have been used for different subsets of the data.

We illustrate with a modified and substantially simplified version of the commands in the built-in `example.overplot()` example trellis function. The part of the command that generates the key has been shaded. Notice its somewhat complicated structure. I have specified three list elements – a numeric value `y`, a list with the name `points`, and a list with the name `text`. The value of `y` sets the vertical positioning; the graphics region finishes at around `y = 1`. I have left `x` at its default value, i.e. 0.5:

```r
dotplot(variety~yield | site, data=barley, groups=year,
    panel=panel.superpose, pch=16, col=3:4,
    key=list(y=1.08,
        points=list(pch=16,col=3:4),
        text=list(text=levels(barley$year),col=3:4)
    )
)
```

There are a wide variety of other settings that one can include in the list: `columns` to specify the number of columns into which to divide the key (in the above we might have set `columns=2`), the parameter `between` to specify the distance in character widths between the different key elements, and `between.columns` for use when `columns>1` to specify the distance between columns. The syntax carries across from that for the function `key()`, which can be used to put a key on a graph after it has been drawn. The difference is that one has to make sure that there is space available before the function `key()` is called.

You might want to control the aspect ratio and layout. Try `aspect=0.4` and `layout=c(1,6)` as parameters to `dotplot()`.

**4.7 The Subscripts Argument**

All of the Trellis functions take a `subscripts` argument. If this argument is set to `TRUE (T)`, then "subscripts" can be passed to the panel function. These subscripts can then be used in conditional statements so that the panel function's behaviour depends on the level of the conditioning variable.

The subscripts are useful when variables other than those passed as `x` or `y` or `groups` are to be used in the individual panels. If for example the variable is called `z`, then the values that are relevant to any specific panel can be passed as `z[subscripts]`.

If you want to use `panel.superpose` inside your own function, you must either explicitly pass the `groups` argument, or else include the `...` argument as a parameter to your function, and call `panel.superpose as panel.superpose(x, y, ...)`. The `...` argument must be specified just as it appears. It allows for the passing of additional arguments, at this point unspecified.

Here is how you might fit a separate smooth curve for each of the different plants. This is given here for completeness. First we define a new panel function:
my.panel <- function(x, y, subscripts, groups, …)
{
  gps <- groups[subscripts]
  ugp <- as.character(unique(gps))
  i <- 1
  for(u in ugp) {
    i <- i + 1
    here <- gps == u
    panel.smooth(x[here], y[here], col = i, pch = i, …)
  }
}

To do the trellis graph, proceed as follows:

```r
xyplot(uptake ~ conc | Type + Treatment, data = CO2, panel = my.panel, groups = Plant, span=1)
```

The `span=1` parameter is passed as an unnamed parameter. Whenever a function has … in the list of arguments, this is allowed. It is passed through to `my.panel` and thence to `panel.smooth`, which knows how to extract the value of span from its … list.

### 4.8 Exercises

1. The following data gives milk volume (g/day) for smoking and nonsmoking mothers:
   - Smoking Mothers: 621, 793, 593, 545, 753, 655, 895, 767, 714, 598, 693
   - Nonsmoking Mothers: 947, 945, 1086, 1202, 973, 981, 930, 745, 903, 899, 961
   Present the data (i) in side by side boxplots; (ii) using a dotplot form of display.
   [The data were taken from the paper “Smoking During Pregnancy and Lactation and Its Effects on Breast Milk Volume” (Amer. J. of Clinical Nutrition).]

2. The built-in data frame `environmental` has columns `ozone` (a variable), `radiation` (a variable), `temp` (a variable), and `wind` (a variable). Plot ozone against radiation for each of three temperature ranges, and each of three wind ranges. [Use `equal.count()` to generate the ranges of `temp` and `wind`.

3. Repeat the plot as in example 1, but this time including a scatterplot smooth on each panel.

4. Taking the supplied data frame `ships`, plot `incidents` against `service` for each level of `consyr` (construction period) and for each level of `period` (period of service).

5. Repeat the plot from exercise 4, but now plot `log(incidents+1)` against `log(service)`, and use a different colour or plot symbol for each different `shiptype`.

6. Use suitable trellis plots to explore the built-in `kyphosis` data set.
   [To get details of the variables, type in `help(kyphosis)`.]

7. For the possum data set, generate the following plots for each separate population (Pop) and for each sex (sex) separately:
   a) histograms of `hdlngth` – use `histogram()`;
   b) normal probability plots of `hdlngth` – use `qqmath()`;
   c) density plots of `hdlngth` – use `densityplot()`.

   The histogram function allows you to control the ratio of the y to x scales (`aspect`) and the number of intervals (`nint`). Investigate the effect of varying these. The `densityplot` function allows you to vary parameters `aspect` and `width`. The parameter `width` controls the width of the smoothing window. Investigate the effect of varying these parameters.

8. Import the data frame called `ACF`, from the file `acf.txt`. The data were obtained from an experiment involving 66 rats which were injected with a carcinogen 1, 2 or 3 times. The rats were sacrificed at either TIME = 6, 12 or 24 weeks, and their colons were stained and examined. Each
colon was divided into 6 sections, and the numbers and sizes of aberrant crypt foci (ACF) were evaluated. The average size (AVERAGE) and total number (TOTAL) of ACF were recorded for each section.

(a) Using the `xyplot` function, explore the relation between the total number of ACF and TIME, taking into account the number of injections and the section.

(b) Repeat (a), using AVERAGE in place of TOTAL.

(c) Construct a contour plot of TOTAL versus TIME and SECTION.

(d) Repeat (c), using the `wireframe` plot instead of the contour plot.

(e) Repeat (c) and (d), using AVERAGE in place of TOTAL.

(f) Repeat (c),(d) and (e), using INJECTION in place of SECTION.

(g) Construct box and whisker plots for TOTAL, using TIME as a factor.

(h) Repeat (g), using AVERAGE in place of TOTAL.

(i) Construct normal probability plots for TOTAL, using TIME>12 as the factor. Is there evidence that the distribution of TOTAL for TIME>12 differs from the distribution of TOTAL for TIME <= 12?

(j) Repeat (i), using AVERAGE instead of TOTAL. What can you say about the distributions of AVERAGE for different times?

(k) Use the command

```
  bwplot(TIME~TOTAL|SECTION, data=ACF, panel=function(x,y){ panel.bwplot(x,y);
                  rug(x)} )
```

to create a rugplot.

(l) Repeat (k), replacing SECTION with SECTION+INJECTION.

(m) Construct a dotplot using

```
  dotplot(TIME~TOTAL|SECTION+INJECTION, data=ACF)
```
5. Regression Models and Analysis of Variance

5.1 The Model Formula in Straight Line Regression

We begin with a straight line regression example:

```r
plot(distance ~ stretch, data=elasticband, pch=16)  # Plot the data
```

The code for the regression calculation is:

```r
elastic.lm <- lm(distance ~ stretch, data=elasticband)
```

Here `distance ~ stretch` is a model formula. We will meet more general types of model formulae in the course of this chapter. The output from the regression is an `lm` object, which we have called `elastic.lm`.

Now examine a summary of the regression results. Notice that the documentation of the call gives details of the model formula.

```r
> options(digits=4)
> summary(elastic.lm)
```

```
Call: lm(formula = distance ~ stretch, data = elasticband)
Residuals:
  1         2         3         4         5         6         7      8 
  2.11  -0.321   18.189   0.321   18.189   0.321   18.189   0.321

Coefficients:             Value  Std. Error  t value  Pr(>|t|)
(Intercept)     -63.571  74.332     0.855 0.4311
stretch            4.554   1.543      2.951 0.0319

Residual standard error: 16.3 on 5 degrees of freedom
Multiple R-Squared: 0.635
F-statistic: 8.71 on 1 and 5 degrees of freedom, the p-value is 0.0319

Correlation of Coefficients:
  (Intercept) stretch
stretch       -0.997
```

5.2 Regression Objects

An `lm` object is a list of named elements. Above, we created the object `elastic.lm`. Let us look at the names of its elements:

```r
> names(elastic.lm)
```

```
[1] "coefficients" "residuals" "fitted.values" "effects"  
[5] "R" "rank" "assign" "df.residual"  
[9] "contrasts" "terms" "call"    
```

Various functions are available for extracting information that you might want from the list. This is better than manipulating the list directly. Examples are:

```r
> coef(elastic.lm)
(Intercept) stretch
 -63.57   4.554
```
The function that one uses most often is `summary()`. This is intended to extract the information that users are most likely to want. For example, in section 5.1, we had

```
summary(elastic.lm)
```

There is a plot method for `lm` objects. Fig. 11 shows the result of typing in:

```
par(mfrow = c(2, 2))
plot(elastic.lm, which.plots = c(1,2,4,6), pch = 16)
```

Fig. 18: Diagnostic plots for `lm(distance~stretch, data=elasticband)`

Note that in the S-PLUS help, the argument `which.plots` is not documented.

In addition one can use `plot.gam` for `lm` objects. Fig. 19 shows the output from:

```
plot.gam(elastic.lm, residuals=T, se=T)
```

```
Figure 19: Graph obtained using plot.gam(elastic.lm, residuals=T, se=T)
```
The X-matrix has two columns, one for the constant term, and one for weight. What the graph shows is the contribution of weight in explaining depression, after taking out the effect that is due to the mean. The dotted lines show the bounds that are determined by 95% confidence intervals for the slope of the line.

5.2.1 Pointwise confidence bounds for fitted values

To get 95% confidence bounds for fitted values one would need to incorporate uncertainty in the estimate of the fitted mean. One can get those as follows:

```r
> elastic.hat <- predict(elastic.lm, se=T)
> elastic.cl <- pointwise(elastic.hat, coverage=0.95)
> elastic.cl

$upper:
  1   2   3   4   5   6   7
163.6 210.9 170.9 181.8 159.2 156.3 195.7

$fit:
  1   2   3   4   5   6   7
145.9 182.3 155.0 164.1 136.8 127.7 173.2

$lower:
  1   2   3   4   5   6   7
128.2 153.7 139.1 146.4 114.3 99.07 150.8
```

Here is way to get smoother confidence bounds:

```r
lines(spline(elasticband$stretch, elastic.ci$lower), lty=3)
```

This has the advantage that you do not need to first order the points.

5.3 Model Formulae, and the X Matrix

The model formula for the elastic band example was `distance ~ stretch`. The model formula is a recipe for setting up the calculations. It describes how to set up the model matrix or X matrix, and specifies the vector y of values of the dependent variable. For some of the examples we discuss later, it helps to know what the X matrix looks like. Details for the elastic band example follow.

For the elastic band example the X matrix, with the y-vector alongside, is:

<table>
<thead>
<tr>
<th>X</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stretch (mm)</td>
<td></td>
</tr>
<tr>
<td>1 46</td>
<td>148</td>
</tr>
<tr>
<td>1 54</td>
<td>182</td>
</tr>
<tr>
<td>1 48</td>
<td>173</td>
</tr>
<tr>
<td>1 50</td>
<td>166</td>
</tr>
<tr>
<td>1 44</td>
<td>109</td>
</tr>
<tr>
<td>1 42</td>
<td>141</td>
</tr>
<tr>
<td>1 52</td>
<td>166</td>
</tr>
</tbody>
</table>
The function `model.matrix()` prints out the model matrix. Thus:

```r
> model.matrix(distance ~ stretch, data=elasticband)
                      (Intercept) stretch
1                  1     46
2                  1     54
3                  1     48
4                  1     50
5                  1     44
6                  1     42
7                  1     52
```

Another possibility, with `elastic.lm` calculated as in section 5.1, is:

```r
model.matrix(elastic.lm)
```

The model matrix corresponds directly to the equation for the model. The model is

\[ y = a + b \times x + \text{residual} \]

which we write as

\[ y = 1 \times a + x \times b + \text{residual} \]

For each row, one takes a multiple \( a \) of the value in the first column of the model matrix, a multiple \( b \) of the value in the second column, and adds them, to give fitted values. Another name is predicted values. The aim is to reproduce, as closely as possible, the values in the y-column. The residuals are the differences between the values in the y-column and the fitted values. Least squares regression, which is the form of regression that we describe in this course, chooses \( a \) and \( b \) so that the sum of squares of the residuals is as small as possible.

The following are the fitted values and residuals that we get with the estimates of \( a (=-63.6) \) and \( b (=4.55) \) that a least squares regression program chooses for us:

<table>
<thead>
<tr>
<th>X</th>
<th>( \hat{y} )</th>
<th>y</th>
<th>( y - \hat{y} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \times -63.6 \times 4.55 )</td>
<td>( 1 \times -63.6 + 4.55 \times \text{Stretch} )</td>
<td>Distance (mm)</td>
<td>Observed - Fitted</td>
</tr>
<tr>
<td>1</td>
<td>46</td>
<td>148</td>
<td>148-145.7 = 2.3</td>
</tr>
<tr>
<td>1</td>
<td>54</td>
<td>182</td>
<td>182-182.1 = -0.1</td>
</tr>
<tr>
<td>1</td>
<td>48</td>
<td>173</td>
<td>173-154.8 = 18.2</td>
</tr>
<tr>
<td>1</td>
<td>50</td>
<td>166</td>
<td>166-163.9 = 2.1</td>
</tr>
<tr>
<td>1</td>
<td>44</td>
<td>109</td>
<td>109-136.6 = -27.6</td>
</tr>
<tr>
<td>1</td>
<td>42</td>
<td>141</td>
<td>141-127.5 = 13.5</td>
</tr>
<tr>
<td>1</td>
<td>52</td>
<td>166</td>
<td>166-173.0 = -7.0</td>
</tr>
</tbody>
</table>

Note that we use \( \hat{y} \) [pronounced y-hat] as the symbol for predicted values. They may also be called fitted values.

We might also fit the simpler (no intercept) model. For this we have

\[ y = x \times b + \text{residual} \]

The X matrix then consists of a single column, the x’s.
5.3.1 Model Formulae in General

Here is what model formulae look like:

\[ y \sim x + z \quad : \text{lm, glm, etc.} \]

\[ y \sim x + \text{fac} + \text{fac} : x \quad : \text{lm, glm, aov, etc. (If \text{fac} is a factor and \text{x} is a variable, \text{fac} : x allows a different slope for each different level of \text{fac}.)} \]

Model formulae are widely used to set up most of the model calculations in S-PLUS. However there are some older S-PLUS analysis commands that do not use model formulae. Examples are \text{prcomp()}, \text{cancor()}, \text{mclust()}, \text{hclust()}, \text{ace()}, and \text{avas()}.

The S-PLUS parser makes no distinction between model formulae and the sorts of formulae that are used for specifying trellis plots. The difference may matter once one tries to do something with the formula. By way of reminder, here is a graph formula for trellis plots.

\[ y \sim x \mid \text{fac1} + \text{fac2} \quad : \text{This gives a plot of} \ y \text{ against} \ x \text{ for each different combination of levels of} \text{fac1} \text{ (across the page) and} \text{fac2} \text{ (up the page).} \]

*5.3.2 Manipulating Model Formulae

Model formulae can be assigned, e.g.

\[ \text{formyxz} \leftarrow \text{formula}(y \sim x + z) \]

or

\[ \text{formyxz} \leftarrow \text{formula}("y \sim x + z") \]

The argument to \text{formula()} can be a text string. This makes it straightforward to paste the argument together from components that are stored in text strings. For example

For example

\[ \text{Call:} \]
\[ \text{lm(formula = formds, data = elasticband)} \]

\[ \text{Coefficients:} \]
\[ (\text{Intercept}) \quad \text{distance} \]
\[ 26.3780 \quad 0.1395 \]

5.4 Multiple Linear Regression Models

5.4.1 The Data Frame Rubber

\[ \text{library(mass, first=T)} \]
\[ \text{MASS library for Venables & Ripley (1999) version 5.1} \]

This library is provided by Venables & Ripley <MASS@stats.ox.ac.uk>

It is not supported by MathSoft. Use the command \text{`library(MASS, help=T)'} to view the \text{`readme.txt'} file for this library.

15 The parser is a part of the S-PLUS implementation code. It takes S-PLUS statements and turns them into code which can be more directly executed by the computer.
Use `addMassMenus()` to install the menus and dialogs
removeMassMenus() to remove them

> `splom(~Rubber)`
> `Rubber.lm <- lm(loss~hard+tens, data=Rubber)`
> `summary(Rubber.lm)`

Call: `lm(formula = loss ~ hard + tens, data = Rubber)`
Residuals:
  Min     1Q  Median     3Q    Max
-79.4 -14.6   3.82   19.8   66

Coefficients:
                  Value Std. Error t value Pr(>|t|)
(Intercept)  885.161   61.752    14.334   0.000
hard       -6.571    0.583    -11.267   0.000
 tens       -1.374    0.194     -7.073   0.000

Residual standard error: 36.5 on 27 degrees of freedom
Multiple R-Squared: 0.84
F-statistic: 71 on 2 and 27 degrees of freedom, the p-value is 1.77e-01

Correlation of Coefficients:
         (Intercept)  hard
tens   -0.766   0.299

Now examine diagnostic plots:
```r
par(mfrow=c(2,2))
plot(Rubber.lm, which=c(1,2,4,6))
par(mfrow=c(1,1))
```

`removeMassMenus()` to remove them

5.4.2 Weights of Books

The books to which the data in the data set `oddbooks` (accompanying these notes) refer were chosen to cover a wide range of weight to height ratios. Here are the data:

> `oddbooks`

<table>
<thead>
<tr>
<th>thick</th>
<th>height</th>
<th>width</th>
<th>weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>44</td>
<td>13.5</td>
<td>9.2</td>
</tr>
<tr>
<td>2</td>
<td>29</td>
<td>17.3</td>
<td>10.5</td>
</tr>
<tr>
<td>3</td>
<td>28</td>
<td>19.8</td>
<td>12.6</td>
</tr>
<tr>
<td>4</td>
<td>25</td>
<td>23.5</td>
<td>15.5</td>
</tr>
<tr>
<td>5</td>
<td>18</td>
<td>27.5</td>
<td>18.5</td>
</tr>
<tr>
<td>6</td>
<td>15</td>
<td>29.1</td>
<td>20.5</td>
</tr>
<tr>
<td>7</td>
<td>14</td>
<td>30.5</td>
<td>23.0</td>
</tr>
</tbody>
</table>

> `logbooks <- log(oddbooks)` # We might expect weight to be
>     # proportional to thick * height * width
> `logbooks.lm1 <- lm(weight~thick, data=logbooks)`
> `summary(logbooks.lm1)$coef`

                  Value Std. Error t value Pr(>|t|)
(Intercept)   10.370    0.6005  17.270   0.00001192
 thick      -1.315    0.1902  -6.913  0.00097087

48
The correlations between

We check the scatterplot matrix, and then proceed with the regression calculations.

