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**A Warning Note:**

A big computer, a complex algorithm and a long time does not equal science.  
 [Robert Gentleman, SSC 2003, Halifax, June 2003]