

# THE SOLUTION OF SINGULAR-VALUE AND SYMMETRIC EIGENVALUE PROBLEMS ON MULTIPROCESSOR ARRAYS

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## ABSTRACT

Parallel Jacobi-like algorithms are presented for computing a singular-value decomposition of an  $m \times n$  matrix ( $m \geq n$ ) and an eigenvalue decomposition of an  $n \times n$  symmetric matrix. A linear array of  $O(n)$  processors is proposed for the singular-value problem; the associated algorithm requires time  $O(mnS)$ , where  $S$  is the number of sweeps (typically  $S \leq 10$ ). A square array of  $O(n^2)$  processors with nearest-neighbour communication is proposed for the eigenvalue problem; the associated algorithm requires time  $O(nS)$ .

## COMMENTS

Only the Abstract is given here. The full paper appeared as [6], which combined results in the earlier reports [1, 2]. For related work and generalisations, see [3, 4, 5]. It is conjectured in [6, page 83] that  $S(n) = O(\log n)$ .

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