Note in passing that for this example the X matrix will have three columns – an initial column of

for 20 guinea pigs. The interest is in predicting brain weight given litter size and body weight.

So is weight proportional to thick * height * width?

The correlations between thick, height and width are so strong that if one tries to use more than one of them as an explanatory variables, the coefficients are ill-determined. They contain very similar information, as is evident from the scatterplot matrix. The regressions on height and width give plausible results, while the coefficient of the regression on thick is entirely an artefact of the way that the books were selected.

The design of the data collection really is important for the interpretation of coefficients from a regression equation. The design for these data was about as bad as it gets!

5.4.3 The Data Frame piglitters

The supplied data frame piglitters has data on litter size (3 - 12), body weight and brain weight for 20 guinea pigs. The interest is in predicting brain weight given litter size and body weight.

Note in passing that for this example the X matrix will have three columns – an initial column of ones, and one column each for litter size and body weight.

We check the scatterplot matrix, and then proceed with the regression calculations.

```
> splom(~piglitters) # First look at the scatterplot matrix
> piglitters.lm <- lm(brainwt ~ lsize + bodywt, data=piglitters)
> summary(piglitters.lm, corr=F)
```

```
Call: lm(formula = brainwt ~ lsize + bodywt, data = piglitters)

Residuals:

  Min 1Q Median 3Q Max
-0.023 -0.009882 0.0004512 0.009204 0.01808

Coefficients: Value Std. Error t value Pr(>|t|)
(Intercept) 0.1782 0.0753 2.3664 0.0301
lsize 0.0067 0.0031 2.1361 0.0475
bodywt 0.0243 0.0068 3.5857 0.0023

Residual standard error: 0.01195 on 17 degrees of freedom
Multiple R-Squared: 0.6505
F-statistic: 15.82 on 2 and 17 degrees of freedom, the p-value is 0.0001315
```

Now examine diagnostic plots

```
par(mfrow=c(2,2))
plot(piglitters.lm, which=c(1,2,4,6))
par(mfrow=c(1,1))
```
As an exercise, the reader is invited to carry out the straight line regressions of brain weight on litter size, and of brain weight on body weight. Why is one of these straight line regression coefficients different in sign from the coefficient in the multiple regression equation above? Look at the scatterplot matrix to find an explanation.

Note the form of the model matrix. Type in:
```r
model.matrix(piglitters.lm)
```

### 5.5 Polynomial regression

We show how calculations that have the same structure as multiple linear regression may be used to model a curvilinear response. We build up curves from linear combinations of transformed values. A warning is that the use of polynomial curves of high degree are in general unsatisfactory. Spline curves, which are constructed by joining together low order polynomial curves (typically cubics) in such a way that the slope changes smoothly, are in general preferable.

#### 5.5.1 Polynomial Terms in Linear Models

The data frame `seedrates` that accompanies these notes gives, for each of a number of different seeding rates, the number of barley grain per head.

```r
> plot(grain ~ rate, data=seedrates, pch=16)  # Plot the data
> seedrates.lm2 <- lm(grain~rate+I(rate^2),data=seedrates)
> summary(seedrates.lm2)

Call: lm(formula = grain ~ rate + I(rate^2), data = seedrates)

Residuals:
   1      2      3        4       5
 0.0457  0.0457  0.0457  0.0457  0.0457

Coefficients:        Value Std. Error t value Pr(>|t|)
(Intercept) 24.060   0.456     52.799   0.000
rate      0.067   0.010      0.067   0.978
I(rate^2)  0.000   0.000      3.497   0.073

Residual standard error: 0.115 on 2 degrees of freedom
Multiple R-Squared: 0.996, F-statistic: 256 on 2 and 2 degrees of freedom, the p-value is 0.0039

Correlation of Coefficients:   
   (Intercept) rate   I(rate^2)
rate       0.978  0.941
I(rate^2)  0.941  0.989

> hat <- predict(seedrates.lm2)
> lines(spline(seedrates$rate, hat))
```

---

# Placing the spline fit through the fitted points allows a smooth curve.
# For this to work the values of seedrates$rate must be ordered.

Fig. 20 shows the plot:

![Figure 20: Plot of number of grain per head versus seeding rate, for the barley seeding rate data. The fitted curve is a quadratic.](image)

Again, check the form of the model matrix. Type in:

```r
> model.matrix(grain~rate+I(rate^2),data=seedrates)
```

```
(Intercept) rate I(rate^2)   (Intercept) rate I(rate^2)   (Intercept) rate I(rate^2)   (Intercept) rate I(rate^2)
1       1       1       1           1   50      2500    1   50      2500    1   50      2500    1   50      2500
2           1   75      56252           1   75      56252           1   75      56252           1   75      5625
3           1  100     100003           1  100     100003           1  100     100003           1  100     10000
4           1  125     156254           1  125     156254           1  125     156254           1  125     15625
5           1  150     225005           1  150     225005           1  150     225005           1  150     22500
```

This example demonstrates a way to extend linear models to handle specific types of non-linear relationships. We can use any transformation we wish to form columns of the model matrix. We could, if we wished, add an \( x^3 \) column.

Once the model matrix has been formed, we are limited to taking linear combinations of columns. It is in that sense that we are still in a linear model framework.

### 5.5.2 What order of polynomial?

A polynomial of degree 2, i.e. a quadratic curve, looked about right for the above data. How does one check?

One way is to fit polynomials, e.g. of each of degrees 1 and 2, and compare them thus:

```r
> seedrates.lm1<lm(grain~rate,data=seedrates)
> seedrates.lm1<lm(grain~rate+I(rate^2),data=seedrates)
```

```r
model.matrix(grain~rate+I(rate^2),data=seedrates)
```
```r
> seedrates.lm2 <- lm(grain ~ rate + I(rate^2), data = seedrates)
> anova(seedrates.lm2, seedrates.lm1)
Analysis of Variance Table
Response: grain
                Terms Resid. Df    RSS       Test Df Sum of Sq
1  rate + I(rate^2)         2 0.0263                        
2             rate         3 0.1870 2             rate         3 0.1870 2   1   1   1   I(rate^2) I(rate^2) I(rate^2) I(rate^2) ----0.1607 0.1607 0.1607 0.1607
F Value   Pr(F)
1                1                1                1
2 12.23 0.072942
```

The F-value is large, but on this evidence there are too few degrees of freedom to make a totally convincing case for preferring a quadratic to a line. However the paper from which these data come gives an independent estimate of the error mean square (0.17 on 35 d.f.) based on 8 replicate results that were averaged to give each value for number of grains per head. If we compare the change in the sum of squares (0.1607, on 1 df) with a mean square of 0.17^2 (35 df), the F-value is now 5.4 on 1 and 35 degrees of freedom, and we have p=0.024. The increase in the number of degrees of freedom more than compensates for the reduction in the F-statistic.

```r
> # However we have an independent estimate of the error mean square
> # The estimate is 0.17^2, on 35 df.
> 1 - pf(0.16/0.17^2, 1, 35)
[1] 0.02437
```

Finally note that R^2 was 0.972 for the straight line model. This may seem good, but given the accuracy of these data it was not good enough! The statistic is not an inadequate guide to whether a model is adequate. Even for any one context, R^2 will in general increase as the range of the values of the dependent variable increases. (R^2 is larger when there is more variation to be explained.) A predictive model is adequate when the standard errors of predicted values are acceptably small, not when R^2 achieves some magic threshold.

R^2 may be used for comparing results from different sets of data where the combinations of values of explanatory variables are broadly similar. Even for that purpose, it is a crude measure.

### 5.5.3 Pointwise confidence bounds for the fitted curve

Here is code that will give pointwise 95% confidence bounds. Note that these do not combine to give a confidence region for the total curve! The construction of such a region is a much more complicated task!

```r
> new.df <- data.frame(rate = c((4:14) * 12.5))
> seedrates.lm2 <- lm(grain ~ rate + I(rate^2), data = seedrates)
> fitinfo <- predict(seedrates.lm2, newdata = new.df, se = T)
> cl <- pointwise(fitinfo, coverage = 0.95)
> lines(new.df$rate, cl$fli)
> lines(new.df$rate, cl$lower, lty = 2)
> lines(new.df$rate, cl$upper, lty = 2)
```

The extrapolation has deliberately been taken beyond the range of the data, in order to show how the confidence bounds spread out. Confidence bounds for a fitted line will spread out much more slowly, but are even less believable!
**5.5.4 Spline Terms in Linear Models**

By now, readers of this document will be used to the idea that it is possible to use linear models to fit terms that may be highly nonlinear functions of one or more variables. The fitting of polynomial functions was a simple example of this. Spline functions variables extend this idea further. The splines that I demonstrate are constructed by joining together cubic curves, in such a way the joins are smooth. The places where the cubics join are known as ‘knots’. It turns out that, once the knots are fixed, and depending on the class of spline curves that are used, spline functions of a variable can be constructed as a linear combination of basis functions, where each basis function is a transformation of the variable.

The data frame `cars` accompanies these notes:

```r
> cars.lm <- lm(kWh ~ insulation) # B-spline fit, 1 knot
> ci5 <- pointwise(predict(cars5.lm, se.fit=T), coverage=0.95
> names(ci5)
[1] "fit" "se.fit" "df" "residual.scale"
> lines(cars$speed, ci5$fit)
```

### 5.6 Using Factors in S-PLUS Models

Factors are essential, when there are categorical or “factor” variables, for specifying S-PLUS models. Consider data from an experiment that compared houses with and without cavity insulation. While one would not usually handle these calculations using an `lm` model, it makes a simple example to illustrate the choice of a baseline level, and a set of contrasts. Different choices, although they fit equivalent models, give output in which some of the numbers are different and must be interpreted differently.

We begin by entering the data from the command line:

```r
insulation <- factor(c(rep("without", 8), rep("with", 7)))
# 8 without, then 7 with
kWh <- c(10225, 10689, 14683, 6584, 8541, 12086, 12467, 12669, 9708, 6700, 4307, 10315, 8017, 8162, 8022)
```

To formulate this as a regression model, we take kWh as the dependent variable, and the factor insulation as the explanatory variable.

```r
> options(contrasts = c("contr.treatment", "contr.poly"), digits = 2)
> insulation.lm <- lm(kWh ~ insulation)
> summary(insulation.lm, corr=F)

Call: lm(formula = kWh ~ insulation)

Residuals:
  Min   1Q Median   3Q  Max
-4409 -979  132 1575 3690

Coefficients:
             Value Std. Error  t value Pr(>|t|)
(Intercept) 7890.143  873.753    9.030  0.000
insulation 3102.857 1196.436    2.593  0.022
```

53
Residual standard error: 2310 on 13 degrees of freedom
Multiple R-Squared: 0.34
F-statistic: 6.7 on 1 and 13 degrees of freedom, the p-value is 0.022

The p-value is 0.022, which may be taken to indicate (p < 0.05) that we can distinguish between the two types of houses. But what does the “intercept” of 9441.57 mean, and what does the value for “insulation” of 1551.43 mean? To interpret this, we need to know that the factor levels are, by default, taken in alphabetical order, and that the initial level is taken as the baseline. So with comes before without, and with is the baseline. Hence:

Average for Insulated Houses = 7980.1

To get the estimate for uninsulated houses take 7980.1 + 3102.9 = 10993.0

The standard error of the difference is 1196.4

Warning: Unless you specifically want helmert contrasts (see section 5.6.2), make sure that before fitting any lm model that uses factors you give the command:

```r
options(contrasts = c("contr.treatment", "contr.poly"), digits = 3)
```

[Setting the number of digits is optional; but three is often sensible.]

Another possibility is:

```r
options(contrasts = c("contr.sum", "contr.poly"), digits = 3)
```

Section 5.6.2 will explain why.

5.6.1 The Model Matrix

It often helps to think in terms of the model matrix or X matrix. Here are the X and the y that are used for the calculations. Note that the first eight data values were all withouts:

<table>
<thead>
<tr>
<th>Contrast</th>
<th>kWh</th>
</tr>
</thead>
<tbody>
<tr>
<td>× 7980.1</td>
<td>× 3102.9</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>. . .</td>
<td>. . .</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>. . .</td>
<td>. . .</td>
</tr>
</tbody>
</table>

Type in

```r
model.matrix(kWh~insulation)
```

and check that one gets the above model matrix.

*5.6.2 Other Choices of Contrasts*

There are other ways to set up the X matrix. In technical jargon, there are other contrasts that one can choose. One obvious alternative is to make without the first factor level, so that it becomes the baseline. You can do this in the following way:

```r
> insulation <- factor(insulation, labels=c("without", "with"))
```
Another possibility is to use what are called the “helmert” contrasts. Although this is the S-PLUS default, I recommend that you avoid them. That was the reason for the option setting:

```r
> options(contrasts = c("contr.treatment", "contr.poly"), digits = 2)
```

Here is the output you get if you use the Helmert contrasts:

```
Coefficients:
                Value Std. Error  t value Pr(>|t|)
(Intercept) 9441.571   598.218   15.783  0.000
insulation  1551.429   598.218    2.593  0.022

Residual standard error: 2310 on 13 degrees of freedom
Multiple R-Squared: 0.341
F-statistic: 6.73 on 1 and 13 degrees of freedom, the p-value is 0.0223
```

Here is the interpretation:

- average of (mean for “without”, “mean for with”) = 9441.57
- To get the estimate for insulated houses (the first level), take 9441.57 - 1551.43 = 7890.14
- To get the estimate for insulated houses (the first level), take 9441.57 + 1551.43 = 10993.

The interpretation of the helmert contrasts is simple enough when there are just two levels. With >2 levels, the helmert contrasts give parameter estimates which in general do not make a lot of sense, basically because the baseline keeps changing, to the average for all previous factor levels. You do better to use either the treatment contrasts, or the sum contrasts. With the sum contrasts the baseline is the overall mean. The sum contrasts are sometimes called “analysis of variance” contrasts. You can set the choice of contrasts for each factor separately, with a statement such as:

```r
insulation <- C(insulation, contr=treatment)
```

The statement that we used earlier, i.e.

```r
options(contrasts=c("contr.treatment", "contr.poly"))
```

does this for all factors, except any that have perhaps been set individually.

**5.6.3 Factor Attributes**

Factors are relatively complex objects. Below, we form a factor and then examine its attributes:

```r
> options(contrasts=c("contr.treatment","contr.poly"))
> fac <- factor(1:5)
> attributes(fac)
$levels:
[1] "1" "2" "3" "4" "5"
$class:
[1] "factor"
```

17 To make the sum contrasts the default for all factors, begin your work by specifying `options(contrasts=c("contr.sum", "contr.poly"))`

The Helmert contrasts, which are the default, contrast each level with the average of all earlier levels. The coefficients are half of this difference.

18 The second string element, i.e. "contr.poly", is the default setting for factors with ordered levels. [One uses the function `ordered()` to create ordered factors.]
One can in fact form a factor in such a way that the contrasts matrix is attached to the factor as an attribute. Specify, e.g.

```r
fac <- C(as.factor(1:5), treatment)
```

Suppose we define fac as an ordered factor. Then we get the contrasts that relate to ordered factors, unless we specify otherwise:

```r
fac <- ordered(1:5)
```

The column names are .L (linear), .Q (quadratic), .C (cubic) and ^ 4 (quartic). For an explanation, look up a text which explains the use of orthogonal polynomial terms where factor levels are ordered.

### 5.7 Multiple Lines – Different Regression Lines for Different Species

The terms which appear on the right of the model formula may be variables or factors, or interactions between variables and factors, or interactions between factors. Here we take advantage of this to fit different lines to different subsets of the data.

In the example which follows, we had weights for a porpoise species (Stellena styx) and for a dolphin species (Delphinus delphis). We take \( x_1 \) to be a variable which has the value 0 for Delphinus delphis, and 1 for Stellena styx. We take \( x_2 \) to be body weight. Then possibilities we may want to consider are:

**A:** A single line: \( y = a + b x_2 \)

**B:** Two parallel lines: \( y = a_1 + a_2 x_1 + b x_2 \)
[For the first group (Stellena styx; \( x_1 = 0 \)) the constant term is \( a_1 \), while for the second group (Delphinus delphis; \( x_1 = 1 \)) the constant term is \( a_1 + a_2 \).]

**C:** Two separate lines: \( y = a_1 + a_2 x_1 + b_1 x_2 + b_2 x_1 x_2 \)
[For the first group (Delphinus delphis; \( x_1 = 0 \)) the constant term is \( a_1 \) and the slope is \( b_1 \). For the second group (Stellena styx; \( x_1 = 1 \)) the constant term is \( a_1 + a_2 \), and the slope is \( b_1 + b_2 \).]

We show results from fitting the first two of these models, i.e. A and B:

```r
> options(contrasts = c("contr.treatment", "contr.poly"))
> names(dolphins)
[1] "wt" "heart" "logweight" "logheart" "species"
> xyplot(logheart ~ logweight, data=dolphins,
panel=panel.superpose, groups=dolphins$species,
pch=c(15,16), col=c(1,5), cex=1.5)
> options(digits=4)
> cet.lm1 <- lm(logheart ~ logweight, data = dolphins)
```
Check what the model matrix looks like:

Now look at an output summary:

Check what the model matrix looks like:

Now look at an output summary:

Check what the model matrix looks like:
Now see why it is not worth wasting time on \texttt{cet.lm3}

```r
> anova(cet.lm1, cet.lm2, cet.lm3)
```

\textbf{Analysis of Variance Table}

\begin{verbatim}
Response: logheart

\begin{tabular}{lrrrr}
  Terms & Resid. Df & RSS & Test Df & Sum of Sq & F Value & Pr(F) \\
  \hline
  1 & logweight & 14 & 0.1717 & & & \\
  2 & species + logweight & 13 & 0.0959 & \texttt{+species} & 1 & 0.07581 & 9.585 & 0.0093 \\
  3 & species * logweight & 12 & 0.0949 & \texttt{+species:logweight} & 1 & 0.00095 & 0.120 & 0.7346 \\
  \hline
\end{tabular}
\end{verbatim}

\section*{5.8 Explaining Fuel Consumption – 2 variables, plus the factor Type}

We will use the data frame \texttt{fuel.frame}. First, here are some of the details of this data frame.

```r
> sapply(fuel.frame, is.factor)
```

\begin{verbatim}
Weight Disp. Mileage Fuel Type
  F  F  F  F  T
```

```r
> levels(fuel.frame$Type)
```

\begin{verbatim}
[1] "Compact" "Large" "Medium" "Small" "Sporty" "Van"
```

Now regress \texttt{Fuel} on \texttt{Weight}, \texttt{Disp} and \texttt{Type}

```r
> options(contrasts=c("contr.treatment", "contr.poly"))
```

```r
> fuel.lm <- lm(Fuel ~ Weight + Disp. + Type, data=fuel.frame)
> summary(fuel.lm, corr=F)
```

\textbf{Call: lm(formula = Fuel ~ Weight + Disp. + Type, data = fuel.frame)}

\textbf{Residuals:}

\begin{verbatim}
Min 1Q Median 3Q Max
-0.6973 -0.2444 -0.01367 0.2 0.6363
```

\textbf{Coefficients:}

\begin{verbatim}
(Intercept) 2.9840 0.5757 5.1829 0.0000
Weight 0.0000 0.0003 0.1611 0.8726
Disp. 0.0076 0.0017 4.3616 0.0001
TypeLarge -0.2906 0.2585 -1.1239 0.2662
TypeMedium 0.1490 0.1357 1.0981 0.2772
TypeSmall -0.5436 0.1570 -3.4626 0.0011
TypeSporty 0.3892 0.1400 2.7793 0.0076
TypeVan 0.9342 0.2086 4.4780 0.0000
```

\textbf{Value Std. Error t value Pr(>|t|)}

| (Intercept)  | 2.9840  | 0.5757  | 5.1829  | 0.0000 |
| Weight       | 0.0000  | 0.0003  | 0.1611  | 0.8726 |
| Disp.        | 0.0076  | 0.0017  | 4.3616  | 0.0001 |
| TypeLarge    | -0.2906 | 0.2585  | -1.1239 | 0.2662 |
| TypeMedium   | 0.1490  | 0.1357  | 1.0981  | 0.2772 |
| TypeSmall    | -0.5436 | 0.1570  | -3.4626 | 0.0011 |
| TypeSporty   | 0.3892  | 0.1400  | 2.7793  | 0.0076 |
| TypeVan      | 0.9342  | 0.2086  | 4.4780  | 0.0000 |
Residual standard error: 0.3139 on 52 degrees of freedom
Multiple R-Squared: 0.8486
F-statistic: 41.65 on 7 and 52 degrees of freedom, the p-value is 0

> res.fuel <- residuals(fuel.lm)  # Store residuals for possible later use

> par(mfrow=c(2,2))
> plot(fuel.lm)  # Gives useful diagnostic plots
> par(mfrow=c(1,1))
> plot.gam(fuel.lm)  # Gives a graphical view of the model
> anova(fuel.lm)

It may be possible to improve on this model, either by transforming one or more of the explanatory variables, or by including interaction terms.

*5.9 aov models (Analysis of Variance)*

The class of models which can be directly fitted as aov models is quite limited. In essence, aov provides, for data where all combinations of factor levels have the same number of observations, another view of an lm model. It has an ability, not available in lm(), to specify the mean square that will be used to estimate the 'error' term.

> sapply(catalyst[4], levels)

# fit main effects and 2 factor interactions
> options(contrasts=c("contr.treatment", "contr.poly"))
> cat.aov2 <- aov(Yield ~ (Temp+Conc+Cat)^2, data=catalyst)
> summary(cat.aov2)  # look at anova table
> summary.lm(cat.aov2)  # Examine effects

Above, we have fitted a model that has all first order interactions. We have one degree of freedom left for estimating error.

*5.9.1 Shading of Kiwifruit Vines*

These data (yields in kilograms) are in the data frame kiwishade which accompanies these notes. They are from an experiment19 where there were four treatments - no shading, shading from August to December, shading from December to February, and shading from February to May. Each treatment appeared once in each of the three blocks. The northernmost plots were grouped in one block because they were similarly affected by shading from the sun. For the remaining two blocks shelter effects, in one case from the east and in the other case from the west, were thought more important. Results are given for each of the four vines in each plot. In experimental design parlance, the four vines within a plot constitute subplots.

19 I am grateful to W. S. Snelgar for the use of these data. Further details, including a diagram showing the layout of plots and vines and details of shelter, are in Maindonald (1992).
The *block:shade* mean square (sum of squares divided by degrees of freedom) provides the error term. (If this is not specified, one still gets a correct analysis of variance breakdown. But the F-statistics and p-values will be wrong.)

```r
> options(contrasts=c("contr.treatment","contr.poly"))
> levels(kiwishade$shade)
[1] "Aug2Dec" "Dec2Feb" "Feb2May" "none"
> lev<-levels(kiwishade$shade)
> kiwishade$shade<-factor(kiwishade$shade,levels=lev[c(2:4,1)])
> kiwishade.aov<-aov(yield~block+shade+Error(block:shade),data=kiwishade)
> summary(kiwishade.aov)

Error: block:shade
     Df Sum of Sq Mean Sq F Value  Pr(>F)
block  2   172.0   86.00  4.1200 0.07488
shade  3 1395.0  464.87 22.2100 0.00119
Residuals  6   126.0  20.99

Error: Within
     Df Sum of Sq Mean Sq F Value Pr(>F)
Residuals 36 438.56  12.18
```

### 5.10 Exercises

1. Here are two sets of data that were obtained the same apparatus, including the same rubber band, as the data frame elasticband. For the data set `elastic1`, the values are:  
   - stretch (mm): 46, 54, 48, 50, 44, 42, 52
   - distance (cm): 183, 217, 189, 208, 178, 150, 249.

   For the data set `elastic2`, the values are:  
   - stretch (mm): 25, 45, 35, 40, 55, 50, 30, 50, 60  

   Using a different symbol and/or a different colour, plot the data from the two data frames `elastic1` and `elastic2` on the same graph. Do the two sets of results appear consistent.

2. For each of the data sets `elastic1` and `elastic2`, determine the regression of stretch on distance. In each case determine (i) fitted values and standard errors of fitted values and (ii) the R² statistic. Compare the two sets of results. What is the key difference between the two sets of data?

3. Use the method of section 5.7 to determine, formally, whether one needs different regression lines for the two data frames `elastic1` and `elastic2`.

4. Using the data in the supplied data frame `ironslag`, plot chemical (i.e. iron content, as measured by a chemical method) against magnetic. Fit a line to this relationship, and plot the line. Then try fitting and plotting a quadratic curve. Does the quadratic curve give a useful improvement to the fit?

   [When you get the fitted values from the quadratic curve, you will need to sort the values of magnetic into increasing order, and apply the same re-arrangement to fitted values. Use `order()` to determine the order in which values of magnetic must be taken, and apply this same re-ordering both to magnetic and to fitted values.]

5. Using the data frame `piglitters`, carry out the straight line regressions of brain weight on litter size, and of brain weight on body weight. Why is one of these straight line regression coefficients different in sign from the corresponding coefficient in the multiple regression equation
of brain weight on litter size and body weight? Look at the scatterplot matrix to find an
explanation.

7. Using the data in the supplied data frame hills, regress time on dist and climb. What can
you learn from the diagnostic plots which you get when you plot the lm object? Try also
regressing log(time) on log(dist) and log(climb). Which of these regression equations
would you prefer?

8. In the supplied data frame beams, regress strength on SpecificGravity and moisture.
Examine the diagnostic plots. What do you observe?

9. Modify the code in section 5.5.3 to fit: (a) a line, with accompanying 95% confidence bounds,
and (b) a cubic curve, with accompanying 95% pointwise confidence bounds. Which of the three
possibilities (line, quadratic, curve) is most plausible? Can any of them be trusted?

10. Type
    ```
    hosp<rep(c("RNC","Hunter","Mater"),2)
    hosphosp<factor(hosp)
    levels(hosphosp)
    ```
    Now repeat the steps involved in forming the factor hosphosp, this time keeping the factor levels in
the order RNC, Hunter, Mater.

    Use contrasts(hosphosp) to form and print out the matrix of contrasts. Do this using helmert
contrasts, treatment contrasts, and sum contrasts. Using an outcome variable

    ```
    y <- c(2,5,8,10,3,9)
    ```
fit the model lm(y~hosphosp), repeating the fit for each of the three different choices of contrasts.
Comment on what you get.

    For which choice(s) of contrasts do the parameter estimates change when you re-order the factor
levels?

11. In section 5.7 check the form of the model matrix (i) for fitting two parallel lines and (ii) for
fitting two arbitrary lines when one uses the sum contrasts. Repeat the exercise for the helmert
contrasts.

5.11 References
397–402.


Prognostic Models: Issues in Developing Models, Evaluating Assumptions and Adequacy, and

of Agricultural Research 35: 121-141.


Williams, G. P. 1983. Improper use of regression equations in the earth sciences. Geology 11:
195-197.
6. Multivariate and Tree-Based Methods

6.1 Multivariate EDA, and Principal Components Analysis

Principal components analysis is often a useful exploratory tool for multivariate data. The supplied data set possum has nine morphometric measurements on each of 102 mountain brushtail possums, trapped at seven sites from southern Victoria to central Queensland. With such data it is sensible to begin by examining relevant scatterplot matrices. This may draw attention to gross errors in the data. A plot in which the sites and/or the sexes are identified will draw attention to any very strong structure in the data. For example one site may be quite different from the others, for some or all of the variables.

Here are some of the possibilities for examining these data:

```
splom(~possum[,6:14], panel=panel.superpose, groups=possum$sex) # We need to exclude missing values
here<-is.na(possum$pes) # We need to exclude missing values
print(sum(here))           # Check how many values are missing
possum.prc <- princomp(possum[!here,6:14])  # Principal components
# Print scores on second pc versus scores on first pc
xyplot(possum.prc$scores[,2] ~ possum.prc$scores[,1]|possum$Pop[!here],
       panel=panel.superpose, groups=possum$sex[!here])
```

Fig. 21 shows the second of these plots:

![Figure 21: Plot of second principal component versus first principal component, for the possum morphometric data.](image)

See chapter 1 of the *S-PLUS 2000 Guide to Statistics*. 
6.2 Cluster Analysis

In the language of Ripley (1996), cluster analysis is a form of unsupervised classification. It is “unsupervised” because the clusters are not known in advance. There are two types of algorithms – algorithms based on hierarchical agglomeration, and algorithms based on iterative relocation. Both types of algorithm are available in S-PLUS.

In hierarchical agglomeration each observation starts as a separate group. Groups that are “close” to one another are then successively merged. The output yields a hierarchical clustering tree which shows the relationships between observations and between the clusters into which they are successively merged. A judgement is then needed on the point at which further merging is unwarranted.

In iterative relocation, the algorithm starts with an initial classification, which it then tries to improve. How does one get the initial classification? Typically, by a prior use of a hierarchical agglomeration algorithm.

6.3 Discriminant Analysis

We start with data which are classified into several groups, and want a rule which will allow us to predict the group to which a new data value will belong. In the language of Ripley (1996), our interest is in supervised classification. For example, we may wish to predict, based on prognostic measurements and outcome information for previous patients, which future patients will remain free of disease symptoms for twelve months or more. Here are calculations for the possum data frame, using the lda() function from the Venables & Ripley MASS library:

```r
> library(MASS, first=T)
> here <- !is.na(possum$pes)
> possum.lda <- lda(site~hdlngth+skullw+totlngth+
+ taill+pes+earconch+eye+chest+belly, data=possum, subset=here)
> possum.lda$svd  # Examine the singular values
[1] 15.7577838  3.9372136  3.1859729
[4]  1.5078461  1.1420103  0.7771947
> plot(possum.lda, dimen=3)  # Scatterplot matrix for scores on 1st 3 canonical variates, as in Fig. 18
```

The singular values are the ratio of between to within group sums of squares, for the canonical variates in turn. Clearly canonical variates after the third have little if any discriminatory power. One can use predict.lda() to get (among other information) scores on the first few canonical variates.

---

20 References are at the end of the chapter.
Where there are two groups, logistic regression is often effective. Perhaps the best source of code for handling more general supervised classification problems is Hastie and Tibshirani’s \texttt{mda} (mixture discriminant analysis) library. There is a brief overview of this library in the Venables and Ripley `Complements’, referred to in section 13.2.

### 6.4 Decision Tree models (Tree-based models)

We include tree-based classification here because it is a multivariate supervised classification, or discrimination, method. A tree-based regression approach is available for use for regression problems. Tree-based methods seem more suited to binary regression and classification than to regression with an ordinal or continuous dependent variable.

Tree-based models, also known as “Classification and Regression Trees” (CART), may be suitable for regression and classification problems when there are extensive data. One advantage of such methods is that they automatically handle non-linearity and interactions. Output includes a “decision tree” which is immediately useful for prediction.

In addition to \texttt{tree()} and related functions, there is a separate \texttt{RPART} library of functions. My preference is for the \texttt{RPART} library.

```r
library(mass)  # Forensic glass fragment data is in mass library
glass.tree <- tree(type ~ RI+Na+Mg+Al+Si+K+Ca+Ba+Fe, data=fgl)
plot(glass.tree); text(glass.tree)
summary(glass.tree)
```

To use these models effectively, it is necessary to know about pruning trees, and about cross-validation.

The Atkinson and Therneau \texttt{RPART} (recursive partitioning) library is closer to CART than is the \texttt{S_PLUS} tree library. Its integration of cross-validation with the algorithm for forming trees gives it advantages over the \texttt{S-PLUS} tree library. See Maindonald (1998).
6.5 Exercises
1. Using the `data.frame` function, convert the object `testscores` into an S-PLUS data frame. Apply principal components analysis to the scores for `diffgeom`, `complex`, `algebra`, and `reals`. Plot the scores for the first principal component against the statistics scores.
2. Apply principal components analysis to the four response variables `pre.mean`, `post.mean`, `pre.dev` and `post.dev` in the dataframe `wafer`. Use `xyplot` to plot the second principal component scores against the first principal component scores for each value of `maskdim`.
3. (a) Use
   ```
predict(kyphosis.tree, data.frame(Kyphosis=NA, Age=11, Number=3, Start=5))
   ```
to predict whether kyphosis will be present or absent for an 11-month-old whose operation involved 3 vertebrae starting at the 5th. What about a 36-month-old whose operation involved 6 vertebrae starting at the 7th.
(b) Use
   ```
summary(kyphosis.tree)
   ```
to obtain an estimate of the misclassification rate.
4. The `mass` library has the `Aids2` data set, containing de-identified data on the survival status of patients diagnosed with AIDS before July 1 1991. Use tree-based classification (`rpart()`) to identify major influences on survival.
5. Investigate discrimination between plagiotropic and orthotropic species in the data set `leafshape`.

6.6 References
Therneau, T. M. and Atkinson, E. J. 1997. An Introduction to Recursive Partitioning Using the RPART Routines. This is one of two documents included in:
   ```
   http://www.stats.ox.ac.uk/pub/SWin/rpartdoc.zip
   ```

---

**7. S-PLUS Data Structures**

Chapter 2 included brief summaries of the S-PLUS data structures that beginning S-PLUS users will encounter. This chapter has more detailed information.

### 7.1 Vectors

Recall that vectors may have mode logical, numeric or character. Recall also the use of `c()` to join (concatenate) vectors.

#### 7.1.1 Subsets of Vectors

Recall (section 2.6.1) two common ways to extract subsets of vectors:

1. Specify the numbers of the elements which are to be extracted. One can use negative numbers to omit elements.
2. Specify a vector of logical values. The elements that are extracted are those for which the logical value is `T`. Thus suppose we want to extract values of `x` which are greater than 10.

The following demonstrates a third possibility, for vectors that have named elements:

```r
> c(Andreas=178, John=185, Jeff=183)[c("John","Jeff")]
```

<table>
<thead>
<tr>
<th>John</th>
<th>Jeff</th>
</tr>
</thead>
<tbody>
<tr>
<td>185</td>
<td>183</td>
</tr>
</tbody>
</table>

A vector of names has been used to extract the elements.

#### 7.1.2 Patterned Data

Use `5:15` to generate the numbers 5, 6, ..., 15. Entering `15:5` will generate the sequence in the reverse order.

To repeat the sequence `(2, 3, 5)` four times over, enter `rep(c(2,3,5), 4)` thus:

```r
> rep(c(2,3,5),4)
[1] 2 3 5 2 3 5 2 3 5 2 3 5
```

If instead one wants four 2s, then four 3s, then four 5s, enter `rep(c(2,3,5), c(4,4,4))`.  

```r
> rep(c(2,3,5),c(4,4,4))
[1] 2 2 2 2 3 3 3 3 5 5 5 5
```

Note further that, in place of `c(4,4,4)` we could write `rep(4,3)`. So a further possibility is that in place of `rep(c(2,3,5), c(4,4,4))` we could enter `rep(c(2,3,5), rep(4,3))`.

Another way to achieve the same effect is `rep(c(2,3,5), each=4)`.

In addition to the above, note that the function `rep()` has an argument `length.out`, meaning “keep on repeating the sequence until the length is `length.out`.”

---

22 Below, we will meet the notion of “class”, which is important for some of the more sophisticated language features of S-PLUS. The logical, numeric and character vectors just given have class NULL, i.e. they have no class. There are special types of numeric vector which do have a class attribute. Factors are the most important example. Although often used as a compact way to store character strings, factors are, technically, numeric vectors. The class attribute of a factor has, not surprisingly, the value “factor”.

---

67
7.2 Missing Values

We noted in section 2.6.2 that any arithmetic operation or relation that involves NA generates an NA. This applies also to the relations <, <=, >, >=, ==, !=. This may have unintended consequences. Specifically, note that x == NA generates NA.

Be sure to use `is.na(x)` to test which values of x are NA. Note the following:

```
> x <- c(1,6,2,NA)
> is.na(x)  # T for when NA appears, and otherwise false
[1] F F F T
> x==NA     # All elements of the result are NA
[1] NA NA NA NA
> x[x>2]
[1] 6 NA
> NA==NA
[1] NA
```

**WARNING**: If x and y have the same length and x has missing values, then

```
y[x>2] <- x[x>2]
```

will not give the result that the naïve user might expect. Suppose for example we make the assignments

```
> x <- c(1,6,2,NA)
> y <- c(1,10,2,3)
> y[x>2] <- x[x>2]
```

Warning messages:

Replacement length not a multiple of number of elements

to replace in: y[x > 2] <- x[x > 2]

The warning messages indicate that something is wrong. As one might expect, y[NA] equals NA. On the left-hand side, any element whose subscript evaluates to NA is omitted. Thus in

```
> y[x>2]
[1] 10 NA
```

there is only one position (that occupied by the 10) to which a value can be assigned. On the right we have

```
> x[x>2]
[1] 6 NA
```

There are two elements, which are used in turn to replace the value 10 on the left. The value that is finally assigned is not 6, but NA.

One can use `!is.na(x)` to limit the selection, on both sides, to those elements of x that are not NAs. Specify

```
y[!is.na(x) & x>2] <- x[!is.na(x) & x>2]
```

We will have more to say on missing values in the section on data frames which now follows.

7.3 Data frames

Recall (section 2.7) that a data frame is a generalisation of a matrix, in which different columns may have different modes. All elements of any column must however have the same mode, i.e. all numeric or all factor, or all character. For some purposes data frames behave like matrices. There
are however important differences that arise because data frames are implemented as lists. Lists are discussed below, in section 7.7.

### 7.3.1 Component Parts of Data frames

Recall that the data frame `primates` has a column of row labels, then `Bodywt` in column 1 of the data frame proper, then `Brainwt` in column 2 of the data frame proper. Any of the following will pick out column 2 of the data frame `primates`:

- `primates$Brainwt`
- `primates[,2]`
- `primates[,"Brainwt"]`
- `primates[[2]]`  # Take the object stored in the second list element.

When the dataset is read in as indicated above, the species names will be used as the row names for the data frame, thus:

```
> primates
    Bodywt Brainwt
Potar Monkey   10.0     115
Gorilla      207.0     406
Human         62.0     1320
Rhesus monkey  6.8     179
Chimp          52.2     440
```

Consider the built-in data frame `barley`.

```
> names(barley)
[1] "yield"   "variety" "year"    "site"
> levels(barley$year)
[1] "1932" "1931"
> levels(barley$site)
[1] "Grand Rapids"    "Duluth"          "University Farm" "Morris"
[5] "Crookston"       "Waseca"
```

We will extract the data for 1932, at the Duluth site.

```
> duluth1932 <- barley[barley$year=="1932" & barley$site=="Duluth", c("yield","variety")]
> duluth1932
     yield   variety
66   22.6    Manchuria
72   25.9     Glabron
78   22.2    Svansota
84   22.5    Velvet
90   30.6     Trebi
96   22.7    No. 457
102  22.5      No. 462
108  31.4    Peatland
114  27.4      No. 475
120  29.3   Wisconsin No. 38
```
The first column holds the row labels, which in this case are the numbers of the rows that have been extracted. In place of `c("yield", "variety")` we could have written, more simply, `c(1, 2)`, or even `1:2`.

### 7.3.2 Built-in data frames

Built-in data frames to which we may refer are:

- **barley** *(yield, variety)*
- **car.all**
- **claims** *(age, car.age, type, cost)*
- **CO2** *(Plant, Type, Treatment, conc, uptake)*
- **ethanol** *(NOx, C = compression ratio, E = richness)*
- **environmental** *(ozone, radiation, temperature, wind)*
- **fuel.frame** *(Weight Disp. Mileage Fuel)*
- **kyphosis** *(Kyphosis, Age, Number, Start)*
- **market.survey** *(pick, income, moves, age, education, employment, usage, nonpub, reach.out, card)*
- **pigment** *(Batch, Sample, Test, Moisture)*

Where a number is given, this is a factor, and the number is the number of levels.

### 7.4 Data Entry

For entering a rectangular array into an S-PLUS data frame, the function `read.table()` is an alternative to the **Import Data** dialogue on the **File** menu. Suppose that the file `primates.dat` contains:

```
"Potar monkey" 10 115
Gorilla       207 406
Human         62 1320
"Rhesus monkey" 6.8 179
Chimp        52.2 440
```

Then

```
primates <- read.table("a:/primates.dat")
```

will create the data frame `primates`, from a file on the `a:` drive. The text strings in the first column will become row names, which you can access as `row.names(primates)`.

Suppose that `primates` is a data frame with two columns — body weight, and brain weight. You can give the columns names by typing in:

```
names(primates) <- c("Bodywt", "Brainwt")
```

### 7.4.1 Idiosyncrasies

The function `read.table()` is straightforward for reading in arrays that are entirely numeric. Problems arise when small mistakes cause S-PLUS to interpret a column of supposedly numeric data as character strings. For example there may be an O (oh) somewhere where there should be a 0 (zero), or an el (l) where there should be a one (1). The same problem arises if you use * or a dot (.) as the missing value (NA) symbol, but fail to warn S-PLUS of this. (The default is to use NA as the missing value symbol.)

---

Note that this is different from the default behaviour of the **Import Data** dialogue. A column of row labels is taken from the data that are to be imported only if the user specifically identifies, through the **Options** dialogue, one of the columns as a column of row labels.
Where the array contains character as well as numeric data, whether by design or accident, the behaviour of `read.table()` may seem idiosyncratic. Users can avoid the use of the first available column of character strings to provide row names by specifying the parameter setting `row.names = NULL`. The parameter setting `as.is = T` will ensure that columns of character strings are not turned into factors.

### 7.4.2 Missing values when using `read.table()`

The function `read.table()` expects missing values to be coded as NA, unless you set `na.strings` to recognise other characters as missing value indicators. For a text file that has been output from SAS, the setting `na.strings=c(.,)` may be appropriate. There may be multiple missing value indicators, e.g. `na.strings=c(.,',','').` The `'` will ensure that empty cells are entered as NAs.

### 7.4.3 Separators when using `read.table()`

It is sometimes necessary to specify tab ("\t") or comma as the separator. The default separator is white space. To set tab as the separator, specify `sep="\t"`. In order to ensure that empty cells are entered as NA, specify `na.strings=c("")`.

### 7.5 Factors

As noted in section 2.6.3, factors provide an economical way to store vectors of character strings in which there are many multiple occurrences of the same strings. Factors have a dual identity. They are stored as integer vectors, with each of the values interpreted according to the information that is in the table of levels. Model formulae (e.g. in analysis of variance and regression models, as in chapter 6), and graphics formulae, provide another reason for the use of factor objects.

The data frame `islandcities` that accompanies these notes holds the populations of the 19 island nation cities with a 1995 urban centre population of 1.4 million or more. The row names are the city names, the first column (`country`) has the name of the country, and the second column (`population`) has the urban centre population, in millions. Here is a table that gives the number of times each country occurs.

<table>
<thead>
<tr>
<th>Australia</th>
<th>Cuba</th>
<th>Indonesia</th>
<th>Japan</th>
<th>Philippines</th>
<th>Taiwan</th>
<th>United Kingdom</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>1</td>
<td>4</td>
<td>6</td>
<td>2</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

[There are 19 cities in all.]

Rather than store ’Australia’ three times, ’Indonesia’ four times, and so on, the factor representation stores different numerical codes for each of the different countries. It then uses a look-up table, stored in a list of levels that is associated with the factor, to associate the code with the name of a country.

```r
> levels(islandcities$country)
[1] "Australia"   "Cuba"       "Indonesia"  "Japan"       "Philippines" "Taiwan"
```

24 The first column of character strings that are distinct is, by default, used for row labels. Specify `row.names = NULL` to over-ride this. Any other column that has one or more character strings will, unless you specify otherwise, become a factor with as many levels as there are unique values in the column. Specify `as.is = T` to over-ride this. Storage of columns of character strings as factors is efficient when a small number of distinct strings are each repeated a large number of times.

25 Specifying `as.is = T` prevents columns of (intended or unintended) character strings from being converted into factors. Under the Import Data dialogue, an option setting is available that has the same effect. The default is, as with `read.table()`, to convert any columns of character strings into factors.

26 Factors are vectors that have mode numeric and class “factor”. They have an attribute levels that holds the level names.
1. When a vector of character strings becomes a column of a data frame, S-PLUS by default turns it into a factor. Enclose the vector of character strings in the wrapper function `factor()` if you want it to remain character.

2. There are some contexts in which factors become numeric vectors. To be sure of getting the vector of text strings specify e.g. `as.character(islandcities$country)`.

### 7.5.1 Changing level names

The “labels” parameter of `factor` makes it possible to change level names. The label text string that is specified for each level becomes the new level name. Care is necessary to ensure that the label names are in the same order as the relevant level names vector.

```r
> factor(c("UC", "UC", "ANU", "ANU"), labels=c("University of Canberra", "Australian National University", "University of Canberra", "Australian National University"))
[1] University of Canberra University of Canberra Australian National University Australian National University
```

Thus "Australia", because it is stored in the first position, has the code 1, "Cuba" has the code 2, "Indonesia" has the code 3, and so on. The country names are the factor levels.

Printing the contents of the column with the name `country` gives the names, not the codes. S-PLUS does the translation invisibly. In fact the codes are invisible in most operations with factors. There are though annoying exceptions that can make the use of factors tricky. To be sure of getting the country names, specify

```r
as.character(islandcities$country)
```

To get the codes, specify

```r
as.integer(islandcities$country)
```

By default, S-PLUS sorts the level names in alphabetical order. If we form a table that has the number of times that each country appears, this is the order that is used:

```r
> table(islandcities$country)
Australia     Cuba     Indonesia Japan Philippines Taiwan United Kingdom
3           1           4           6           2           1           2
```

This order of the level names is purely a convenience. We might prefer countries to appear in order of latitude, from North to South. We can change the order of the level names to reflect this desired order:

```r
> lev <- levels(islandcities$country)
> lev[c(7,4,6,2,5,3,1)]
[1] "United Kingdom" "Japan" "Taiwan" "Cuba"
> country <- factor(islandcities$country, levels=lev[c(7,4,6,2,5,3,1)])
> table(country)
United Kingdom Japan Taiwan Cuba Philippines Indonesia Australia
2       6       1       1       2       4       3
```

Later we will meet ordered factors, i.e. factors with ordered levels, where the order is not arbitrary.

Note the dual identity of the factor `country`. It is at one and the same time a numeric vector and a vector of character strings. In truth it is neither of these, but rather a data structure that encompasses them both. The view which a factor presents depends on how you intend to use it.

Factors have the potential to cause a few surprises, so be careful! Points to note are:

1. When a vector of character strings becomes a column of a data frame, S-PLUS by default turns it into a factor. Enclose the vector of character strings in the wrapper function `factor()` if you want it to remain character.

2. There are some contexts in which factors become numeric vectors. To be sure of getting the vector of text strings specify e.g. `as.character(islandcities$country)`. 

### 7.5.1 Changing level names

The “labels” parameter of `factor` makes it possible to change level names. The label text string that is specified for each level becomes the new level name. Care is necessary to ensure that the label names are in the same order as the relevant level names vector.

```r
> factor(c("UC","UC", "ANU", "ANU"), levels=c("Australian National University", "University of Canberra"))
[1] University of Canberra University of Canberra
[3] Australian National University Australian National University
```

Thus "Australia", because it is stored in the first position, has the code 1, "Cuba" has the code 2, "Indonesia" has the code 3, and so on. The country names are the factor levels.

Printing the contents of the column with the name `country` gives the names, not the codes. S-PLUS does the translation invisibly. In fact the codes are invisible in most operations with factors. There are though annoying exceptions that can make the use of factors tricky. To be sure of getting the country names, specify

```r
as.character(islandcities$country)
```

To get the codes, specify

```r
as.integer(islandcities$country)
```
7.6 Ordered Factors

Actually, it is their levels which are ordered. To create an ordered factor, or to turn a factor into an ordered factor, use the function `ordered()`. The levels of an ordered factor are assumed to specify positions on an ordinal scale. Try

```r
cstress.level <- rep(c("low","medium","high"),2)
ordf.stress <- ordered(stress.level, levels=c("low","medium","high"))
class(ordf.stress)
as.character(ordf.stress)
ordf.stress == "low"
ordf.stress >= "medium"
```

7.7 Lists

Lists make it possible to collect an arbitrary set of S-PLUS objects together under a single name. You might for example collect together vectors of several different modes and lengths, scalars, matrices or more general arrays, functions, etc. Lists can be, and often are, a rag-tag of different objects. We will use for illustration the list object that S-PLUS creates as output from an `lm` calculation.

For example, suppose that we create a `elastic.lm` object (c.f. section 2.1.4) by specifying

```r
elastic.lm <- lm(distance~stretch, data=elasticband)
```

The elements of the list `elastic.lm` are a variety of different kinds of objects, joined together in a list. To obtain the names of these objects, type in

```r
> names(elastic.lm)
[1] "coefficients" "residuals" "fitted.values" "effects" "R" 
[6] "rank" "assign" "df.residual" "contrasts" "terms" 
[11] "call"
```

The first list element is:

```r
> elastic.lm$coefficients
                        (Intercept)         stretch 
                        -63.57            4.554
```

Equivalent ways to extract the first list element are:

```r
elastic.lm["coefficients"]
elastic.lm[1]
```

**Note:** Here is a subtle point, which can be important for the use of lists. We can also ask for `elastic.lm["coefficients"]` or `elastic.lm[1]`. Either of these give us the list whose only element is the above vector. This is reflected in the result that is printed out. The information is preceded by `$coefficients`, meaning “list element with name coefficients”.

```r
> elastic.lm[1]
$coefficients:
 (Intercept)         stretch 
 -63.57            4.554
```

The second list element is a vector of length 10

```r
> elastic.lm$residuals
1 2 3 4 5 6 7 8 9 10 
2.11 0.321 18 1.89 27.8 13.3 7.21
```
We defer discussion of list elements 3 to 10, interesting though they are. The final list element is

```r
> elastic.lm$call
lm(formula = distance ~ stretch, data = elasticband)
```

*7.8 Matrices and Arrays*

In this course the use of matrices and arrays will be quite limited. For the purposes of this course, data frames have more general relevance, and can do almost everything that we require. Matrices are likely to be important for those users who wish to implement new regression and multivariate methods.

All the elements of a matrix have the same mode, i.e. all numeric, or all character. Thus a matrix is a more restricted structure than a data frame. One reason for numeric matrices is that they allow a variety of mathematical operations which are not available for data frames. Another reason is that matrix generalises to array, which may have more than two dimensions.

Note that matrices are stored columnwise. Thus consider

```r
> xx <- matrix(1:6,ncol=3)    # Equivalently, enter matrix(1:6,nrow=2)
> xx
[,1] [,2] [,3]
[1,]  1  3  5
[2,]  2  4  6
```

If `xx` is any matrix, the assignment

```r
x <- as.vector(xx)
```

places columns of `xx`, in order, into the vector `x`. In the example above, we get back the elements `1, 2, . . . , 6`.

Names may be assigned to the rows and columns of a matrix. We leave details until later.

Matrices have the attribute “dimension”. Thus

```r
> dim(xx)
[1] 2 3
```

In fact a matrix is a vector (numeric or character) whose dimension attribute has length 2.

Now set

```r
> x34 <- matrix(1:12,ncol=4)
> x34
[1,]  1  4  7 10
[2,]  2  5  8 11
[3,]  3  6  9 12
```

Here are examples of the extraction of columns or rows or submatrices

```r
x34[2:3,c(1,4)]  # Extract rows 2 & 3 & columns 1 & 4
x34[2,]    # Extract the second row
x34[-2,]    # Extract all rows except the second
x34[-2,-3] # Extract the matrix obtained by omitting row 2 & column 3
```

Use the `dimnames()` function to assign and/or extract matrix row and column names. The `dimnames()` function gives a list, in which the first list element is the vector of row names, and the second list element is the vector of column names. This generalises in the obvious way for use with arrays, which we now discuss.
7.8.1 Arrays

The generalisation from a matrix (2 dimensions) to allow > 2 dimensions gives an array. Thus a matrix is a 2-dimensional array.

Suppose you have a numeric vector of length 24. So that we can easily keep track of the elements, we will make them 1, 2, ..., 24. Thus

```r
> x <- 1:24
```

Then

```r
> dim(x) <- c(4,6)
```

turns this into a 4 x 6 matrix.

```r
> x
[1,]  1   5   9  13  17  21
[2,]  2   6  10  14  18  22
[3,]  3   7  11  15  19  23
[4,]  4   8  12  16  20  24
```

Now try

```r
> dim(x) <- c(3,4,2)
> x
```

```
, , 1
[1,]   1   4   7  10
[2,]   2   5   8  11
[3,]   3   6   9  12

, , 2
[1,]  13  16  19  22
[2,]  14  17  20  23
[3,]  15  18  21  24
```

7.8.2 Conversion of Numeric Data frames into Matrices

Use `as.matrix()` for this purpose.

Suppose for example that you want to interchange the rows and columns of a data frame that contains only numbers. You can do this by using `t(as.matrix())` to convert it to a matrix and transpose it, then `data.frame()` to convert it back to a data frame. The first three columns of the `moths` data frame are numeric. So we can do this:

```r
transposed.moths <- data.frame(t(as.matrix(moths[,1:3])))
```

7.9 Different Types of Attachments

When S-PLUS starts up, it has a list of directories where it looks, in order, for objects. The `attach` function extends this list. You can inspect the current list by typing in `search()`.

The working directory comes first on the search list.

You can extend the search list in two ways. You can add new directories. Alternatively, or in addition, you can place a list of S-PLUS objects on the search list. The syntax is subtly different in the two cases. The S-PLUS documentation speaks of attaching databases, as a way of encompassing both these types of extension.
A data frame is in fact a specialised list, with its columns as the objects. If you add a data frame to the search list, then you can refer to the columns by name, without the need to specify the data frame to which they belong. If there is any overlap of names, the order on the search list determines what name will be taken.

### 7.9.1 Attaching Data Frames

Thus

```r
> attach(primates)
```

then allows you to refer to `Brainwt` and `Bodywt`, where you would otherwise have to type `primates$Brainwt` and `primates$Bodywt`. This assumes that you do not have any other variables or columns of attached data frames that have either of these names.

```r
> Brainwt
Potar monkey Gorilla Human Rhesus monkey Chimp
115 115 115 115 406 1320
```

To detach this data frame, type

```r
> detach("primates")
```

i.e. quotes are now used.

Note how the use of quotes changes. You specify the name (without quotes) when you attach, and enclose the name between quotes when you detach.

### 7.9.2 The S-PLUS Directory Structure

S-PLUS has a search list, which can however be changed in the course of a session. This is the list of directories where S-PLUS will look for the objects that are needed as the session proceeds. To get a full list of these directories, type in

```r
search()
```

The following are the different sorts of directories that will or (in the case of third party libraries) may appear on the search list:

- **Working Directory:** e.g. "C:/jhm/s-course/_Data"
- **System Directories:** "C:/Program Files/splus45/"
- **MathSoft Libraries:** "C:/Program Files/splus45/library/"
- **Third Party Libraries:** "C:/Program Files/splus45/library/"

(Note that within S-PLUS you need to use `/` or `\\`, not `\`. This is a throwback to Unix.)

Objects that the user creates or changes are, unless specified otherwise, kept in the working directory.

### 7.9.3 Directories as databases

The syntax for attaching and detaching a directory is a little different. For example I have a directory `c:/stats/shape/_Data` where I keep S-PLUS functions and other objects for size and shape calculations. Inside S-PLUS this will be referred to as `c:/stats/shape/_Data`, i.e. forward slashes replace backslashes.

I can attach this directory, and so gain use to its functions and other objects, by specifying

```r
attach("c:/stats/shape/_Data")  # N. B. forward slashes
```
The default action is to attach it at position 2 in the search list. [You can check this by typing in `search()`.] The directory automatically detaches at the end of your S-PLUS session. Otherwise, assuming that it is at position 2 on the search list, specify `detach(2)`.

Observe that, here, the path was enclosed in quotes when you attached. To detach, specify the position on the search list. Thus if the directory was attached at position 2, specify

`detach(2)`

### 7.10 Exercises

1. Generate the numbers 101, 102, ..., 112, and store the result in the vector `x`.
2. Generate four repeats of the sequence of numbers (4, 6, 3).
3. Generate the sequence consisting of eight 4s, then seven 6s, and finally nine 3s.
4. Create a vector consisting of one 1, then two 2’s, three 3’s, etc., and ending with nine 9’s.
5. In the built-in data frame `environmental` determine, for each of the columns, the median, mean, upper and lower quartiles, and range.
6. For each of the following calculations, decide what you would expect, and then check to see if you were right!
   a) `answer <- c(2, 7, 1, 5, 12, 3, 4)`
      `for (j in 2:length(answer)){ answer[j] <- max(answer[j],answer[j-1])}`
   b) `answer <- c(2, 7, 1, 5, 12, 3, 4)`
      `for (j in 2:length(answer)){ answer[j] <- sum(answer[j],answer[j-1])}`
7. In the data frame `environmental` (a) extract the row or rows for which `ozone` has its maximum value; and (b) extract the vector of values of `wind` for values of `ozone` that are above the upper quartile.
8. Determine which columns of the built-in data frame `claims` are factors. For each of these factor columns, print out the levels vector. Which of these are ordered factors?
9. Determine which columns in the built-in data frame `market.survey` are variables, which are factors, and which are ordered factors.
10. Use `summary()` to get information about data in the data frames `environmental`, `claims`, and `market.survey`. Write brief notes, for each of these data sets, on what you have been able to learn.
11. From the data frame `claims`, extract a data frame `claimsA` which holds only the information for car type A.
12. From the data frame `car.test.frame` extract a data frame which holds only information for cars manufactured in Germany, France, Sweden, or England.
13. Store the numbers obtained in exercise 2, in order, in the columns of a 3 x 4 matrix.
    Store the numbers obtained in exercise 3, in order, in the columns of a 6 by 4 matrix. Extract the matrix consisting of rows 3 to 6 and columns 3 and 4, of this matrix.
8. Useful Functions

8.1 Matching and Ordering

match(<vec1>, <vec2>)  ## For each element of <vec1>, returns the
## position of the first occurrence in <vec2>

order(<vector>)  ## Returns the vector of subscripts giving
## the order in which elements must be taken
## so that <vector> will be sorted.

rank(<vector>)  ## Returns the ranks of the successive elements.

Numeric vectors will be sorted in numerical order. Character vectors will be sorted in
alphanumeric order.

The function `match()` can be used in all sorts of clever ways to pick out subsets of data. For
example:

```r
> x <- rep(1:5,rep(3,5))
> x
[1] 1 1 1 2 2 2 3 3 3 4 4 4 5 5 5
> two4 <- match(x,c(2,4), nomatch=0)
> two4
[1] 0 0 0 1 1 1 0 0 0 2 2 2 0 0 0
> # We can use this to pick out the 2s and the 4s
> as.logical(two4)
[1] F F F T T T F F F T T T F F F
```

8.2 String Functions

substring(<vector of text strings>, <first position>, <last position>)
nchar(<vector of text strings>)  ## Returns vector of number of characters in each element.

*8.2.1 Operations with Vectors of Text Strings - A Further Example*

The following stores, in `nblank`, the position of the first occurrence of a blank space in each of
the row names of the built-in dataset `fuel.frame`.

```r
nblank <- sapply(row.names(fuel.frame), function(x) {n <- nchar(x);
a <- substring(x,1:n,1:n); m <- match(" ", a, nomatch=1); m})
```

To extract the first part of the name, up to the first space, specify

```r
car.names <- substring(row.names(fuel.frame), 1, nblank-1)
```

8.3 Application of a Function to the Columns of an Array or Data Frame

apply(<array>, <dimension>, <function>)

```r
lapply(<list>, <function>)  ## N. B. A dataframe is a list. Output is a list.
sapply(<list>, <function>)  ## As lapply(), but simplify (e. g. to a vector
## or matrix), if possible.
```
8.3.1 apply()

The function `apply()` can be used on data frames as well as matrices. Here is an example:

```r
> apply(possum[, -(3:4)], 2, mean)

<table>
<thead>
<tr>
<th>case</th>
<th>site</th>
<th>age</th>
<th>hdlngth</th>
<th>skullw</th>
<th>totlngth</th>
<th>taill</th>
<th>pes</th>
</tr>
</thead>
<tbody>
<tr>
<td>52.5</td>
<td>3.62</td>
<td>NA</td>
<td>92.6</td>
<td>56.9</td>
<td>87.1</td>
<td>37</td>
<td>NA</td>
</tr>
<tr>
<td>48.1</td>
<td>15</td>
<td>27</td>
<td>32.6</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
```

The use of `apply(possum[, -(3:4)], 1, mean)` will give means for each row. These are not, for these data, useful information!

8.3.2 sapply()

The function `sapply()` can be useful for getting information about the columns of a data frame. Here we use it to count that number of missing values in each column of the supplied data frame `possum`.

```r
> sapply(possum[, -(3:4)], function(x) sum(is.na(x)))

<table>
<thead>
<tr>
<th>case</th>
<th>site</th>
<th>age</th>
<th>hdlngth</th>
<th>skullw</th>
<th>totlngth</th>
<th>taill</th>
<th>pes</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>2</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>
```

Here are several further examples that use the data frame `moths` that accompanies these notes:

```r
> sapply(moths, function(x) if(!is.factor(x)) return(0) else length(levels(x)))

<table>
<thead>
<tr>
<th>meters</th>
<th>A</th>
<th>P</th>
<th>habitat</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>8</td>
</tr>
</tbody>
</table>
```

The function `sapply()` often works most conveniently if we can ensure that the function we use returns just one element for each column. In some circumstances, it may be helpful to use the `paste()` function to paste several different items together into a character string.

*8.4 tapply()

The arguments are a variable, a list of factors, and a function that operates on a vector to return a single value. For each combination of factor levels, the function is applied to corresponding values of the variable. The output is an array with as many dimensions as there are factors. Where there are no data values for a particular combination of factor levels, NA is returned.

Often one wishes to get back, not an array, but a data frame with one row for each combination of factor levels. For example, we may have a data frame with two factors and a numeric variable, and want to create a new data frame with all possible combinations of the factors, and the cell means as the response. Here is an example of how to do it.

First, use `tapply()` to produce an array of cell means. The function `dimnames()`, applied to this array, returns a list whose first element holds the row names (i.e. for the level names for the first factor), and whose second element holds the column names. [Further dimensions are possible.]
We pass this list (row names, column names) to `expand.grid()`, which returns a data frame with all possible combinations of the factor levels. Finally, stretch the array of means out into a vector, and append this to the data frame. Here is an example using the S-PLUS data set 'catalyst'.

```r
> names(catalyst)
[1] "Temp" "Conc" "Cat" "Yield"
> attach(catalyst)

> cat.tab <- tapply(Yield,list(Temp,Cat),mean)
> cat.tab
# Examine the two-dimensional array
  A  B
160 57 48.5
180 70 81.5

> cat.names <- dimnames(cat.tab) # The list cat.names holds the two vectors c("160","180") and c("A","B")
> cat.df <- expand.grid(Temp=factor(cat.names[[1]]),
                        Cat=factor(cat.names[[2]]))
> cat.df$Means <- as.vector(cat.tab) # Stretch the array of means out into a vector, and create a new column of cat.df, named Means, to hold the array values.

> cat.df

   Temp Cat Means
 1 160  A  57.0
 2 180  A  70.0
 3 160  B  48.5
 4 180  B  81.5
```

In a case where there are no data for some combinations of factor levels, one might want to omit the corresponding rows.

### 8.5 Breaking Vectors and Data Frames Down into Lists – `split()`

As an example,

```r
split(catalyst$Yield, catalyst$Cat)
```
returns a list with two elements, the first named “A” and containing values of Yield where Cat has the level A, and the second named “B” that has the values of Yield where Cat has the level B. You need to use `split()` in this way in order to do side by side boxplots. The function `boxplot()` takes as its first element a list in which the first list element is the vector of values for the first boxplot, the second list element is the vector of values for the second boxplot, and so on.

You can use `split` to split up a data frame into a list of data frames. For example

```r
split(catalyst[,3], catalyst$Cat) # Split remaining columns by levels of Cat
split(fuel.frame[,5], fuel.frame$Type)
```

### *8.6 Merging Data Frames*

The data frame `car.all` holds extensive information on 111 cars, derived from the April 1990 edition of the US publication “Consumer Reports”. One of the variables, stored as a factor, is
I have created a data frame `type.df` which holds two character abbreviations of each of the car types, suitable for use in plotting.

```r
> type.df  # Let's look at type.df
          Type abbrev
1       Small Sm
2 Medium Md
3 Compact Cm
4 Large Lr
5
6  Van Vn
7  Sporty Sp
```

Then

```r
> new.df <- merge(car.all, type.df, by="Type")
```

will create a data frame which has the abbreviations in the additional column with name "abbrev". Note that rows with missing values will be omitted from the new data frame.

```r
> dim(car.all)  # car.all is a built-in data frame
[1] 111  36
> dim(new.df)
[1] 105  37
```

There are six missing values in `car.all$Type`, which explains the discrepancy. One way to get them included is to specify

```r
> car.all$Type <- as.character(car.all$Type)
> type.df$Type <- as.character(type.df$Type)
> new.df <- merge(car.all, type.df, by="Type")
> dim(new.df)
[1] 111  37
```

The function `as.character()` converts the missing values into empty strings (`""`). So rows initially with NA in `car.all$Type` will have the empty string in `new.df$Type`. Moreover `new.df$Type` will be a vector of character strings.

Here is a longwinded way, using `match()`, to achieve the same effect.

```r
> unique(as.character(car.all$Type))  # Just checking
[1] "Small" "Medium" "Compact" "Large" "" "Van" "Sporty"

> entry <- match(as.character(car.all$Type), as.character(type.df$Type))
> sum(is.na(entry))  # Just checking that there are no NAs
[1] 0
> car.all$abbrev <- type.df$abbrev[entry]
> table(car.all$abbrev)

  Cm Lr Md Sm Sp Vn
6 19  7 26 22 11 10
```

### 8.7 Dates

The function `dates()` will convert a character string into a dates object. By default, dates are stored using January 1 1960 as origin. This is important when you use `as.integer` to convert a date into an integer value.

```r
> as.integer(dates("20/7/1999", format="d/m/year"))
[1] 14445
> as.integer(dates("1/1/1960", format="d/m/year"))
```
A wide variety of different formats are possible. You can specify the origin that is to be used for dates, if you prefer something different from the default.

One can subtract two dates and get the time between them in days.

```r
dates("20/7/99", format="d/m/y") - dates("27/1/98", format="d/m/y")
```

8.8 Exercises

1) For the data frame `fuel.frame`, get the information provided by `summary()` for each level of `Type`. (Use `split()`.)

2) Determine the number of cars, in the built-in data frame `car.all`, for each `Country` and `Type`.

3) In the data frame `claims`: (a) determine the number of rows of information for each age category (`age`) and car type (`type`); (b) determine the total number of claims for each age category and car type; (c) determine, for each age category and car type, the number of rows for which data are missing; (d) determine, for each age category and car type, the total cost of claims.

4) Determine the number of days, according to S-PLUS, between the following dates:
   a) January 1 in the year 1, and January 1 in the year 500
   [Remember to specify the format as e. g. “d/m/year”]
   b) January 1 in the year 500, and January 1 in the year 1000
   c) January 1 in the year 1000, and January 1 in the year 1500
   d) January 1 in the year 1500, and January 1 in the year 2000

5) Generate a dates object that holds dates for each day in the year 1999. Specify the format so that the first day is printed as `1 January 1999`.

83
9. Writing Functions and other Code

We have already met several functions. Here is a function to convert Fahrenheit to Celsius:

```r
> fahrenheit2celsius <- function(fahrenheit = 32:40)(fahrenheit - 32)*5/9
> # Now invoke the function
> fahrenheit2celsius(c(40,50,60))
[1] 4.444444 10.000000 15.555556
```

The function returns the value \((fahrenheit - 32)*5/9\). More generally, a function returns the value of the last statement of the function. Unless the result from the function is assigned to a name, the result is printed.

Here is a function that prints out the mean and standard deviation of a set of numbers:

```r
> mean.and.sd <- function(x = 1:10){
+ av <- mean(x)
+ sd <- sqrt(var(x))
+ c(mean=av, SD=sd)
+ }
> # Now invoke the function
> mean.and.sd()
mean      SD
5.5 3.02765
> mean.and.sd(hills$climb)
mean       SD
1815.314 1619.151
```

9.1 Syntax and Semantics

A function is created using an assignment. On the right hand side, the parameters appear within round brackets. You can if you wish give a default. In the example above the default was \(x = 1:10\), so that users can run the function without specifying a parameter, just to see what it does.

Following the closing “}” the function body appears. Except where the function body consists of just one statement, this is enclosed between curly braces (\{
\}). The return value usually appears on the final line of the function body. In the example above, this was the vector consisting of the two named elements mean and sd.

9.2 A Function that gives Data Frame Details

First we will define a function which accepts a vector \(x\) as its only argument. It will allow us to determine whether \(x\) is a factor, and if a factor, how many levels it has. The built-in function is.factor() will return T if \(x\) is a factor, and otherwise F. The following function faclev() uses is.factor() to test whether \(x\) is a factor. It prints out 0 if \(x\) is not a factor, and otherwise the number of levels of \(x\).

```r
faclev <- function(x)if(!is.factor(x))return(0) else length(levels(x))
```

The function `sapply()` can be used to repeat a calculation on all columns of a data frame. [More generally, the first argument of `sapply()` may be a list.] To apply `faclev()` to all columns of the data frame market_survey we can specify

```r
sapply(market_survey, faclev)
```

We can alternatively put the definition of faclev in directly as the second argument of `sapply`, thus
Finally, we may want to do similar calculations on a number of different data frames. So we create a function `check.df()` which encapsulates the calculations. Here is the definition of `check.df()`.

```r
check.df <- function(df = market.survey) sapply(df, function(x) if(!is.factor(x)) return(0) else length(levels(x)))
```

### 9.3 Coding that assists Data Management

Where data, labelling etc must be pulled together from a number of sources, and especially where you may want to retrace your steps some months later, take the same care over structuring data as over structuring code. Thus if there is a factorial structure to the data files, choose file names that reflect it. You can then generate the file names automatically, using `paste()` to glue the separate portions of the name together.

Lists are a useful mechanism for grouping together all data and labelling information that one may wish to bring together in a single set of computations. Use as the name of the list a unique and meaningful identification code. Consider whether you should include objects as list items, or whether identification by name is preferable. Bear in mind, also, the use of `switch()` with the identification code used to determine what `switch()` should pick out, to pull out specific information and data that is required for a particular run.

Concentrate in one function the task of pulling together data and labelling information, perhaps with some subsequent manipulation, from a number of separate files. This structures the code, and makes the function a source of documentation for the data.

Use user-defined data frame attributes to document your data. For example, given a data frame “roller” containing roller weights and resulting lawn depressions, you might specify

```r
attributes(elasticband)$title <-
"Extent of stretch of band, and Resulting Distance"
```

### 9.4 Issues for the Writing and Use of Functions

There can be many functions. Choose the names for your own functions carefully, so that they are meaningful.

Choose meaningful names for arguments, even if this means that they are longer than you would like. Remember that they can be abbreviated in actual use.

Settings that you may need to change in later use of the function should appear as default settings for parameters. Use lists, where this seems appropriate, to group together parameters that belong together conceptually.

As far as possible, make code self-documenting. Use meaningful names for S-PLUS objects. Ensure that the names used reflect the hierarchies of files, data structures and code.

S-PLUS allows the use of names for elements of vectors and lists, and for rows and columns of arrays and dataframes. Consider the use of names rather than numbers when you pull out individual elements, columns etc. Thus `dead.tot[, "dead"]` is more meaningful and safer than `dead.tot[,2]`.

Where appropriate, provide a demonstration mode for functions. Such a mode will print out summary information on the data and/or on the results of manipulations prior to analysis, with appropriate labelling. The code needed to implement this feature has the side-effect of showing by example what the function does, and may be useful for debugging.

Break your functions up into a small number of sub-functions or “primitives”. Re-use existing functions wherever possible. Write any new “primitives” so that they can be re-used. This helps
ensure that functions contain well-tested and well-understood components. Watch s-news (section 13.3) for useful functions for routine tasks.

If at all possible, give parameters sensible defaults. Often a good strategy is to use as defaults parameters that will serve for a demonstration run of the function.

NULL is a useful default where the parameter mostly is not required, but where the parameter if it appears may be any one of several types of data structure. The test \texttt{if(!is.null())} then determines whether one needs to investigate that parameter further.

Structure code to avoid multiple entry of information.

Structure computations so that it is easy to retrace them. For this reason substantial chunks of code should be incorporated into functions sooner rather than later.

9.4.1 Graphs
Use graphs freely to shed light both on computations and on data. One of S-PLUS’s big pluses is its tight integration of computation and graphics.

9.5 Calling Modelling Functions from User-Written Functions
Objects that are in the working directory are global, i.e. any function can refer to them without passing them as parameters.

There are however occasions when commands work when invoked from the working directory, but not from within a function. All objects in the working directory are visible to functions that are called from that directory, to any functions that they call, and so on. Objects that are visible within a function are visible only to any function that is immediately called, unless specific action is taken to ensure otherwise. An assignments in frame 1 (use \texttt{assign()}) is sometimes necessary to deal with this problem. This is not a tidy solution to the problem, but it does work! The problem turns up in a number of different contexts.

9.6 A Simulation Example
We would like to know how well such a student would do, by random guessing, on a multiple choice test consisting of 100 questions each with five alterantives. We can get an idea by using simulation. Each question corresponds to an independent Bernoulli trial with probability of success equal to 0.2. We can simulate the correctness of the student for each question by generating an independent uniform random number. If this number is less than 0.2, we say that the student guessed correctly; otherwise, we say that the student guessed incorrectly.

This will work, because the probability that a uniform random variable is less than 0.2 is exactly 0.2, while the probability that a uniform random variable exceeds 0.2 is exactly 0.8, which is the same as the probability that the student guesses incorrectly. Thus, the uniform random number generator is simulating the student. S-PLUS can do this as follows:

\begin{verbatim}
Guesses <- runif(100)
correct.answers <- 1*(guesses < 0.2)
\end{verbatim}

The multiplication by 1 causes \texttt{guesses < 0.2}, which is calculated as \texttt{T} or \texttt{F}, to be coerced to 1 (\texttt{T}) or 0 (\texttt{F}). The vector \texttt{correct.answers} thus contains the results of the student's guesses. A 1 is recorded each time the student correctly guesses the answer, while a 0 is recorded each time the student is wrong.

One can thus write an S-PLUS function which simulates a student guessing at a True-False test consisting of some arbitrary number of questions. We leave this as an exercise.
9.6.1 Poisson Random Numbers

You can think of the Poisson distribution as the distribution of the total for occurrences of rare events. For example, the occurrence of an accident at an intersection on any one day should be a rare event. The total number of accidents over the course of a year may well follow a distribution which is close to Poisson. [However the total number of people injured is unlikely to follow a Poisson distribution. Why?] We can generate Poisson random numbers using \texttt{rpois()}. It is similar to the \texttt{rbinom} function, but there is only one parameter – the mean. Suppose for example traffic accidents occur at an intersection with a Poisson distribution that has a mean rate or 3.7 per year. To simulate the annual number of accidents for a 10-year period, we can specify \texttt{rpois(10,3.7)}.

We pursue the Poisson distribution in an exercise below.

9.7 Exercises

1. Use the \texttt{round} function together with \texttt{runif()} to generate 100 random integers between 0 and 99. Now look up the help for \texttt{sample()}, and use it for the same purpose.

2. Write a general function to carry out the calculations of section 8.6. More specifically, the function will take as its arguments a list of response variables, a list of factors, a data frame, and a function. It will return a data frame in which each value for each combination of factor levels is summarised in a single statistic, for example the mean or the median.

3. The supplied data frame \texttt{angina} has columns \texttt{placebo} and \texttt{TNG}. Here is a function that plots, for each patient, the \texttt{TNG} result against the \texttt{placebo} result, but insisting on the same range for the \texttt{x} and \texttt{y} axes.27

```r
plot.angina <- function()
{
  xyrange <- range(angina)  # Calculates the range of all values
  par(pin=c(6.75, 6.75))    # Set plotting area = 6.75 in. by 6.75 in.
  plot(TNG~placebo,data=angina, xlim=xyrange, ylim=xyrange, pch=16)
  abline(0,1)               # Line where TNG value = placebo value
}
```

Rewrite this function so that, given the name of a data frame and of any two of its columns, it will plot the second named column against the first named column, showing also the line \(y=x\).

4. Write a function that prints, with their row and column labels, only those elements of a correlation matrix for which \(\text{abs}(\text{correlation}) \geq 0.9\).

5. Write your own wrapper function for one-way analysis of variance which provides a side by side boxplot of the distribution of values by groups. If no response variable is specified, the function will generate random normal data (no difference between groups) and provide the analysis of variance and boxplot information for that.

6. Write a function which adds a text string containing documentation information as an attribute to a dataframe.

7. Write a function that computes a moving average of order 2 of the values in a given vector. Apply the above function to the data (in the data set \texttt{huron} that accompanies these notes) for the levels of Lake Huron. Repeat for a moving average of order 3.

---

27 The acronym TNG stands for trinitroglycerine, taken to help ward off attacks of angina. Data are from a clinical trial that compared TNG with placebo. All patients were assessed on both treatments, with the order randomised. The TNG treatment was known to be short-lived in its effect, acting only for five to fifteen minutes. So there is unlikely to be any serious carry-over effect to the later result with a placebo.
8. Find a way of computing the moving averages in exercise 3 that does not involve the use of a for loop.

9. Create a function to compute the average, variance and standard deviation of 1000 randomly generated uniform random numbers, on [0,1]. (Compare your results with the theoretical results: the expected value of a uniform random variable on [0,1] is 0.5, and the variance of such a random variable is 0.0833.)

10. Write a function which generates 100 independent observations on a uniformly distributed random variable on the interval [3.7, 5.8]. Find the mean, variance and standard deviation of such a uniform random variable. Now modify the function so that you can specify an arbitrary interval.

11. Look up the help for the \texttt{sample()} function. Use it to generate 50 random integers between 0 and 99, sampled without replacement. (This means that we do not allow any number to be sampled a second time.) Now, generate 50 random integers between 0 and 9, with replacement.

12. Write an S-PLUS function which simulates a student guessing at a True-False test consisting of 40 questions. Find the mean and variance of the student's answers. Compare with the theoretical values of .5 and .25.

13. Write an S-PLUS function which simulates a student guessing at a multiple choice test consisting of 40 questions, where there is chance of 1 in 5 of getting the right answer to each question. Find the mean and variance of the student's answers. Compare with the theoretical values of .2 and .16.

14. Write an S-PLUS function which simulates the number of working light bulbs out of 500, where each bulb has a probability .99 of working. Using simulation, estimate the expected value and variance of the random variable \( X \), which is 1 if the light bulb works and 0 if the light bulb does not work. What are the theoretical values?

15. Write a function that does an arbitrary number \( n \) of repeated simulations of the number of accidents in a year, plotting the result in a suitable way. Assume that the number of accidents in a year follows a Poisson distribution. Run the function assuming an average rate of 2.8 accidents per year.

16. Write a function which simulates the repeated calculation of the coefficient of variation (= the ratio of the mean to the standard deviation), for independent random samples from a normal distribution.

17. Write a function which, for any sample, calculates the median of the absolute values of the deviations from the sample median.

*18. Generate random samples from normal, exponential, t (2 d. f.), and t (1 d. f.), thus:

\begin{enumerate}
\item \( x_n \leftarrow \textbf{rnorm}(100) \)
\item \( x_e \leftarrow \textbf{rexp}(100) \)
\item \( x_{t2} \leftarrow \textbf{rt}(100, \ df =2) \)
\item \( x_{t2} \leftarrow \textbf{rt}(100, \ df =1) \)
\end{enumerate}

Apply the function from exercise 17 to each sample. Compare with the standard deviation in each case.

*19. The vector \( x \) consists of the frequencies
\begin{align*}
5, & \\
3, & \\
1, & \\
4, & \\
6 &
\end{align*}

The first element is the number of occurrences of level 1, the second is the number of occurrences of level 2, and so on. Write a function which takes any such vector \( x \) as its input, and outputs the vector of factor levels, here 1 1 1 1 2 2 2 2 3 . . . .

[You’ll need the information that is provided by \texttt{cumsum(x)}. Form a vector in which 1’s appear whenever the factor level is incremented, and is otherwise zero. . . .]
*20. Write a function which calculates the minimum of a quadratic, and the value of the function at the minimum.

*21. A “between times” correlation matrix, has been calculated from data on heights of trees at times 1, 2, 3, 4, . . . . Write a function that calculates the average of the correlations for any given lag.

*22. Given data on trees at times 1, 2, 3, 4, . . . , write a function that calculates the matrix of “average” relative growth rates over the several intervals. Apply your function to the data frame that accompanies these notes.

[The relative growth rate may be defined as \( \frac{1}{w} \frac{dw}{dt} = \frac{d \log w}{dt} \). Hence its is reasonable to calculate the average over the interval from \( t_1 \) to \( t_2 \) as \( \frac{\log w_2 - \log w_1}{t_2 - t_1} \).]
10. GLM, GAM and General Non-linear Models

GLM models are Generalized Linear Models. GAM models are Generalized Additive Models. GLM models extend the multiple regression model. The GAM model is a further extension.

10.1 A Taxonomy of Extensions to the Linear Model

S-PLUS allows a variety of extensions to the multiple linear regression model. In this chapter we describe the alternative functional forms.

The basic model formulation\(^{28}\) is:

\[
\text{Observed value} = \text{Model Prediction} + \text{Statistical Error}
\]

Often it is assumed that the statistical error values (values of \(\varepsilon\) in the discussion below) are independently and identically distributed as Normal. Generalised Linear Models, and the other extensions we describe, allow a variety of non-normal distributions. In the discussion of this section, our focus is on the form of the model prediction, and we leave until later sections the discussion of different possibilities for the “error” distribution.

**Multiple regression model**

\[
y = \alpha + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_p x_p + \varepsilon
\]

Use \(\text{lm()}\) to fit multiple regression models. The various other models we describe are, in essence, generalizations of this model.

**Generalized Linear Model** (e. g. logit model)

\[
y = g(a + b_1 x_1) + \varepsilon
\]

Here \(g(.)\) is selected from one of a small number of options.

For logit models, \(y = \pi + \varepsilon\), where

\[
\log\left(\frac{\pi}{1-\pi}\right) = a + b_1 x_1
\]

Here \(\pi\) is an expected proportion, and

\[
\log\left(\frac{\pi}{1-\pi}\right) = \text{logit}(\pi) \text{ is log(odds)}.
\]

We can turn this model around, and write

\[
y = g(a + b_1 x_1) + \varepsilon = \frac{\exp(a + b_1 x_1)}{1 + \exp(a + b_1 x_1)} + \varepsilon
\]

Here \(g(.)\) undoes the logit transformation.

We can add more explanatory variables: \(a + b_1 x_1 + \ldots + b_p x_p\).

\(^{28}\) This may be generalised in various ways. Models that have this form may be nested within other models which have this basic form. Thus there may be ‘predictions’ and ‘errors’ at different levels within the total model.
Use glm() to fit generalised linear models.

**Additive Model**

\[ y = \phi_1(x_1) + \phi_2(x_2) + \ldots + \phi_p(x_p) + \epsilon \]

Additive models are a generalisation of lm models. In 1 dimension

\[ y = \phi_1(x_1) + \epsilon \]

Some of \( z_1 = \phi_1(x_1) \), \( z_2 = \phi_2(x_2) \), \ldots, \( z_p = \phi_p(x_p) \) may be smoothing functions, while others may be the usual linear model terms. The constant term gets absorbed into one or more of the \( \phi \) s.

**Generalized Additive Model**

\[ y = g(\phi_1(x_1) + \phi_2(x_2) + \ldots + \phi_p(x_p)) + \epsilon \]

Generalised Additive Models are a generalisation of Generalised Linear Models. For example, \( g(.) \) may be the function that undoes the logit transformation, as in a logistic regression model.

Some of \( z_1 = \phi_1(x_1) \), \( z_2 = \phi_2(x_2) \), \ldots, \( z_p = \phi_p(x_p) \) may be smoothing functions, while others may be the usual linear model terms.

We can transform to get the model

\[ y = g(z_1 + z_2 + \ldots + z_p) + \epsilon \]

Notice that even if \( p = 1 \), we may still want to retain both \( \phi_1(.) \) and \( g(.) \), i.e.

\[ y = g(\phi_1(x_1)) + \epsilon \]

The reason is that \( g(.) \) is a specific function, such as the inverse of the logit function. The function \( \phi_1(.) \) does any further necessary smoothing, in case \( g(.) \) is not quite the right transformation. One wants \( g(.) \) to do as much of the task of transformation, with \( \phi_1(.) \) giving the transformation any necessary additional flourishes.

Use gam() to fit generalised additive models.

We now give examples of fitting glm, gam, and other models besides.

### 10.2 Logistic Regression

We will use a logistic regression model as a starting point for discussing Generalized Linear Models.

With proportions that range from less than 0.1 to 0.99, it is not reasonable to expect that the expected proportion will be a linear function of \( x \). Some such transformation (‘link’ function) as the logit is required. A good way to think about logit models is that they work on a log(odds) scale. If \( p \) is a probability (e.g. that horse A will win the race), then the corresponding odds are \( p/(1-p) \), and

\[ \log(\text{odds}) = \log\left(\frac{p}{1-p}\right) = \log(p) - \log(1-p) \]
The linear model predicts, not $p$, but $\log\left(\frac{p}{1-p}\right)$. Fig. 23 shows the logit transformation.

![Figure 23: The logit or log(odds) transformation. The left panel shows a plot of log(odds) versus proportion, while the right panel shows a plot of proportion versus log(odds). Notice how the range is stretched out at both ends.](image)

The logit or log(odds) function turns expected proportions into values that may range from $-\infty$ to $+\infty$. It is not satisfactory to use a linear model to predict proportions. The values from the linear model may well lie outside the range from 0 to 1. It is however in order to use a linear model to predict logit(proportion). The logit function is an example of a link function.

There are various other link functions that we can use with proportions. One of the commonest is the complementary log-log function.

### 10.2.1 Anaesthetic Depth Example

Thirty patients were given an anaesthetic agent which was maintained at a pre-determined [alveolar] concentration for 15 minutes before making an incision. It was then noted whether the patient moved, i.e. jerked or twisted. The interest is in estimating how the probability of jerking or twisting varies with increasing concentration of the anaesthetic agent.

The response is best taken as $\text{nomove}$, for reasons that will emerge later. There is a small number of concentrations; so we begin by tabulating proportion that have the $\text{nomove}$ outcome against concentration.

<table>
<thead>
<tr>
<th>Alveolar Concentration</th>
<th>nomove</th>
<th>0.8</th>
<th>1</th>
<th>1.2</th>
<th>1.4</th>
<th>1.6</th>
<th>2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>6</td>
<td>4</td>
<td>2</td>
<td>2</td>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>1</td>
<td>4</td>
<td>4</td>
<td>4</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>7</td>
<td>5</td>
<td>6</td>
<td>6</td>
<td>4</td>
<td>2</td>
<td></td>
</tr>
</tbody>
</table>

Table 1: Patients moving (0) and not moving (1), for each of six different alveolar concentrations.

---

29 I am grateful to John Erickson (Anesthesia and Critical Care, University of Chicago) and to Alan Welsh (Centre for Mathematics & its Applications, Australian National University) for use of these data.
Fig. 24 then displays a plot of these proportions.

![Figure 24: Plot, versus concentration, of proportion of patients not moving. The dotted horizontal line is the estimate of the proportion of moves one would expect if the concentration had no effect.](image)

We fit two models, the logit model and the complementary log-log model. We can fit the models either directly to the 0/1 data, or to the proportions in Table 1. To understand the output, you need to know about “deviances”. A deviance has a role very similar to a sum of squares in regression. Thus we have:

<table>
<thead>
<tr>
<th>Regression</th>
<th>Logistic regression</th>
</tr>
</thead>
<tbody>
<tr>
<td>degrees of freedom</td>
<td>degrees of freedom</td>
</tr>
<tr>
<td>sum of squares</td>
<td>deviance</td>
</tr>
<tr>
<td>mean sum of squares</td>
<td>mean deviance</td>
</tr>
<tr>
<td>(divide by d.f.)</td>
<td>divide by d.f.)</td>
</tr>
<tr>
<td>We prefer models with a small mean residual sum of squares.</td>
<td>We prefer models with a small mean deviance.</td>
</tr>
</tbody>
</table>

If individuals respond independently, with the same probability, then we have Bernoulli trials. While individuals will be different in their response the assumption is that, each time a new individual is taken, they are drawn at random from some larger population. Here is the S-PLUS code:

```r
> anaes.logit <- glm(nomove ~ conc, family = binomial(link = logit),
                    data = anesthetic)
```

The output summary is:
> summary(anaes.logit)

Call: glm(formula = nomove ~ conc, family = binomial(link = logit), data = anesthetic)

Deviance Residuals:
Min 1Q Median 3Q Max
-1.77 0.03 0.687 2.07

Coefficients:

                   Value Std. Error t value
(Intercept) -6.47 2.42   -2.68
conc         5.57 2.04    2.72

(Dispersion Parameter for Binomial family taken to be 1)

Null Deviance: 41.5 on 29 degrees of freedom
Residual Deviance: 27.8 on 28 degrees of freedom
Number of Fisher Scoring Iterations: 5

Correlation of Coefficients:

  (Intercept)
conc  -0.981

Fig. 25 is a graphical summary of the results:

![Graph showing concentration vs. proportion](image)

Figure 25: Plot, versus concentration, of logit(proportion) of patients not moving. The line is the estimate of the proportion of moves, based on the fitted logit model.

With such small sample sizes it is impossible to do much about checking the adequacy of the model.

One can also try `plot(anaes.logit)` and `plot.gam(anaes.logit)`. 

95
10.3 glm models (Generalised Linear Regression Modelling)

In the above we had

```r
anaes.logit <- glm(nomove ~ conc, family = binomial(link = logit), data = anesthetic)
```

The `family` parameter specifies the distribution for the dependent variable. There is an optional argument which allows us to specify the link function. Below we give further examples.

10.3.1 Further analyses of binomial data

In the first example below the family is again `binomial`, with the default `logit` link. The dependent variable is `Kyphosis`, which may be either `Present` or `Absent`.

```r
kyph.glm <- glm(Kyphosis ~ poly(Age, 2) + (Number > 5)*Start, family = binomial, data = kyphosis)  # logit link
summary(kyph.glm)
res.kyph <- residuals(kyph.glm, type="deviance")
# Other types of residuals are "pearson" and "working"
```

10.3.2 Data in the form of counts

Data that are in the form of counts can often be analysed quite effectively assuming the `poisson` family. The link that is commonly used here is `log`. The `log` link transforms from positive numbers to numbers in the range $-\infty$ to $+\infty$ which a linear model may predict.

```r
skips.glm <- glm(skips ~ ., family = poisson, data = solder.balance)  # log link
summary(skips.glm)
```

10.3.3 The gaussian family

If no family is specified, then the family is taken to be `gaussian`. The default link is then the `identity`, as for an `lm` model. This way of formulating an `lm` type model does however have the advantage that one is not restricted to the identity link.

```r
air.glm <- glm(ozone^(1/3) ~ bs(radiation, 5) + poly(wind, temperature, degree = 2), data = air)  # Assumes gaussian family, i.e. normal errors model
# B-spline models can in fact be fitted as linear models!
plot(air.glm)
plot.gam(air.glm)
```

10.3.4 The robust(gaussian) family

We investigate what a robust fit will make of the aberrant point in the hills data:

```r
hills.glm <- glm(log(time) ~ log(distance) + log(climb), family = robust(gaussian), data = hills)
> summary(hills.glm, corr=F)
```

```
Call: glm(formula = log(time) ~ log(distance) + log(climb), family = robust(gaussian), data = hills)
Deviance Residuals:
    Min     1Q Median     3Q    Max
 -0.396 0.0581 0.00356 0.0618 0.723

Coefficients:
```

96
<table>
<thead>
<tr>
<th></th>
<th>Value</th>
<th>Std. Error</th>
<th>t value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>0.377</td>
<td>0.2862</td>
<td>1.32</td>
</tr>
<tr>
<td>log(dist)</td>
<td>0.903</td>
<td>0.0653</td>
<td>13.83</td>
</tr>
<tr>
<td>log(climb)</td>
<td>0.240</td>
<td>0.0490</td>
<td>4.91</td>
</tr>
</tbody>
</table>

(Duration Parameter for Robust Gaussian family taken to be 0.024)

Null Deviance: 16.9 on 34 degrees of freedom
Residual Deviance: 1.15 on 32 degrees of freedom
Number of Fisher Scoring Iterations: 5

### 10.4 `gam` models (Generalised Additive Models)

These make it possible to fit spline and other smooth transformations of explanatory variables.

```r
gam(Kyphosis ~ s(Age, 4) + Number, family = binomial, data = kyphosis)
```

Here `s(Age, 4)` is a spline smooth transformation of Age, with the smoothing chosen to account for around 4 degrees of freedom. Kyphosis is a factor that has two levels (present/absent); it is treated as a variable with values 0 or 1.

```r
gam(ozone^(1/3) ~ lo(radiation) + lo(wind, temperature), data = air)
kypsub.gam <- gam(Kyphosis ~ poly(Age, 2) + s(Start), data = kyphosis, subset = Number>5)
```

```r
plot(kyph.gam)
print(kyph.gam)
summary(kyph.gam)
summary.glm(kyph.gam)  # Output is hard to interpret!
```


### 10.5 Prediction with New Data

The function `predict()` is a generic function that may be used to get model predictions. It does however have serious traps. If you have fitted a `gam` model, then the default is to use `predict.gam` (of course!), and all should be well. There is potential for trouble when you fit the inherently simpler `lm` or `glm` models. The problem arises with the computations which the more mathematically sophisticated novice is likely to undertake!

**Warning:** With models other than `gam` (i.e., `lm`, `glm`, etc.), you must explicitly use `predict.gam()` rather than `predict()` when you want predictions for new data under any of the following circumstances:

- the model uses `poly()` to include polynomial terms in one or more explanatory variables. [For example `poly(x, 2)` is mathematically equivalent to including terms in $x$ and $x^2$.]
- one or more factors has a levels vector which is a subset of the levels for the original data
- spline terms are included. [Usually one would then use a `gam` model.]
10.6 Non-linear Models
You can use nls() (non-linear least squares) to obtain a least squares fit to a non-linear function. You can use nlmin() (minimum of a non-linear function) or ms() (another way to find a minimum of a non-linear function) to fit non-linear models using maximum likelihood or other such statistical criteria.

10.7 Model Summaries
Type in

?methods(summary)

to get a list of the summary methods that are available. You may want to mix and match, e.g. summary.lm() on an aov or gam object. The output may not be what you might expect. So be careful!

10.8 Further Elaborations
Generalised Linear Models were developed in the 1970s. They unified a huge range of diverse methodology. They have now become a stock-in-trade of statistical analysts. Their practical implementation built on the powerful computational abilities which, by the 1970s, had been developed for handling linear model calculations.

Practical data analysis demands further elaborations. An important elaboration is to the incorporation of more than one term in the error structure. The S-PLUS nlme library implements such extensions, both for linear models and for a wide class of nonlinear models.

Each such new development builds on the theoretical and computational tools that have arisen from earlier developments. Exciting new analysis tools will continue to appear for a long time yet. This is fortunate. Most professional users of S-PLUS will regularly encounter data where the methodology that the data ideally demands is not yet available.

10.9 Exercises
1. Fit a Poisson regression model to the data in the data frame moths. Allow different intercepts for different habitats. Use log(meters) as covariate.

10.10 References


11. Multi-level Models, Time Series and Survival Analysis

*11.1 Multi-Level Models, Including Repeated Measures Models

Variance component models and repeated measures models are special cases of multi-level models.

Models have both a fixed effects structure and an error structure. For example, in an inter-laboratory comparison there may be variation between laboratories, between observers within laboratories, and between multiple determinations made by the same observer on different samples. If we treat laboratories and observers as random, the only fixed effect is the mean.

The functions \texttt{lme()} and \texttt{nlme()}, from the Pinheiro and Bates library, handle models in which a repeated measures error structure is superimposed on a linear (\texttt{lme}) or non-linear (\texttt{nlme}) model. Version 3 of \texttt{lme}, which is currently in \texttt{\alpha}-test, is broadly comparable in its abilities to Proc Mixed which is available in the widely used SAS statistical package. The function \texttt{lme} has associated with it highly useful abilities for diagnostic checking and for various insightful plots.

There is a strong link between a wide class of repeated measures models and time series models. In the time series context there is usually just one realisation of the series, which may however be observed at a large number of time points. In the repeated measures context there may be a large number of realisations of a series which is typically quite short.

11.1.1 The Kiwifruit Shading Data, Again

Refer back to section 6.9.1 for details of these data. The fixed effects are block and treatment (shade). The random effects are block (though making block a random effect is optional), plot within block, and units within each block/plot combination. Here is the analysis:

```
> kiwishade.lme <- lme(yield ~ shade, random = ~1|block/plot, data=kiwishade)
> summary(kiwishade.lme)
Linear mixed-effects model fit by REML
Data: kiwishade
  AIC   BIC logLik     AIC   BIC logLik     AIC   BIC logLik
272.3 284.8   272.3 284.8   272.3 284.8   272.3 284.8   272.3
Random effects:
  Formula: ~ 1 | block
    (Intercept)
    StdDev:  2.019

  Formula: ~ 1 | plot %in% block
    (Intercept) Residual
    StdDev:  1.479  3.49

Fixed effects: yield ~ shade
  Value Std.Error DF t-value p-value
(Intercept) 96.53 1.340  36 72.05  <.0001
shade1  1.43   0.934   6  1.53   0.1774
shade2  2.95   0.539   6  5.47   0.0016
shade3  2.23   0.381   6  5.86   0.0011
Correlation:
  (Intr) shade1 shade2
```

99
This was a balanced design, which is why in section 6.8.2 we could use `aov()` for an analysis. We can get an output summary that is helpful for showing how the error mean squares match up with standard deviation information given above thus:

\[ \text{block plot \%in\% block} \]

\[ \text{3} \quad 12 \]

\[ > \text{anova(kiwishade.lme)} \]

\[ \begin{array}{cccc}
  \text{numDF} & \text{denDF} & \text{F-value} & \text{p-value} \\
  (\text{Intercept}) & 1 & 36 & 5191 < .0001 \\
  \text{shade} & 3 & 6 & 22 0.0012 \\
\end{array} \]

**Fixed effects:**

\[ \begin{array}{ccc}
  \text{lower} & \text{est.} & \text{upper} \\
  (\text{Intercept}) & 93.8153 & 96.533 & 99.250 \\
  \text{shade1} & -0.8583 & 1.427 & 3.712 \\
  \text{shade2} & 1.6324 & 2.952 & 4.271 \\
  \text{shade3} & 1.3007 & 2.234 & 3.166 \\
\end{array} \]

**Random Effects:**

\[ \begin{array}{ccc}
  \text{Level: block} \\
  \text{lower est. upper} \\
  \text{sd((Intercept))} & 0.5469 & 2.019 & 7.456 \\
\end{array} \]

\[ \begin{array}{ccc}
  \text{Level: plot} \\
  \text{lower est. upper} \\
  \text{sd((Intercept))} & 0.3676 & 1.479 & 5.947 \\
\end{array} \]

**Within-group standard error:**

\[ \begin{array}{ccc}
  \text{lower est. upper} \\
  2.77 & 3.49 & 4.397 \\
\end{array} \]

We are interested in the three estimates. By squaring the standard deviations and converting them to variances we get the information in the following table:

<table>
<thead>
<tr>
<th>Variance component</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>block</td>
<td>2.019² = 4.076</td>
</tr>
<tr>
<td>plot</td>
<td>1.479² = 2.186</td>
</tr>
<tr>
<td>residual (within group)</td>
<td>3.490²=12.180</td>
</tr>
</tbody>
</table>
The above allows us to put together the information for an analysis of variance table. We have:

<table>
<thead>
<tr>
<th>Variance component</th>
<th>Mean square for anova table</th>
<th>d.f.</th>
</tr>
</thead>
<tbody>
<tr>
<td>block</td>
<td>4.076</td>
<td>2 (3-1)</td>
</tr>
<tr>
<td>plot</td>
<td>2.186</td>
<td>6 (3-1) ×(2-1)</td>
</tr>
<tr>
<td>residual (within group)</td>
<td>12.180</td>
<td>3×4×(4-1)</td>
</tr>
</tbody>
</table>

Now find see where these same pieces of information appeared in the analysis of variance table of section 6.9.1:

```
> kiwishade.aov <- aov(yield~block+shade+Error(block:shade), data=kiwishade)
> summary(kiwishade.aov)
Error: block:shade
             Df Sum of Sq  Mean Sq F Value  Pr(>F) 
block          2   172.33  86.166  4.1207 0.07488 
shade          3   1395.5 465.167 22.2035 0.00119 
Residuals     36    27.50   0.764

Error: Within
             Df Sum of Sq  Mean Sq F Value Pr(>F) 
Residuals   36  438.6000  12.1833
```

11.1.2 The Pigment Data

These are multi-level analysis of variance models. The varcomp() function offers one way to fit them. They are now better handled using the function `lme()` in the Pinheiro and Bates `nlme` library, which can handle a vastly wider class of problems. In this particular instance, the data are balanced over factor levels, and we can use analysis of variance.

We give scant explanation. This section may perhaps be useful for readers who already have some understanding of the methodology. Data are from the built-in data frame `pigment`.

First, we use analysis of variance:

```
> pigment.aov <- aov(Moisture ~ Batch/Sample, data=pigment)
> summary(pigment.aov)
             Df Sum of Sq Mean Sq  F value  Pr(>F) 
Batch        14  1210.933  86.495 94.358448 0.00000 
Sample %in% Batch 15  869.750  57.983 63.249554 0.00000 
Residuals     30    27.500   0.917

> pigment.lme <- lme(Moisture~1, random=~1|Batch/Sample, data=pigment)
> intervals(pigment.lme)
Approximate 95% confidence intervals
```

101
Fixed effects:

<table>
<thead>
<tr>
<th>lower est. upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Intercept) 24.33 26.78 29.24</td>
</tr>
</tbody>
</table>

Random Effects:

Level: Batch

<table>
<thead>
<tr>
<th>lower est. upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>sd((Intercept)) 0.6999 2.67 10.18</td>
</tr>
</tbody>
</table>

Level: Sample

<table>
<thead>
<tr>
<th>lower est. upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>sd((Intercept)) 3.713 5.342 7.684</td>
</tr>
</tbody>
</table>

Within-group standard error:

<table>
<thead>
<tr>
<th>lower est. upper</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.7427 0.9574 1.234</td>
</tr>
</tbody>
</table>

Thus the variance components are 7.12 (between batches), 28.54 (between samples within batches), and 0.92 (within samples).

Finally, for completeness, here is the output from varcomp():

```r
> is.random(pigment) <- T # make all factors random
> pigment.varcomp <- varcomp(Moisture ~ Batch/Sample, pigment)
> # Explain variation in Moisture in terms of variation between batches,
> # and variation of samples within batches
>
> summary(pigment.varcomp)   # Components of variance breakdown

Call:
varcomp(formula = Moisture ~ Batch/Sample, data = pigment)
Variance Estimates:

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Batch</td>
<td>7.1279762</td>
<td></td>
</tr>
<tr>
<td>Sample %in% Batch</td>
<td>28.533333</td>
<td></td>
</tr>
<tr>
<td>Residuals</td>
<td>0.9166667</td>
<td></td>
</tr>
</tbody>
</table>

Method: minque0

Coefficients:

<table>
<thead>
<tr>
<th>(Intercept)</th>
</tr>
</thead>
<tbody>
<tr>
<td>26.783333</td>
</tr>
</tbody>
</table>

Approximate Covariance Matrix of Coefficients:

| [1] | 1.441587 |
```

The first summary above is an analysis of variance (aov) summary. It gives the sum of squares table, and the corresponding mean squares. The variance components, given using lme() and varcomp(), provide a model for the generation of the mean squares. We now show how the mean square can be constructed from the variance components.
11.1.3 Analysis of Variance Versus Variance Components – The Pigment Data

<table>
<thead>
<tr>
<th></th>
<th>df</th>
<th>AOV Mean Square</th>
<th>Estimate from Variance Components</th>
<th>Number of these units in next level</th>
</tr>
</thead>
<tbody>
<tr>
<td>Batch</td>
<td>14</td>
<td>86.5</td>
<td>0.92+2x28.53+2x2x7.128 = 86.5</td>
<td>15</td>
</tr>
<tr>
<td>Sample in Batch</td>
<td>15</td>
<td>58.0</td>
<td>0.92+2x28.23 = 57.98</td>
<td>2</td>
</tr>
<tr>
<td>Residual</td>
<td>30</td>
<td>0.92</td>
<td>0.92</td>
<td>2</td>
</tr>
</tbody>
</table>

Here is another possibility:

```r
varcomp(Moisture ~ Batch/Sample, pigment, method=c("winsor", "r"))
```

*11.2 Repeated Measures Models*

The functions `lme()` and `nlme()` handle models in which a repeated measures error structure is superimposed on a linear (`lme`) or non-linear (`nlme`) model. Version 3 of lme, which is currently in beta-test, is broadly comparable in its abilities to Proc Mixed which is available in the widely used SAS statistical package. The function `lme` has associated with it vastly superior abilities for diagnostic checking and for various insightful plots.

There is a strong link between a wide class of repeated measures models and time series models. In the time series context there is usually just one realisation of the series, which may however be observed at a large number of time points. In the repeated measures context there may be a large number of realisations of a series which is typically quite short.

Here is an example of the use of `lme()` for the Michelson speed of light data which are in the Venables and Ripley MASS library.

```r
> michelson$Run <- as.numeric(michelson$Run) # Ensure Run is a variable
> mich.lme20 <- lme(fixed = Speed ~ Run, data = michelson, 
                   random = ~ Run| Expt, correlation = corARMA(value = c(0.25, 0.25), 
                      form = ~ 1 | Expt, p = 2, q = 0),   
                   weights = varIdent(form = ~ 1 | Expt))
```

```r
> summary(mich.lme20)
```

Linear mixed-effects model fit by maximum likelihood

Data: michelson

AIC  BIC logLik
1117 1148 -546.4

Random effects:

<table>
<thead>
<tr>
<th></th>
<th>StdDev</th>
<th>Corr</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Intercept)</td>
<td>47.031</td>
<td></td>
</tr>
<tr>
<td>Run</td>
<td>3.628</td>
<td>-1</td>
</tr>
<tr>
<td>Residual</td>
<td>121.930</td>
<td></td>
</tr>
</tbody>
</table>

Correlation Structure: ARMA(2,0)

Parameter estimate(s):

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Phi1</td>
<td>0.6321</td>
</tr>
<tr>
<td>Phi2</td>
<td>0.3106</td>
</tr>
</tbody>
</table>

Variance function:

| Structure: Different standard deviations per stratum |
Formula: ~ 1 | Expt

Parameter estimates:
1 2 3 4 5
1 0.2993 0.6276 0.5678 0.4381

Fixed effects: Speed ~ Run

<table>
<thead>
<tr>
<th>Value</th>
<th>Std.Error</th>
<th>z-value</th>
<th>p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Intercept)</td>
<td>860.9</td>
<td>27.2</td>
<td>31.6</td>
</tr>
<tr>
<td>Run</td>
<td>-1.6</td>
<td>2.1</td>
<td>-0.7</td>
</tr>
</tbody>
</table>

Correlation:

<table>
<thead>
<tr>
<th>(Intr)</th>
<th>Run</th>
</tr>
</thead>
<tbody>
<tr>
<td>Run</td>
<td>0.962</td>
</tr>
</tbody>
</table>

Standardized Within-Group Residuals:

<table>
<thead>
<tr>
<th>Min</th>
<th>Q1</th>
<th>Med</th>
<th>Q3</th>
<th>Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>-2.905</td>
<td>-0.6207</td>
<td>0.1222</td>
<td>0.7373</td>
<td>1.955</td>
</tr>
</tbody>
</table>

Number of Observations: 100
Number of Groups: 5

> # Now plot population residuals versus BLUP fitted values
> plot(mich.lme20, fitted(.) ~ Run | Expt, between = list(x = 0.25, y = 0.25), type = "b")

11.3 Time Series Models

S-PLUS has a number of functions for manipulating and plotting time series, and for calculating the autocorrelation function.

There are two styles of analysis methods – time domain methods and frequency domain methods. In the time domain there are two classes of models – the conventional “short memory” models where the autocorrelation function decays quite rapidly to zero, and the relatively recently developed “long memory” time series models, where the autocorrelation function decays very slowly as observations move apart in time. A characteristic of “long memory” models is that there is variation at all temporal scales. Thus in a study of wind speeds it may be possible to characterise windy days, windy weeks, windy months, windy years, windy decades, and perhaps even windy centuries. S-PLUS has functions both for fitting conventional short memory models and for fitting the more recently developed long memory models.

The function `stl()` decomposes a times series into a trend and seasonal components, etc. (This is intended to replace the older `sabl()` function.) The functions `ar()` (for “autoregressive” models) and `arima.mle()` (“autoregressive integrated moving average models”) fit standard types of time domain short memory models. Advanced users may want to be aware of the function `arima.fracdiff()` (“fractionally differenced ARIMA model”). This is designed for fitting “long memory” time domain models in which there is some residual correlation even at very long time lags.

There is in addition an extensive collection of functions for working with frequency domain or “spectral” analysis.

See the discussion of these models, including a brief survey of the statistical theory, in chapters 20-21 of the *S-PLUS 4 Guide to Statistics* (MathSoft, 1997).
11.4 Survival Analysis

For example times at which subjects were either lost to the study or died (“failed”) may be recorded for individuals in each of several treatment groups. Engineering or business failures can be modelled using this same methodology. S-PLUS is strong in this area, with what may be the best abilities for survival analysis that are available in any statistical analysis package.

Chapters 22-26 of the S-PLUS4 Guide to Statistics (MathSoft, 1997) give an extended overview of the relevant theory, and details of S-PLUS abilities. There is a progression from the Kaplan-Meier non-parametric model, to models which assume specific parametric forms for the hazard ratio, and then through to fully parametric survival models.

11.5 Exercises

1. Use the function acf() to plot the autocorrelation function of lake levels in successive years in the data set huron that accompanies these notes. Do the plots both with type="correlation" and with type="partial".

11.6 References


12. Advanced Programming Topics

12.1. Methods

S-PLUS is an object-oriented language. Objects may have a “class”. For functions such as `print()`, `summary()`, etc., the class of the object determines what action will be taken. Thus in response to `print(x)`, S-PLUS determines the class attribute of `x`, if one exists. If for example the class attribute is “factor”, then the function which finally handles the printing is `print.factor()`. The function `print.default()` is used to print objects which have not been assigned a class.

More generally, the class attribute of an object may be a vector of strings. If there are “ancestor” classes – parent, grandparent, . . ., these are specified in order in subsequent elements of the class vector. For example, ordered factors have the class “ordered”, which inherits from the class “factor”. Thus:

```r
> fac <- ordered(1:3)
> class(fac)
[1] "ordered" "factor"
```

Here `fac` has the class “ordered”, which inherits from the parent class “factor”.

The function `print.ordered()`, which is the function that is called when you invoke `print()` with an ordered factor, makes use of the fact that “ordered” inherits from “factor”.

```r
> print.ordered
function(x, ...)
{
  NextMethod("print")  ## Causes printing as for "factor"
  cat("\n", paste(levels(x), collapse = " < "), "\n")
  ## Adds extra information because factor is ordered
  invisible(x)
}
```

Note that it is purely a convenience for `print.ordered()` to operate in this way. The printing of a gam object generates a call to `print.gam()`, which does not call `print.glm()`. Nor does `print.glm()` call `print.lm()`.

Here is an example:

```r
> kyph.gam(formula = Kyphosis ~ lo(Age, 0.8) + Start +
  lo(Number, 0.8), family = binomial, data = kyphosis)
> class(kyph.gam)
[1] "gam" "glm" "lm"
```

12.2 Extracting Arguments to Functions

How, inside a function, can one extract the value assigned to a parameter when the function was called? Below there is a function `extract.arg()`. When it is called as `extract.arg(a=xx)`, we want it to return “xx”. When it is called as `extract.arg(a=xy)`, we want it to return “xy”. Here is how it is done.

```r
extract.arg <- 
function (a) 
{
  s <- substitute(a)
}
```
If the argument is a function, we may want to get at the arguments to the function. Here is how one can do it:

```r
deparse.args <-
function (a)
{
  s <- substitute (a)
  if(mode(s) == "call"){
    # the first element of a 'call' is the function called
    # so we don't deparse that, just the arguments.
    print(paste("The function is:  ", s[1],"()", collapse=""))
    lapply (s[-1], function (x)
      paste (deparse(x), collapse = "")
    )
  } else stop ("argument is not a function call")
}
```

For example:

```r
> deparse.args(list(x+y, foo(bar)))
[1] "The function is:  list()"
[[1]]:
[1] "x + y"
[[2]]:
[1] "foo(bar)"
```

### 12.3 Parsing and Evaluation of Expressions

When you type in an expression such as `mean(x+y)` or `cbind(x,y)` for S-PLUS to evaluate, there are two steps:

1. The text string which you type in is parsed and turned into an expression, i.e. the syntax is checked and it is turned into code which the S-PLUS engine can more immediately evaluate.

2. The expression is evaluated.

If you type in

```r
expression(mean(x+y))
```

the output is the unevaluated expression `expression(mean(x+y))`. By setting

```r
my.exp <- expression(mean(x+y))
```

you can store this unevaluated expression in `my.exp`. Actually what is actually stored in `my.exp` is a little different from what is printed out. S-PLUS gives you as much information as it judges is (most of the time) helpful for you to know.

Note that `expression(mean(x+y))` is different from `expression("mean(x+y)")`, as is obvious when the expression is evaluated. A text string is a text string is a text string, unless you explicitly change it into an expression or part of an expression.

Let’s see how this works in practice.
> x <- 101:110
> y <- 21:30
> my.exp <- expression(mean(x+y))
> my.txt <- expression("mean(x+y)")
> eval(my.exp)
[1] 131
> eval(my.txt)
[1] "mean(x+y)"

What if we already have "mean(x+y)" stored in a text string, and we want to turn it into an expression? The answer is to use the function parse(), but you must tell it that you are supplying text rather than the name of a file. Thus

> parse(text="mean(x+y)")
expression(mean(x + y))

Let’s store the expression in my.exp2, and then evaluate it

> my.exp2 <- parse(text="mean(x+y)")
> eval(my.exp2)
[1] 131

Here is a function that creates a new data frame from an arbitrary set of columns of an existing data frame. Once in the function, we attach the data frame so that we can leave off the name of the data frame, and use only the column names

```r
function(old.df = fuel.frame, colnames = c("Disp.", "Fuel"))
{
  attach(old.df)
on.exit(detach("old.df"))
argtxt < paste(colnames, collapse = ",")
exprtxt < paste("data.frame(" , argtxt , ", sep = ",")
expr < parse(text = exprtxt)
df < eval(expr)
names(df) <- colnames
df
}
```

To verify that the function does what it should, type in

> z <- make.new.df()
> z[1:4,]  # Display the first four rows of z

<table>
<thead>
<tr>
<th>Disp.</th>
<th>Fuel</th>
</tr>
</thead>
<tbody>
<tr>
<td>Eagle Summit 4</td>
<td>97 3.030303</td>
</tr>
<tr>
<td>Ford Escort   4</td>
<td>114 3.030303</td>
</tr>
<tr>
<td>Ford Festiva 4</td>
<td>81 2.702703</td>
</tr>
<tr>
<td>Honda Civic 4</td>
<td>91 3.125000</td>
</tr>
</tbody>
</table>

The function do.call() may be convenient if you want to keep the function name and the argument list in separate text strings. When do.call is used it is only necessary to use parse() in generating the argument list.

For example

```r
make.new.df <- function(old.df = fuel.frame, colnames = c("Disp.", "Fuel"))
{
  attach(old.df)
}
on.exit(detach("old.df"))
argtxt <- paste(colnames, collapse = ",")
listexpr <- parse(paste("list(" argtxt, ")", sep = "))
df <- do.call("data.frame", eval(listexpr))
names(df) <- colnames
df
}

12.4 Searching S-PLUS functions for a specified token.
A token is a syntactic entity; for example function names are tokens. For example, we search all
functions in the working directory. The purpose of using unlist() in the code below is to
change myfunc from a list into a simple vector of characters.

> mygrep
function(str)
{
  ## Assign the names of all objects in current S-PLUS
  ## working directory to tempobj
  ##
  tempobj <- objects()
  objstring <- character(0)
  for(i in tempobj) {
    myfunc <- get(i)
    if(is.function(myfunc))
      if(length(grep(str,
          unlist(myfunc))))
        objstring <- c(objstring, i)
  }
  return(objstring)
}
13. Appendix 1 – S-PLUS Resources

13.1 Official Documentation
The quality is variable. Some chapters are excellent summaries of the current state of the statistical
methodology, and of the S-PLUS abilities.
These documents are available at the web site:

http://www.insightful.com

13.2 Literature written by expert users
This 439 page document is available from
http://www.seanet.com/~pburns/Spoetry/.
Although the style is leisurely, this assumes some prior knowledge of computing language terms. It may be a
good book to work through once you have some initial knowledge of S-PLUS.
New York.
This is a book for specialists. It describes a version 4 (N. B. 4, not 5) of the S language, which is the basis for
version 5 of S-PLUS. To date, version 5 of S-PLUS is available only for Unix.
Advanced Books and Software, Pacific Grove CA.
This is the basic reference on S-PLUS model formulae and models.
London.
The choice of analysis methods may seem idiosyncratic. It has little on the more recently developed methods
which are S-PLUS’s strength.
Harrell, F. An Introduction to S-PLUS and the Hmisc and Design Libraries.
The latest version of this manual is available from
Chapters 1-4 and 9-10 are a good introduction to S-PLUS, likely to be particularly helpful to anyone who
comes to S-PLUS from SAS. The examples in this manual are largely medical.
This is an introductory book, at about the same level as Spector.
This is a readable and compact beginner’s guide to the S-PLUS language. Copies are available from the ANU
Co-op bookshop.
This has become a text book for the use of S-PLUS for applied statistical analysis. It assumes a fair level of
statistical sophistication. Explanation is careful, but often terse. Together with the ‘Complements’ it gives
brief introductions to extensive libraries of functions that have been written or adapted by Ripley, Venables,
and a number of other statisticians. Supplementary material (‘Complements’) is available from
http://www.stats.ox.ac.uk/pub/MASS3/.
The supplementary material is extensive, and is continually supplemented. The present version of the statistical ‘Complements’ has extensive information on new libraries that have come from third party sources. There is helpful information, additional to what is in the book, that is specific to the S-PLUS 4.0 and S-PLUS 4.5 releases for Microsoft Windows.


13.3 Libraries
Extensive libraries and/or collections of S-PLUS functions are available from the web sites:

http://hesweb1.med.virginia.edu/biostat/s/index.html (Hmisc and Design)
http://www.stats.ox.ac.uk/pub/MASS3/ (MASS2, and other libraries)
http://lib.stat.cmu.edu

13.4 The s-news electronic mail discussion list
This is an email list which is devoted to discussion of S-PLUS. To subscribe, send the message
subscribe s-news
to s-news-request@wubios.wustl.edu
If your mailer inserts a signature, follow the above request with
end
on a separate line.
There is an archive of past discussion that you can access via the web page
http://lib.stat.cmu.edu

13.5 Competing Systems – R and XLISP-STAT
The R language implementation is an S clone that is available at no cost. It has a less extensive range of analysis functions than S-PLUS. There is wide international co-operation in adding new function libraries, which . You can get it from (among other places):
http://mirror.aarnet.edu.au/pub/CRAN
It is available for Unix, for the Macintosh and for Windows 95.
The Venables and Ripley collection of libraries is now also available for R.

XLISP-STAT is a lisp-based system that, like S-PLUS and R, allows a seamless extensibility. It is available from
14. Appendix

14.1 Data Sets Used in this Course

Data Sets that Accompany these Notes

<table>
<thead>
<tr>
<th>ACF</th>
<th>ais</th>
<th>anaesthetic</th>
<th>angina</th>
<th>austpop</th>
</tr>
</thead>
<tbody>
<tr>
<td>beams</td>
<td>cars</td>
<td>dolphins</td>
<td>elasticband</td>
<td>florida</td>
</tr>
<tr>
<td>huron</td>
<td>ironslag</td>
<td>islandcities</td>
<td>kiwishade</td>
<td>moths</td>
</tr>
<tr>
<td>oddbooks</td>
<td>piglitters</td>
<td>possum</td>
<td>primates</td>
<td>rainforest</td>
</tr>
<tr>
<td>roller</td>
<td>seederates</td>
<td>snow.cover</td>
<td>type.df</td>
<td>vehicle.summary</td>
</tr>
</tbody>
</table>

Data Sets in Library MASS

| fgl | hills | michelson | Rubber |

Data Sets Supplied with S-PLUS

<table>
<thead>
<tr>
<th>CO2</th>
<th>air</th>
<th>barley</th>
<th>brains</th>
<th>car.all</th>
</tr>
</thead>
<tbody>
<tr>
<td>catalyst</td>
<td>environmental</td>
<td>fuel.frame</td>
<td>hills</td>
<td>kyphosis</td>
</tr>
<tr>
<td>market.survey</td>
<td>pigment</td>
<td>singer</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

14.2 Answers to Selected Exercises

Section 1.6
1. plot(distance~stretch,data=elasticband)
2. (ii), (iii)
   ```r
   plot(snow.cover ~ year, data = snow)
   hist(snow$snow.cover)
   hist(log(snow$snow.cover))
   ```

Section 2.8
1. The value of answer is (a) 12, (b) 22, (c) 600.
2. `prod(c(10,3:5))`
3(i) `bigsum <- 0; for (i in 1:100) {bigsum <- bigsum+i }; bigsum`
3(ii) `sum(1:100)`
4(i) `bigprod <- 1; for (i in 1:50) {bigprod <- bigprod*i }; bigprod`
4(ii) `prod(1:50)`
5. `radius <- 3:20; volume <- 4*pi*radius^3/3`
sphere.data <- data.frame(radius=radius, volume=volume)
6. sapply(market.survey, is.factor)
sapply(market.survey[, -7], levels)
sapply(market.survey, is.ordered)

Section 3.8
1. plot(brain ~ body, data=brains, pch=1,
       xlab="Body weight (kg)", ylab="Brain weight (g)")
2. plot(log(brain) ~ log(body), data=brains, pch=1,
       xlab="Body weight (kg)", ylab="Brain weight (g)", axes=F)
   brainaxis <- 10^seq(-1,4)
   bodyaxis <- 10^seq(-2,4)
   axis(1, at=log(bodyaxis), lab=bodyaxis)
   axis(2, at=log(brainaxis), lab=brainaxis)
   box()
   identify(log(brains$body), log(brains$brain), labels=row.names(brains))
(See problem 4.)
3. par(mfrow = c(1,2)), etc.
4. (a) plot(mean.height ~ year, data=huron)
    (b) identify(huron$year, huron$mean.height, labels=huron$year)
    (c) lag.plot(huron$mean.height)
5. The following is a simple version:
   plot.florida <- function(xvar="BUSH", yvar="BUCHANAN", fun = sqrt){
      x <- florida[,xvar]
      y <- florida[,yvar]
      plot(fun(x), fun(y), xlab=xvar, ylab=yvar)
      mtext(side=3, line=1,
            "Votes in Florida, by county, in the 2000 US Presidential election")
   }
A better version, which labels the axes with the actual numbers of votes, is:
   plot.florida <- function(xvar="BUSH", yvar="BUCHANAN", fun = sqrt){
      x <- florida[,xvar]
      y <- florida[,yvar]
      xticks <- pretty(x)
      yticks <- pretty(y)
      plot(fun(x), fun(y), xlab=xvar, ylab=yvar, axes=F)
      axis(1, at=fun(xticks), labels=xticks)
      axis(2, at=fun(yticks), labels=yticks)
      box()
      mtext(side=3, line=1,
            "Votes in Florida, by county, in the 2000 US Presidential election")
   }
6. rnorm(10, 170, 4)
7. par(mfrow = c(3, 4))
for(i in 1:4)qqnorm(rnorm(10))
for(i in 1:4)qqnorm(rnorm(100))
for(i in 1:4)qqnorm(rnorm(1000))
8. par(mfrow = c(3, 4))
for(i in 1:4)qqnorm(runif(10))
for(i in 1:4)qqnorm(runif(100))
for(i in 1:4)qqnorm(runif(1000))
9. Replace rnorm(10) by rnorm(chisq, 1), etc.
10. names(hills)
   attach(hills)
   hist(distance)
   plot(density(distance))
   qqnorm(distance)
   hist(log(distance))
   plot(density(log(distance)))
   qqnorm(log(distance))
   detach("hills")

Section 4.8, example 2
environmental$Temp <- equal.count(environmental$temperature, 3, 1/2)
environmental$Wind <- equal.count(environmental$wind, 3, 1/2)
xyplot(ozone ~ radiation | Temp * Wind,
data = environmental, panel = function(x, y)
{
  panel.grid(v = 2)
  panel.xyplot(x, y, cex = 0.5)
  panel.loess(x, y, span = 1)
}
, aspect = 2, xlab = "Radiation (langleys)",
ylab = "Ozone (ppb)")

Section 7.10
1. x <- seq(101,112) or x <- 101:112
2. rep(c(4, 6, 3), 4)
3. c(rep(4, 8), rep(6, 7), rep(3, 9)) or rep(c(4, 6, 3), c(8, 7, 9))
4. rep(seq(1, 9), seq(1, 9)) or rep(1:9, 1:9)
5. Use summary(environmental) to get this information.
6(a) 2 7 7 5 12 12 4
6(b) 2 9 8 6 17 15 7
7. environmental[environmental$ozone == max(environmental$ozone),]
   environmental$wind[environmental$ozone > quantile(environmental$ozone, .75)]
8. `sapply(claims, function(x) if(is.factor(x)) levels(x) else "")`
9. `sapply(market.survey, is.factor); sapply(market.survey, is.ordered)`
10. `summary(environmental); summary(claims); summary(market.survey)`
11. `claimsA <- claims[claims$type == "A",]`
12. `gfse <- as.logical(match(car.test.frame$Country, c("Germany", "France", "Sweden", "England"), nomatch=0)) car.test.frame[gfse.]`
13. `mat34 <- matrix(rep(c(4, 6, 3), 4), nrow=3, ncol=4)`
14. `mat64 <- matrix(c(rep(4, 8), rep(6, 7), rep(3, 9)), nrow=6, ncol=4) mat64[3:6, 3:4]`

Additional solutions will be included in later versions of this document.